Quantifying cooperative intermolecular interactions for improved carbon dioxide capture materials

Katrina M. de Lange and Joseph R. Lane^{a)}
Department of Chemistry, University of Waikato, Private Bag 3105, Hamilton 3240, New Zealand
(Received 25 May 2011; accepted 20 July 2011; published online 11 August 2011)

We have optimized the geometry and calculated interaction energies for over 100 different complexes of CO₂ with various combinations of electron accepting (Lewis acid) and electron donating (Lewis base) molecules. We have used the recently developed explicitly correlated coupled cluster singles doubles and perturbative triples [CCSD(T)-F12] methods and the associated VXZ-F12 (where X = D,T,Q) basis sets. We observe only modest changes in the geometric parameters of CO₂ upon complexation, which suggests that the geometry of CO₂ adsorbed in a nanoporous material should be similar to that of CO₂ in gas phase. When CO₂ forms a complex with two Lewis acids via the two electron rich terminal oxygen atoms, the interaction energy is less than twice what would be expected for the same complex involving a single Lewis acid. We consider a series of complexes that exhibit simultaneous CO₂-Lewis acid and CO₂-Lewis base intermolecular interactions, with total interaction energies spanning 14.1–105.9 kJ mol⁻¹. For these cooperative complexes, we find that the total interaction energy is greater than the sum of the interaction energies of the constituent complexes. Furthermore, the intermolecular distances of the cooperative complexes are contracted as compared to the constituent complexes. We suggest that metal-organic-framework or similar nanoporous materials could be designed with adsorption sites specifically tailored for CO2 to allow cooperative intermolecular interactions, facilitating enhanced CO₂ adsorption. © 2011 American Institute of Physics. [doi:10.1063/1.3624363]

INTRODUCTION

Any serious effort to reduce anthropogenic carbon dioxide (CO_2) emissions must contend with the geopolitical and economic reality that fossil fuels will continue to make a dominant contribution to the world's energy supply for decades to come. This makes development of scalable, cost-effective CO_2 capture technologies of equal importance to innovations in renewable energy resources over the near future. Furthermore, captured CO_2 is potentially a cheap and green carbon source that can be converted into a variety of valuable organic molecules. $^{3-5}$

Metal organic framework (MOF) materials are a relatively new class of nanoporous crystalline compounds that demonstrate promising ability as physical adsorbents for the separation of gases, including CO₂ (see, for example, Refs. 6–9). However, current MOF materials do not yet show the necessary selectivity for CO₂ from combustion exhaust gas mixtures. 10 In particular, very little is known about adsorption of CO₂ in the presence of H₂O, the co-product of combustion.^{1,11} CO₂ has previously been found to bind to MOF materials at either electron deficient open metal adsorption sites via the electron rich terminal oxygen atom^{12–14} or to electron rich adsorption sites via the electron deficient central carbon atom. 9,15, 16 We propose that MOF adsorption sites which allow simultaneous interaction of the electron rich terminal oxygen atoms and the electron deficient central carbon atom of CO₂ could be designed to exploit so-called cooper-

The use of supercritical CO₂ as a "green solvent" for industrial processes has resulted in a number of recent experimental¹⁷⁻²¹ and theoretical¹⁸⁻²⁴ investigations concerning the fundamental intermolecular interactions of CO₂. For molecules containing carbonyl functional groups, CO2 demonstrates simultaneous Lewis acid-Lewis base $R_2C=O\cdots CO_2$ and hydrogen bonding interactions $CH \cdot \cdot \cdot O = C = O.^{17,20,21,24}$ These two simultaneous intermolecular interactions work cooperatively to strengthen the total interaction.¹⁷ Similar cooperative intermolecular interactions have also been observed for CO2 complexes with dimethyl ether and 1,2,dimethoxyethane $[(CH_3)_2O\cdots CO_2 \text{ and } CH\cdots O=C=O],^{19,21} \text{ small fluori-}$ nated alkanes (RF···CO₂ and CH···O=C=O), 22 and various nitrogen containing Lewis bases (N···CO2 and CH···O=C=O). 25,26 These previous works conclusively demonstrate that CO2 is able to form cooperative intermolecular interactions but they do not quantify the strength of the individual Lewis acid-Lewis base or hydrogen bonding interactions. As a consequence, it is not yet known how strongly cooperative interactions affect the total interaction energy and intermolecular distance(s) of CO₂ complexes.

In the present work, we investigate over 100 different complexes involving CO_2 with various combinations of electron accepting (Lewis acid) and electron donating (Lewis base) molecules. We consider a range of different donor and acceptor molecules of various strengths that contain first and second row elements. We optimize the geometry and

ative intermolecular interactions, increasing the total adsorption strength.

a) Electronic mail: jlane@waikato.ac.nz.

calculate the interaction energy for each complex using explicitly correlated coupled cluster methods. We impose a few minor geometric constraints on the complexes to simplify interpretation of the intermolecular interactions and to allow more systematic investigation of the nature of cooperative interactions involving CO₂. Our primary objective is to quantify the effect of cooperative interactions on the adsorption strength and optimal intermolecular distance(s) for CO₂ complexes to ultimately facilitate a more rational design of MOF materials with adsorption sites specifically tailored for CO₂. The present work complements some recent DFT and MP2 studies that have investigated the interactions of CO₂ with potential organic framework linker molecules.

