

1       **A novel machine learning method to investigate the web crippling**  
2       **behaviour of perforated roll-formed aluminium alloy unlippped**  
3       **channels under interior-two flange loading**

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9  
10   **Abstract:** This study presents a novel machine-learning model using the eXtreme Gradient  
11   Boosting (XGBoost) tool, for assessing the web crippling behaviour of perforated roll-formed  
12   aluminium alloy (RFA) unlippped channels (both fastened and unfastened) under interior-two-  
13   flange loading. A total of 1,080 data points were generated for training the XGBoost model,  
14   utilizing an elastoplastic finite element (FE) model that was validated against 30 experimental  
15   results from the literature. A comparison against the numerical failure loads was conducted,  
16   and it was found that the prediction accuracy of XGBoost model was 94%. When compared  
17   with Random Forest and Linear Regression methods, it was found that the proposed XGBoost  
18   model performed better than both the beforementioned methods. The web crippling strengths  
19   obtained from the XGBoost model, tests, and finite element analysis (FEA) were utilized to  
20   evaluate the performance of current design rules from the American Iron and Steel Institute  
21   (AISI), Australian/New Zealand Standards (AS/NZS 1664.1; AS/NZS 4600:2018) and  
22   Eurocode (CEN 2007). It is shown that the current design rules are not reliable to predict the  
23   web crippling strength of perforated RFA unlippped channels. As a consequence of the  
24   parametric analysis, new web crippling strength and web crippling strength reduction factor  
25   formulae for perforated RFA unlippped channels were proposed. A reliability analysis was then

26 conducted, which confirmed that the proposed equations are capable of accurately predicting  
27 the ITF web crippling strengths of perforated RFA unlipped channels.

28 **Keywords:** Web crippling, eXtreme Gradient Boosting (XGBoost) tool, Aluminium alloy,  
29 Unlipped channels, Finite element analysis, Machine learning, Parametric analysis, Interior-  
30 two-flange loading.

## 31 **1 Introduction**

32 Thin-walled structures are widely used in building construction, storage racks,  
33 transmission towers, automotive, ships and aircraft [1-12]. Carbon steel, stainless steel, and  
34 aluminium are the most common materials used in the construction of thin-walled structures.  
35 As a sustainable building material, aluminium alloy has recently gained popularity in the  
36 construction industry [13-16], and roll-formed aluminium alloy (RFA) channels are being used  
37 as beam members. The inclusion of web perforations in such RFA channels is often required  
38 to facilitate the electrical and plumbing services. However, no research on the web crippling  
39 behaviour of perforated RFA unlipped channels when subjected to interior-two-flange (ITF)  
40 loading is available in the literature. Furthermore, current design standards i.e., American Iron  
41 and Steel Institute [17], the Australian and New Zealand Standards (AS/NZS 1664.1; AS/NZS  
42 4600:2018) [18-19], as well as the Eurocode (CEN 2007) [20], do not include  
43 recommendations for perforated RFA unlipped channels under ITF loading. In this paper, a  
44 novel machine learning model using the eXtreme Gradient Boosting (XGBoost) tool is trained  
45 based on the validated elasto-plastic finite element (FE) model to investigate the interior-two  
46 flange (ITF) web crippling behaviour of perforated RFA unlipped channels (see Fig.1) and new  
47 design equations were proposed.

48 Limited research is available in the literature for the web crippling performance of  
49 perforated RFA unlipped channels. Previous research studies [21-28] have mainly focused on  
50 RFA lipped channels. The effect of lip on the stiffness of the flange, which would normally  
51 increase the web crippling strength, was often ignored, although there are few studies available  
52 in the literature which demonstrates the effect of lip and folded flanges on the stiffness of  
53 channel sections [29-32]. Furthermore, research into the effect of web holes on aluminium

54 alloy sections under web crippling is very limited. As a result, a thorough investigation on the  
55 web crippling behaviour of perforated RFA unlipped channels is required.

56 The web crippling behaviour of roll-formed carbon steel (RFCS) sections has been  
57 studied extensively. Bhakta et al. [33] investigated the enhancement of web crippling capacity  
58 from fastened supports of different RFCS sections. Similarly, Cain et al. [34] and Gerges and  
59 Schuster [35] examined the effects of fastened flanges on the web crippling behaviour. The  
60 web crippling strength of fastened sections was found to be over 30% higher than that of  
61 sections with unfastened flanges. These findings are in line with most of the recent results  
62 reported in the literature [36-49]. The design calculation methods from the standards are  
63 discussed in the literature [36-41], however, the proposed Direct Strength Method in the  
64 literature [36-41] are only available in predicting the web crippling strength of plain sections;  
65 Uzzaman et al. [42-49] therefore proposed new equations in the form of reduction factor  
66 equation to predict the web crippling strength of perforated cold-formed steel channels based  
67 on experimental and numerical studies.