THEORETICAL METHODS

We have optimized the geometries of all complexes and their constituent monomers using the explicitly correlated CCSD(T)-F12 methods as implemented in MOLPRO 2010.1 (Refs. 29 and 30) and the VXZ-F12 (where X=D,T,Q) orbital basis sets. Recently, we showed that interaction energies and intermolecular distances of weakly bound complexes obtained with this approach are in excellent agreement with the CCSD(T)/CBS limit. 32,33

Density fitting approximations 34,35 and the resolution of the identity approximation were utilized in all explicitly correlated calculations with the default auxiliary basis sets $^{36-38}$ for all atoms except Li. For Li, the def2-TZVPP/JKFIT auxiliary basis set was used. The default complementary auxiliary basis set singles correction was applied, 29 which substantially improves the accuracy of the Hartree-Fock (HF) contributions particularly with smaller orbital basis sets. 39 The diagonal, fixed amplitude 3C(FIX) ansatz was used, which is orbital invariant, size consistent, and free of geminal basis set superposition error. $^{40-42}$ The default CCSD-F12 correlation factor $[(1/\beta)e^{-\beta r_{12}}]$, where $\beta = 1$ was used in all explicitly correlated calculations. We have not scaled the triples contribution in our CCSD(T)-F12 calculations.

Unless specified all coupled cluster calculations assume a frozen core (B:1s, C:1s; N:1s; O:1s; F:1s; P:1s,2s,2p; S:1s,2s,2p; Cl:1s,2s,2p) and were performed using MOLPRO 2010.1.³⁰ The optimization threshold criteria were set to: gradient = 1×10^{-6} a.u., stepsize = 1×10^{-6} a.u., energy = 1×10^{-8} a.u. All single point energies were converged to 1×10^{-9} a.u.

We calculate atomic charges using the natural bond orbital (NBO) analysis in GAUSSIAN 09 with the B3LYP/aug-cc-pVTZ method using the CCSD(T)-F12a/VDZ-F12 optimized geometries.⁴³

RESULTS AND DISCUSSION

As shown in Fig. 1, CO_2 is able to form simultaneous intermolecular interactions via the electron rich terminal oxygen atoms $(O \cdot \cdot \cdot X)$ and the electron deficient central carbon atom $(C \cdot \cdot \cdot Y)$. These simultaneous interactions work cooperatively such that the total interaction energy of a complex is different to the sum of the individual parts. Within this context, we define the magnitude of the coop-

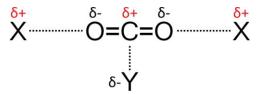


FIG. 1. A simplified model of simultaneous intermolecular interactions in X_2 – CO_2 –Y complexes.

erative interaction as being the difference (either positive or negative) between the interaction energy of the total complex and the interaction energy of the constituent individual complexes. For example, if the interaction energy of X₂-CO₂-Y was 40 kJ mol⁻¹ and the interaction energies of X_2 - CO_2 and CO_2 -Y were 20 and 15 kJ mol⁻¹, respectively, the magnitude of the cooperative interaction would be $+5 \,\mathrm{kJ} \,\mathrm{mol}^{-1}$. It is important to note that our definition of cooperative interaction assumes that the effect of basis set superposition error (BSSE) is negligible. While this requirement can not be satisfied with any finite basis set, the magnitude of BSSE obtained with explicitly correlated CCSD(T)-F12 methods is much smaller than with conventional CCSD(T).³³ For example, the difference between the interaction energy of H₂O-CO₂ obtained with and without counterpoise correction is 0.8 kJ mol⁻¹ for CCSD(T)-F12a/VDZ-F12 and 3.2 kJ mol⁻¹ for CCSD(T)/aug-cc-pVDZ. The difference in the corresponding optimized intermolecular distance of H₂O-CO₂ obtained with and without counterpoise correction is 0.013 Å for CCSD(T)-F12a/VDZ-F12 and 0.089 Å for CCSD(T)/aug-cc-pVDZ. Furthermore, the absolute values of the non-counterpoise corrected CCSD(T)-F12a/VDZ-F12 interaction energy (12.4 kJ mol⁻¹) and intermolecular distance (2.761 Å) for H₂O-CO₂ are in better agreement with the CCSD(T)/CBS limits (12.2 kJ mol⁻¹ and 2.755 Å) than the counterpoise corrected values (11.5 kJ mol⁻¹ and 2.774 Å).³³ Finally, it should also be noted that the magnitude of the cooperative interaction in the electronic energy of our model adsorption site will not necessarily be the same as the magnitude of the cooperative interaction for the enthalpy of adsorption (ΔH_{ads}) of a bulk MOF material that incorporates the same adsorption site. This work, therefore, is a "proof of concept" that cooperative intermolecular interactions may facilitate enhanced CO₂ adsorption in MOF or similar nanoporous materials.

$(HF)_n$ - CO_2

We begin by investigating the suitability of the CCSD(T)-F12 methods to accurately calculate interaction energies and hence the magnitude of cooperative interactions in a model system consisting of $(HF)_n$ – CO_2 (where n=1-4,6). We consider two CO_2 -Lewis acid complexes with either 1 or 2 HF molecules forming hydrogen bond(s) with the electron rich terminal oxygen atom(s) of CO_2 and three CO_2 -Lewis base complexes with either 1, 2, or 4 HF molecules interacting via the electron rich fluorine atom(s) and the electron deficient central carbon atom of CO_2 . We also consider three cooperative complexes in which two HF molecules form hydrogen

TABLE I. CCSD(T)-F12 interaction energies (in kJ mol⁻¹) for $(HF)_n$ -CO₂.^a

	VDZ-F12		VTZ-F12		VQZ-F12		
	F12a	F12b	F12a	F12b	F12a	F12b	
CO ₂ -Lewis a	cid comple	xes:b					
(HF) – CO_2	12.11	12.00	12.22	12.24	12.16	12.19	
$(HF)_2$ - CO_2	20.18	20.00	20.39	20.43	20.26	20.32	
CO ₂ -Lewis base complexes: ^c							
(HF) – CO_2	5.60	5.50	5.51	5.49	5.47	5.47	
$(HF)_2$ - CO_2	9.60	9.42	9.39	9.36	9.34	9.33	
$(HF)_4$ – CO_2	10.99	10.67	10.55	10.51	10.50	10.50	
Cooperative complexes:							
$(HF)_3$ – CO_2	32.62	32.29	32.77	32.80	32.60	32.65	
$(HF)_4$ - CO_2	43.24	42.78	43.30	43.30	43.10	43.15	
$(HF)_6$ – CO_2	57.12	56.43					
Cooperative interaction ^d							
$(HF)_3$ - CO_2	+6.83	+6.79	+6.88	+6.87	+6.87	+6.87	
$(HF)_4$ - CO_2	+13.45	+13.36	+13.52	+13.52	+13.51	+13.51	
$(HF)_6$ – CO_2	+25.94	+25.76					

^a All interaction energies are determined at the corresponding optimized geometry.

bonds to the two oxygen atoms of CO_2 and either 1, 2, or 4 HF molecules interact via the fluorine atom(s) with the central carbon atom of CO_2 . Representative images of all $(HF)_n$ – CO_2 (where n = 1-4,6) complexes optimized with the CCSD(T)-F12a/VDZ-F12 method are included in Fig. S1 of the supplementary material.⁴⁴

In Table I, we present CCSD(T)-F12a and CCSD(T)-F12b interaction energies for $(HF)_n$ – CO_2 (where n = 1-4,6) obtained with the VDZ-F12, VTZ-F12 and VQZ-F12 basis sets. We have previously found that CCSD(T)-F12b/VQZ-F12 interaction energies are in exceptionally good agreement with the CCSD(T)/CBS limit so we consider this the benchmark for comparison.^{32,33} Overall, we find that the calculated interaction energies converge as the cardinal number of the basis set increases from VDZ-F12 to VQZ-F12, although there is some small oscillation in some of the results. We find there to be relatively small differences between the CCSD(T)-F12a and CCSD(T)-F12b interaction energies obtained with a given basis set and not surprisingly these differences are largest for the VDZ-F12 basis set and smallest for the VQZ-F12 basis set. As some of the complexes considered in the subsequent subsections are relatively large, we are, however, restricted to use of the VDZ-F12 basis set. We find that interaction energies of the CO₂-Lewis acid complexes are slightly underestimated with the VDZ-F12 basis set whereas interaction energies of the CO2-Lewis base complexes are slightly overestimated. For both types of complexes, these discrepancies become larger as the number of HF molecules increases. Interestingly, the CCSD(T)-F12a method appears to better describe the CO₂-Lewis acid complexes and the CCSD(T)-F12b method appears to better describe the CO₂-Lewis base complexes with the VDZ-F12 basis set. For the cooperative complexes where both types of intermolecular interactions are present, the CCSD(T)-F12a/VDZ-F12 interaction energies are appreciably closer to the CCSD(T)-F12b/VQZ-F12b results as compared to the CCSD(T)-F12b/VDZ-F12 interaction energies. As a consequence, we find that the magnitude of the cooperative interaction determined with CCSD(T)-F12a/VDZ-F12 method is slightly (<0.1 kJ mol⁻¹ difference) more accurate than if determined with the CCSD(T)-F12b/VDZ-F12 method. This result is consistent with other theoretical investigations that recommend use of the CCSD(T)-F12a method with smaller VDZ-F12 and VTZ-F12 basis sets and use of the CCSD(T)-F12b method with the larger VQZ-F12 basis set.32,45 It follows that all geometry optimizations and interaction energies in the rest of this investigation are determined using the CCSD(T)-F12a/VDZ-F12 method. This method is expected to give interaction energies for all three types of complexes and the magnitude of the cooperative interaction to within a few tenths of a kJ mol⁻¹ of the CCSD(T)-F12b/VQZ-F12 result.

CO₂-Lewis acid complexes

In Table II, we present CCSD(T)-F12a/VDZ-F12 interaction energies, optimized intermolecular distances, and the magnitude of the cooperative interaction for a series of X_n - CO_2 (where n = 1 or 2) complexes. We consider 20 Lewis acid molecules that bind to CO₂ via O···X interactions involving four different electron deficient atoms (H, Li, B, Al). In Fig. 2, we show a representative image of the $(H_2O)_2$ - CO_2 complex with the optimized geometries of all other X-CO₂ and X₂-CO₂ complexes given in Figs. S2-S4 of the supplementary material.⁴⁴ As our primary motivation is to ascertain the effect of "cooperative interactions" on CO₂, we have introduced some minor geometric constraints to simplify this interpretation. We assume that all diatomic and linear molecules bind CO₂ in a linear fashion with either $C_{\infty v}$ (X=1) or $D_{\infty h}$ (X = 2) symmetry. For the polyatomic hydrogen bonding molecules, we restrict the hydrogen bond to be linear [e.g., $\theta(C=O\cdots H)$ and $\theta(O\cdots HO)$ of H_2O-CO_2 are 180°] and orientate the two X molecules to be on the opposite side to each other to minimize any potential $X \cdots X$ interactions. For the boron and aluminum hydrides and halides, we assume that the $\theta(C=O\cdots B)$ or $\theta(C=O\cdots Al)$ angle is linear and that the two electron deficient groups are in a staggered orientation (D_{3h} symmetry). All other geometric parameters are optimized.