68 Machine Learning (ML) is a useful method for identifying useful data features [50], and  
69 the use of ML to predict the trend of data has gained popularity in recent times [51-56].  
70 XGBoost is an effective ML tool, which is used for eXtreme Gradient Boosting. Compared  
71 with traditional gradient boosting algorithms, XGBoost is much faster while classifying and  
72 training the data.

73 This research has therefore proposed a XGBoost framework for investigating the ITF  
74 web crippling strength of perforated RFA unlipped channels. A nonlinear elasto-plastic finite  
75 element (FE) model was developed and validated against the experimental data available in the  
76 literature. A total of 1,080 data points were obtained for training the XGBoost utilizing the  
77 validated FE model. When the XGBoost predictions were compared to the web crippling

78 strengths of perforated RFA unlipped channels determined from the AISI 2016 [17] and  
79 AS/NZS 2018 [19], AS/NZS 1997 [18], and CEN 2007 [20], it was found that the XGBoost  
80 performs better. Additionally, the prediction accuracy of XGBoost was checked against the  
81 results of other ML methods, i.e., Random Forest and Linear Regression, and it was found that  
82 XGBoost outperformed the other two methods when predicting the web crippling strength of  
83 RFA unlipped channels. Based on the XGBoost output data, a parametric study was carried out  
84 and design equations for the reduced web crippling strength of RFA channels were proposed.  
85 Furthermore, a reliability analysis of the proposed equations confirmed that the proposed  
86 equations could closely predict the (reduced) ITF web crippling strength of RFA unlipped  
87 channels.

## 88 **2 Summary of experimental results reported by Fang et al. [57]**

89 Fang et al. [57] conducted 30 new experimental tests on perforated RFA lipped channels  
90 under ITF loading condition. The size and location of web perforations were altered to  
91 determine its influence on the web crippling behaviour of such channels. The test specimens  
92 had web holes placed at the centre and also offset longitudinally from the bearing plate. The  
93 specimens were labelled in such a manner that the label stated the nominal dimensions of the  
94 web, bearing length, hole position, hole size, and flange type. For instance, the label "ITF240-  
95 N50-DH-A0.6-FR" can be defined as follows: "ITF" represents the study's web crippling  
96 loading case; "240" denotes the nominal web depth in millimetres ( $d=240$  mm); "N50" denotes  
97 the bearing's length in millimetres ( $N=50$  mm); the abbreviations "NH", "DH", and "OH"  
98 denote the web hole status. "NH" indicates that there are no web holes, whereas "DH" and  
99 "OH" indicate that the web has a down hole and an offset hole, respectively; "A0.6" denotes  
100 the ratio of the hole diameter to the total web depth ( $a/h=0.6$ ). The final two notations "FR"  
101 and "FX" denote sections with unfastened and fastened flanges, respectively.

102 The test results of Fang et al. [57] were used in the current study to validate the FE models  
103 developed herein, as described in the following section. More details of the experiments and  
104 its results can be found in Fang et al. [57].

### 105 **3 Advanced finite element analysis (FEA)**

#### 106 *3.1 Development of the FE model*

107 The experimental behaviour was simulated numerically through a nonlinear nonlinear  
108 elasto-plastic FE model, which was developed using the software ABAQUS [58]. The material  
109 properties obtained from the tensile coupon tests [57] were input into the FE models. S4R shell  
110 elements (having a mesh size of 5 mm × 5 mm) were used in the FE modelling to model the  
111 RFA unlipped channels, and rigid quadrilateral shell elements (R3D4) were used to model the  
112 endplates. Fig.2 illustrates the details of FE meshing and the boundary conditions of the FE  
113 model.

114 The interface of bearing plate and the channel was modelled using the surface-to-surface  
115 contact option available in ABAQUS [58]. The target surface was the bearing plate, whereas  
116 the contact surface was selected to be the channel surface. No penetration of the two contact  
117 surfaces was permitted. The vertical load was applied to the channels through the reference  
118 node of the top bearing plate by means of displacement control load application procedure.  
119 Similar FE modelling techniques were also employed by Chi et al. [59], Chen et al. [60-63],  
120 Roy et al. [64-68], Fang et al. [69-74] and Yao and Li [75], and it should be noted that Fang et  
121 al. [74] have demonstrated that such modelling methods are feasible for simulating both  
122 unlipped and lipped channels subjected to web crippling.