As expected, there are only modest differences between the geometric parameters of CO_2 as a monomer and in the $X-CO_2$ and X_2-CO_2 complexes. For $X-CO_2$, we find that the bonded $R(C=O)_b$ distance is slightly elongated and the free $R(C=O)_f$ distance is slightly contracted, as compared to R(C=O) in CO_2 monomer. Furthermore, there is a strong correlation between the interaction energy of a complex and the values of both $R(C=O)_b$ and $R(C=O)_f$ (Figs. S5 and S6 of the supplementary material).⁴⁴ These results are consistent with the Lewis acid essentially polarizing the CO_2 molecule so that electron density moves from a non-bonding orbital of the free C=O group into an anti-bonding orbital of the bonded C=O group (Table S1 of the supplementary material).⁴⁴ In

^bComplexes where CO₂ acts as an electron donor.

^cComplexes where CO₂ acts as an electron acceptor.

^dDifference between the interaction energy of a cooperative complex and the interaction energy of the constituent CO₂-Lewis acid and CO₂-Lewis base complexes. See text for details.

TABLE II. CCSD(T)-F12a/VDZ-F12 interaction energies (in kJ mol⁻¹) and selected geometric parameters (in Å) for a series of CO_2 -Lewis acid complexes.

X-CO ₂			X ₂ -CO ₂				
Molecule	Int. energy	$R(O\cdots X)^a$	Int. energy	$R(O\!\cdots\!X)^a$	$R(X \cdot \cdot \cdot X)^b$	Coop. Int. ^c	
HNC	12.4	2.058	19.6	2.123	6.568	-5.1	
HF	12.1	1.981	20.2	2.037	6.395	-4.0	
НСООН	10.5	2.071	18.7	2.114	6.551	-2.3	
C_4H_5N	8.6	2.217	15.2	2.255	6.835	-2.1	
HCN	8.3	2.269	13.5	2.324	6.973	-3.1	
ОН	8.2	2.182	14.2	2.228	6.779	-2.2	
HCl	7.9	2.217	14.2	2.256	6.836	-1.6	
CH ₃ OH	7.4	2.200	13.6	2.252	6.786	-1.3	
H_2O	7.0	2.221	12.5	2.252	6.828	-1.4	
C_6H_6	3.1	2.603	6.1	2.605	7.536	-0.0	
CH ₄	1.7	2.743	3.4	2.744	7.815	-0.0	
LiCl	37.2	1.990	43.3	2.093	6.504	-31.1	
LiH	32.4	2.008	39.8	2.104	6.526	-25.1	
LiF	31.4	2.028	37.7	2.127	6.572	-25.1	
BF_3	9.9	2.674	18.5	2.706	7.736	-1.3	
BH_3	8.4	2.518	16.0	2.550	7.423	-0.8	
BCl ₃	7.3	3.042	14.7	3.044	8.413	+0.1	
AlF_3	50.8	2.027	67.8	2.167	6.646	-33.7	
AlCl ₃	37.2	2.065	47.4	2.290	6.896	-27.1	
AlH ₃	24.5	2.229	36.7	2.385	7.088	-12.3	

^aDistance from the electron rich oxygen atom of CO₂ to the electron deficient atom of the acceptor molecule.

contrast we find that the $R(C=O)_b$ distance for X_2 - CO_2 is actually contracted as compared to R(C=O) in CO_2 monomer. We attribute this result to electron density transfer from the non-bonding orbitals of CO_2 to the electron deficient atom of the Lewis acid (Table S1 of the supplementary material).⁴⁴ The value of $R(C=O)_b$ for X_2 - CO_2 is again very well correlated with the interaction energy of the complex and is shortest for strongly bonded complexes (Fig. S7 of the supplementary material).⁴⁴

With exception of the BCl_3 results, we find that the cooperative interaction of all X_2 – CO_2 complexes is negative. That is the total interaction energy is less than two times the interaction energy of the X– CO_2 complex. This result can be rationalized by considering the atomic charges of oxygen atoms of CO_2 from NBO analysis (Table S1 of the supplementary material). Upon forming the X– CO_2 complex, the non-bonded oxygen atom of CO_2 becomes less electron rich and is hence less attractive to the electron deficient atom of the second X molecule in X_2 – CO_2 . The magnitude of the cooperative interaction is well correlated with the interaction energy of X– CO_2 and is large for strongly bound complexes such as $(AlF_3)_2$ – CO_2 and small for weakly bound complexes such

as $(CH_4)_2$ – CO_2 (Fig. S8 of the supplementary material).⁴⁴ We find that the $R(O \cdot \cdot \cdot X)$ intermolecular distance for X_2 – CO_2 is longer than for X– CO_2 and this difference can be thought of as the primary geometric effect of the cooperative interactions. The difference between $R(O \cdot \cdot \cdot X)$ for X_2 – CO_2 and X– CO_2 correlates reasonably well with the magnitude of the cooperative interaction (Fig. S9 of the supplementary material).⁴⁴ This correlation is more pronounced if the results of the very strongly bonded lithium and aluminum hydrides and halides are excluded (Fig. S10 of the supplementary material).⁴⁴

The optimized $R(X \cdots X)$ distances for X_2 – CO_2 shown in Table II represent the optimal dimensions for a CO_2 adsorption site based on two equivalent electron deficient atoms through $O \cdots X$ intermolecular interactions. We find that there is considerable variation in the $R(X \cdots X)$ distance even for the same atom type (H,Li,B,AI) and hence it is not reasonable to generalize the optimal dimensions of an adsorption site based purely on the immediate atom of interaction $O \cdots X$. For example, $R(X \cdots X)$ is 6.395 Å for HF_2 – CO_2 and 7.815 Å for $(CH_4)_2$ – CO_2 despite both molecules binding through an electron deficient hydrogen atom.

In Table III.

FIG. 2. The CCSD(T)-F12a/VDZ-F12 optimized geometry of (H₂O)₂-CO₂.

CO₂-Lewis base complexes

In Table III, we present CCSD(T)-F12a/VDZ-F12 interaction energies, optimized intermolecular distances and the OCO angle of CO_2 for a series of CO_2 -Y complexes. We consider 29 different Lewis base molecules that bind to CO_2 via $C \cdot \cdot \cdot Y$ interactions involving seven different electron rich atoms (C, N, O, F, P, S, and Cl). Each complex adopts

^bDistance between the electron deficient atoms of the two acceptor molecules.

^cInteraction energy of X₂-CO₂ subtract interaction energy of two times the X-CO₂ interaction energy.

TABLE III. CCSD(T)-F12a/VDZ-F12 interaction energies (in kJ mol^{-1}) and selected geometric parameters (in Å and degrees) for a series of CO₂-Lewis base complexes.

Molecule	Int. energy	$R(C{\cdot}\cdot{\cdot}Y)^{{\boldsymbol a}}$	$\theta(OCO)$	Molecule	Int. energy	$R(C\!\cdots\!Y)^{\boldsymbol{a}}$	$\theta(OCO)$
	C-do	nor					
$C_3H_4N_2^b$	19.2	2.900	175.6				
HNC	8.7	3.117	178.5				
	N-do	nor			P-do	onor	
$C_5H_5N^b$	18.5	2.751	176.3				
$N(CH_3)_3^b$	18.3	2.778	176.3				
$C_4H_4N_2^b$	16.6	2.787	177.3				
NH ₃ ^b	12.8	2.926	177.5	PH_3	6.3	3.536	179.2
CH ₃ CN	10.6	2.936	178.1				
HCN	8.9	2.976	178.5	HCP	2.3	3.670	180.1
FCN	8.4	2.981	178.7				
CH_2N_2	7.6	2.967	179.1				
	O-do	nor			S-do	onor	
O(CH ₃) ₂ ^b	17.2	2.660	177.6				
OPH ₃	13.6	2.756	177.6				
$C_4H_4O^b$	12.5	2.760	178.8	$C_4H_4S^a$	6.3	3.536	179.7
H_2O	12.4	2.761	178.2				
(CH ₃) ₂ CO	12.1	2.765	178.2				
CH ₂ O	9.8	2.811	178.6	CH_2S	2.3	3.387	179.9
OPF ₃	9.4	2.843	178.6				
CF ₂ O	7.0	2.891	179.2				
CH_2CO	6.8	2.901	179.2				
F-donor				Cl-donor			
LiF	20.6	2.565	175.5	LiCl	10.7	3.228	178.0
CH ₃ F	7.1	2.825	179.0	CH ₃ Cl	3.2	3.430	179.8
HF	5.6	2.874	179.2	HCl	1.8	3.527	180.1

^aDistance from the electron deficient carbon atom of CO₂ to the electron rich atom of the donor molecule.

either a symmetric "t-shape" structure with both C=O bonds of CO_2 equivalent (e.g., $C_3H_4N_2$) or an asymmetric "t-shape" structure with the two C=O bonds approximately equivalent [e.g., $N(CH_3)_3$]. In Fig. 3, we show a representative image of the CO_2 - C_5H_5N complex with the optimized geometries of all other CO_2 -Y complexes given in Figs. S11-S13 of the supplementary material.⁴⁴

It is worth noting that many of the complexes that have large interaction energies already exhibit cooperative intermolecular interactions via hydrogen bonding (OCO···H) to hydrogen atoms adjacent to the electron rich atom. For example, $C_3H_4N_2$, C_5H_5N , $N(CH_3)_3$, NH_3 , $C_4H_4N_2$, $O(CH_3)_2$, and C₄H₄O. This perhaps complicates the interpretation of the strength of the "cooperative interactions" in Table IV (vide infra) as the net effect of simultaneous OCO···H and O···X interactions will likely result in a small positive cooperative effect (Table II). As expected, we find that the interaction energies of the complexes involving second row electron rich atoms (P, S, Cl) are generally not as strong as their first row equivalents. This suggests that first row electron rich atoms are a better choice for design of an adsorption site that strongly binds CO₂ via the electron deficient central carbon atom.

Overall, there are modest changes in the geometric parameters of CO₂ upon formation of the CO₂–Y complexes.



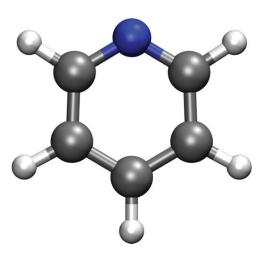


FIG. 3. The CCSD(T)-F12a/VDZ-F12 optimized geometry of CO₂-C₅H₅N.

^bHydrogen atoms adjacent to the primary interaction site permit additional hydrogen bonding interactions to the oxygen atoms of CO₂.

TABLE IV. CCSD(T)-F12a/VDZ-F12 interaction energies (in kJ mol⁻¹) and selected geometric parameters (in Å) for cooperatively bonded complexes of the type (HF)₂-CO₂-Y.

Molecule	Int. energy	Coop.	Enhancement ^b	ΔR $(O \cdot \cdot \cdot H)^c$	ΔR $(C \cdots Y)^d$
LiF	66.3	+25.5	63%	-0.137	-0.148
$C_3H_4N_2$	58.8	+19.3	49%	-0.142	-0.175
C_5H_5N	52.1	+13.4	34%	-0.109	-0.110
LiCl	48.4	+17.5	57%	-0.080	-0.171
$O(CH_3)_2$	47.7	+10.3	28%	-0.090	-0.072
$C_4H_4N_2$	46.9	+10.1	27%	-0.098	-0.086
$(CH_3)_2CO$	45.4	+13.1	41%	-0.078	-0.115
H_2O	42.4	+9.8	30%	-0.072	-0.078
CH_2O	40.1	+10.1	34%	-0.063	-0.104
HCN	39.5	+10.4	36%	-0.061	-0.121
HNC	39.0	+10.2	35%	-0.060	-0.123
C_4H_4O	38.8	+6.1	19%	-0.067	-0.054
FCN	37.9	+9.3	33%	-0.058	-0.116
CH_2N_2	34.6	+8.6	33%	-0.047	-0.096
CF_2O	33.3	+6.1	22%	-0.044	-0.091
CH_2CO	33.2	+7.3	28%	-0.042	-0.098
HF	32.6	+6.8	26%	-0.041	-0.109
C_4H_4S	29.9	+3.4	13%	-0.032	-0.247
HCl	23.8	+1.8	8%	-0.004	-0.111
HCP	22.8	+0.4	2%	-0.003	-0.034

^aThe interaction energy of (HF)₂−CO₂−Y subtract the interaction energy of (HF)₂−CO₂ and CO₂−Y.

We find that the R(C=0) bond distance becomes slightly elongated and this is attributed to electron density from the Lewis base transferring into anti-bonding CO₂ orbitals (Table S2 of the supplementary material).⁴⁴ With exception of CO₂-HCP and CO₂-HCl, we find that the obtuse angle $(<180^{\circ})$ of CO₂ is orientated on the opposite side of CO₂ to Y. Even for the strongest Lewis bases, we find that $\theta(OCO)$ is >175°, which indicates that CO₂ should remain largely linear upon adsorption in MOF materials via C···Y interactions. This result corroborates recent findings by Wu et al. that large apparent variations in the value of $\theta(OCO)$ for MOF materials with CO₂ adsorbed are due to the high orientational disorder of CO₂ in the crystal structures rather than any actual chemical changes in CO₂.46 We find that the θ (OCO) angle exhibits a clear correlation with the interaction energy, whereas the R(C=O) bond distance exhibits a weaker correlation (Figs. S14 and S15 of the supplementary material).44

Similar to what was observed in Table II, there is significant variation in the intermolecular distance $R(C \cdot \cdot \cdot Y)$ for a given electron rich atom. For example, $R(C \cdot \cdot \cdot Y)$ is 2.660 Å for CO_2 – $C(CH_3)_2$ and 2.901 Å for CO_2 – CH_2CO despite both molecules binding through an electron rich oxygen atom. It follows that the optimal $R(C \cdot \cdot \cdot Y)$ distance for constructing a CO_2 adsorption site cannot be generalized based on the immediate atom of interaction.

TABLE V. CCSD(T)-F12a/VDZ-F12 interaction energies (in kJ mol $^{-1}$) and selected geometric parameters (in Å) for cooperatively bonded complexes of the type X_2 –CO $_2$ –CH $_2$ O.

Molecule	Int. energy	Coop.	Enhancement ^b	ΔR $(O \cdot \cdot \cdot X)^c$	ΔR $(C \cdots O)^d$
AlF ₃	105.9	+28.3	37%	-0.056	-0.291
LiCl	83.7	+30.7	58%	-0.062	-0.211
LiH	76.5	+26.9	54%	-0.059	-0.198
LiF	74.4	+26.9	57%	-0.062	-0.192
AlH_3	64.0	+17.5	38%	-0.108	-0.211
HNC	41.1	+11.7	40%	-0.073	-0.101
HF	40.1	+10.1	34%	-0.063	-0.104
HCOOH	35.3	+6.7	24%	-0.062	-0.061
BF ₃	34.6	+6.3	22%	-0.066	-0.085
HCN	32.5	+9.2	39%	-0.082	-0.072
OH	31.7	+7.6	32%	-0.071	-0.073
BH_3	31.0	+5.2	20%	-0.085	-0.080
HCl	31.0	+7.0	29%	-0.073	-0.073
CH ₃ OH	29.8	+6.6	28%	-0.059	-0.082
H_2O	28.9	+6.6	29%	-0.062	-0.080
CH ₄	14.1	+0.9	7%	-0.050	-0.013

 $[^]a The$ interaction energy of $X_2\text{--}CO_2\text{--}CH_2O$ subtract the interaction energy of $X_2\text{--}CO_2$ and $CO_2\text{--}CH_2O$.

Cooperative complexes

In Tables IV and V, we present CCSD(T)-F12a/VDZ-F12 results for two sets of cooperative complexes, namely, (HF)₂-CO₂-Y and X₂-CO₂-CH₂O. It is not computationally practicable to evaluate all possible combinations of X and Y considered in this investigation with the CCSD(T)-F12a/VDZ-F12 method. Hence, to illustrate the effects of cooperative intermolecular interactions we consider just one electron acceptor (HF) with various electron donors and one electron donor (CH₂O) with various electron acceptors. The linear structure of the (HF)₂-CO₂ complex and the perpendicular orientation of CH₂O relative to the "t-shape" plane of the CO₂-CH₂O complex, minimize potentially confounding $X \cdots Y$ intermolecular interactions. The geometry of $(HF)_2$ -CO₂-CH₂O is shown in Fig. 4 to illustrate the general structure of the cooperative complexes considered with the optimized geometries of all other X₂-CO₂-CH₂O and (HF)₂-CO₂-Y complexes given in Figs. S16-S20 of the supplemen-

To limit the computational expense of the $(HF)_2$ – CO_2 –Y calculations, we consider only electron donor molecules that permit C_{2v} symmetry for the cooperative complex. We find that the total interaction energy of these complexes varies from 66.3 kJ mol $^{-1}$ with the strong electron donor LiF to 22.8 kJ mol $^{-1}$ with the weak electron donor HCP. This wide range is important as it shows that the adsorption energy for a X_2 – CO_2 –Y type adsorption site can be readily tuned for optimal adsorption/desorption processes by varying the electron donor functional group. We find that the cooperative interactions of all $(HF)_2$ – CO_2 –Y complexes are positive, with the total interaction energy larger than the sum of the individual

^bPercentage increase in the interaction energy of (HF)₂–CO₂–Y compared with the interaction energy of CO₂–Y.

 $^{^{}c}R(O \cdot \cdot \cdot H)$ of $(HF)_{2}$ – CO_{2} –Y subtract $R(O \cdot \cdot \cdot H)$ of $(HF)_{2}$ – CO_{2} .

 $^{{}^}dR(C\cdots Y)$ of $(HF)_2$ - CO_2 -Y subtract $R(C\cdots Y)$ of CO_2 -Y.

^bPercentage increase in the interaction energy of X₂–CO₂–CH₂O compared with the interaction energy of X₂CO₂.

 $^{^{}c}R(O \cdot \cdot \cdot X)$ of X_2 - CO_2 - CH_2O subtract $R(O \cdot \cdot \cdot X)$ of X_2 - CO_2 .

 $^{{}^}dR(C \cdot \cdot \cdot O)$ of X_2 – CO_2 – CH_2O subtract $R(C \cdot \cdot \cdot O)$ of CO_2 – CH_2O .

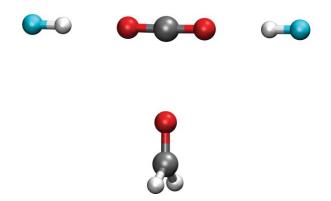


FIG. 4. The CCSD(T)-F12a/VDZ-F12 optimized geometry of (HF)₂–CO₂–CH₂O

interaction energies of the electron donor (CO_2-Y) and electron acceptor $[(HF)_2-CO_2]$ complexes. Again, we rationalize this result by considering the NBO atomic charges on CO_2 (Table S3 of the supplementary material).⁴⁴ The central carbon atom of $(HF)_2-CO_2$ is more electron deficient than in CO_2 monomer and hence is more attractive to the electron rich atom of Y. Correspondingly, the terminal oxygen atoms of the CO_2-Y complex are more electron rich than in CO_2 and hence are more attractive to the electron deficient hydrogen atoms of HF.

In general, we find that the magnitude of the cooperative interactions for $(HF)_2$ – CO_2 –Y is well correlated with total interaction energy and is large for the more strongly bound complexes and small for the more weakly bound complexes (Fig. S21 of the supplementary material).⁴⁴ The primary geometric effects of these cooperative interactions is to decrease both the $R(O\cdots H)$ and $R(C\cdots Y)$ intermolecular distances for $(HF)_2$ – CO_2 –Y as compared to the respective $(HF)_2$ – CO_2 and CO_2 –Y complexes. We find that $\Delta R(O\cdots H)$ correlates strongly with the magnitude of the cooperative interactions, whereas the correlation between $\Delta R(C\cdots Y)$ is much weaker (Figs. S22-S24 of the supplementary material).⁴⁴

For the X₂–CO₂–CH₂O complexes, we consider all electron acceptors from Table II except for C_4H_5N , C_6H_6 , BCl₃, and AlCl₃ as these were too computationally demanding with our present resources with the CCSD(T)-F12a/VDZ-F12 method. We again assume that the diatomic and linear X molecules bind CO₂ in a linear fashion with $\theta(C=O\cdots X)$ equal to 180°. For the polyatomic hydrogen bonding molecules, we also restrict the hydrogen bond to be linear and orientate the two X molecules to be on the opposite side to the Y molecule. Note that in this orientation, the two X molecules are on the same side as each other; whereas in Table II, the two X molecules were on opposite sides. For the boron and aluminum hydrides and halides, the $\theta(C=O\cdots B)$ or $\theta(C=O\cdots Al)$ angle is also restricted to be linear with the two electron deficient groups orientated in an eclipsed position with the in-plane hydrogen or halide trans to the CH_2O group to minimize potentially confounding $X \cdots Y$ intermolecular interactions. We have reoptimized the geometries of these "same side" and "eclipsed" X₂–CO₂ complexes and use these reoptimized results when determining the magnitude of the cooperative interactions and change in $R(O \cdot \cdot \cdot X)$ and $R(C \cdot \cdot \cdot Y)$ for X_2 – CO_2 – CH_2O .

We find that the total interaction energy of the X₂–CO₂– CH₂O complexes varies from 105.9 kJ mol⁻¹ with the strong electron acceptor AlF₃ to 14.1 kJ mol⁻¹ with the weak electron acceptor CH₄. The cooperative interactions of all X₂-CO₂–CH₂O complexes are positive, with the total interaction energy larger than the sum of the interaction energies of the constituent complexes. Similar to the (HF)₂–CO₂–Y results, the strength of the cooperative interactions for the X₂–CO₂– CH₂O complexes also appears well correlated with the total interaction energy (Fig. S25 of the supplementary material).⁴⁴ These two results are together important as it shows that the magnitude of cooperative interactions affecting CO2 binding in a potential adsorption site can be tuned via modification of either the electron poor (X) or the electron rich (Y) atoms. Again, the primary effect of these cooperative interactions on the geometry of X₂–CO₂–CH₂O is to decrease both the $R(O \cdot \cdot \cdot X)$ and $R(C \cdot \cdot \cdot O)$ intermolecular distances as compared to the respective X₂–CO₂ and CO₂–CH₂O complexes. Interestingly, we find that there is essentially no correlation between $\Delta R(O \cdot \cdot \cdot X)$ and the magnitude of the cooperative interactions whereas the correlation between $\Delta R(C \cdot \cdot \cdot O)$ is strong (Figs. S26 and S27 of the supplementary material).⁴⁴

If we consider the intermolecular distances of the $(HF)_2$ – CO_2 –Y and X_2 – CO_2 – CH_2O results collectively, we observe significant variation in the optimal $R(O\cdots X)$ and $R(C\cdots Y)$ distances for the different combinations of X and Y. This, in turn, suggests that when designing the optimal adsorption site for CO_2 it is important to consider the effect that cooperative interactions will have on the optimal dimensions of that site. It is worth noting that even if an adsorption site is not deliberately designed to exploit "cooperative interactions" these may still be present from adjacent atoms with potentially unwanted effects.

CONCLUSIONS

We have calculated the optimized geometry and interaction energy for over 100 different complexes containing CO₂ with various combinations of Lewis acids and bases using the explicitly correlated CCSD(T)-F12a/VDZ-F12 method. Our initial calculations on the model complexes (HF)_n-CO₂ (where n = 1-4,6) showed that this method generally gave interaction energies and the magnitude of the cooperative effect to within a few tenths of a kJ mol⁻¹ of the CCSD(T)-F12b/VQZ-F12 results.

Overall, we observe only modest changes in the geometric parameters of CO_2 upon formation of the various complexes considered in this work. This result indicates that the geometry of CO_2 adsorbed in a MOF material should be similar to that of CO_2 monomer. We find that when CO_2 interacts with a single electron deficient atom via one of the terminal oxygen atoms $(X-CO_2)$, the bonded $R(C=O_b)$ distance slightly elongates and the free $R(C=O_f)$ distance slightly contracts. However, when CO_2 interacts simultaneously with two electron deficient atoms via both terminal oxygen atoms (X_2-CO_2) , the two bonded $R(C=O_b)$ distances slightly contract. For the CO_2 -Lewis base complexes, we find that complexation causes a slight increase in the CO_2 bond distances

and a minor deviation from linearity ($< 5^{\circ}$) in the θ (OCO) angle.

The interaction energy of the X_2 – CO_2 complex is found to be less than twice the interaction energy of the X– CO_2 complex. In addition, the $R(O \cdot \cdot \cdot X)$ intermolecular distance for X_2 – CO_2 is found to be longer than for X_2 – CO_2 . These results are attributed to a decrease in the electron density of the non-bonded oxygen atom of X– CO_2 as compared to CO_2 monomer, which in turn makes the non-bonded oxygen atom less attractive to a second Lewis acid molecule.

We investigated two series of cooperative complexes [(HF)₂-CO₂-Y and X₂-CO₂-CH₂O] that exhibit simultaneous CO_2 -Lewis acid $(O \cdot \cdot \cdot X)$ and CO_2 -Lewis base $(C \cdot \cdot \cdot Y)$ intermolecular interactions. The interaction energy of these cooperative complexes was found to be larger than the sum of the interaction energies of the constituent X₂–CO₂ and CO₂–Y complexes. Furthermore, the $R(O \cdot \cdot \cdot X)$ and $R(C \cdot \cdot \cdot Y)$ intermolecular distances of the cooperative complexes were found to be shorter than the corresponding intermolecular distances of the constituent complexes. We rationalize these results by considering that formation of (HF)₂–CO₂ reduces the electron density on the central carbon atom of CO₂ making it more attractive to a Lewis base, whereas formation of CO₂–CH₂O increases the electron density on the terminal oxygen atoms of CO₂ making them more attractive to a Lewis acid. We find that the magnitude of this cooperative enhancement of the interaction energy and contraction of the intermolecular distances are correlated to the strength of the various Lewis acids and Lewis bases involved. It follows that the total adsorption strength and optimal dimensions of a MOF CO₂ binding site can in principle be tuned via modification of either electron deficient (X) or electron rich (Y) atoms.

ACKNOWLEDGMENTS

We thank Cameron J. Kepert for helpful discussions and the University of Waikato High Performance Computing Facility for computer time.

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