123 The effects of initial geometric imperfections and residual stresses can be neglected in  
124 the finite element models of light gauge steel sections subject to web crippling. In the web  
125 crippling study, the expected buckling modes exhibit stable post buckling behaviour which

126 significantly reduces its effects on imperfection sensitivity, and meanwhile, the stocky channel  
127 sections with restraints at both ends also reduce the imperfection effects. This is already  
128 confirmed by a number of research studies [76-79]. In these studies [26,28,42-46,74], the  
129 researchers conducted both the experimental and numerical investigations on the web crippling  
130 behaviour of thin-walled structures, where the ratio of channel length to the web depth was  
131 around 3. This ratio has been adopted in the parametric study of this paper. Therefore, the  
132 effects of initial geometric imperfections and residual stresses were not considered in the FE  
133 models developed in this study.

### 134 *3.2 FEM validation*

135 In total, 30 experimental results from Fang et al. [57] were used to validate the FE model,  
136 and the comparison results of FEA and tests are reported in Table 1. The mean values of the  
137 ratio of experimental to FEA strengths ( $P_{EXP}/P_{FEA}$ ) are 1.06 and 1.04, respectively for  
138 unfastened and fastened sections, with coefficients of variation (COVs) of 0.02 and 0.03,  
139 respectively. Fig.3 depicted the numerical and experimental ITF web crippling failure modes  
140 of the investigated channels. In terms of load-vertical displacement behaviour, the numerical  
141 results were found to be very close to the experimental results (see Fig.3). Therefore, the  
142 developed FE models could closely predict the ITF web crippling strength of perforated RFA  
143 channels.

## 144 **4 Current design rules**

### 145 *4.1 Web crippling strength for plain channels*

#### 146 *4.1.1 AS/NZS 1664.1 [18]*

147 The nominal web crippling strength ( $P_{AS/NZS1664}$ ) of RFA unclipped channels subjected  
148 ITF loading could be calculated using Equation 1 as below.

149 
$$P_{AS/NZS1664} = \frac{t^2 \sin \theta (0.46 f_y + 0.02 \sqrt{E f_y}) (N + C_{w1})}{C_{w3} + r_i (1 - \cos \theta)} \quad (1)$$

150 where,  $C_{w1}=140\text{mm}$ ;  $C_{w2}=33\text{mm}$ ;  $C_{w3}=10\text{mm}$ ;  $\theta=90^\circ$ .

151 *4.1.2 Eurocode [20]*

152 The ITF web crippling strength ( $P_{CEN}$ ) of RFA unliped channels can be determined by  
153 Equation 2 available in Eurocode [20].

154 
$$P_{CEN} = \alpha t^2 \sqrt{f_y E} \left( 2.4 + \left( \frac{\theta}{90} \right)^2 \right) \left( 1 - 0.1 \sqrt{\frac{r_i}{t}} \right) \left( 0.5 + \sqrt{\frac{0.02N}{t}} \right) \quad (2)$$

155 where,  $\alpha$  represents the coefficient for several local loads as well as for support categories of  
156 the cross-sections.

157 *4.1.3 AISI&AS/NZS 4600:2018 [17,19]*

158 The unified web crippling design strength ( $P_{AISI&AS/NZS}$ ) of RFCS plain sections could be  
159 determined by using Equation 3 of AISI&AS/NZS 4600:2018 [17,19].

160 
$$P_{AISI&AS/NZS} = C t^2 f_y \sin \theta (1 - C_w \sqrt{\frac{h}{t}}) (1 - C_r \sqrt{\frac{r}{t}}) (1 + C_l \sqrt{\frac{N}{t}}) \quad (3)$$

161 where,  $C$ ,  $N$ ,  $C_r$ ,  $C_l$  and  $C_w$  represent equation coefficients.

162 *4.2 Web crippling strength reduction factor*

163 Due to the absence of design rules for the strength reduction factor of roll-formed  
164 aluminium alloy channel sections, the equations proposed by Uzzaman et al. [42-44] were  
165 employed in this study. It should be noted that these equations [42-44] are for roll-formed  
166 carbon steel perforated lipped channels and are limited to  $h/t \leq 156$ ,  $N/t \leq 84$ ,  $N/h \leq 0.63$  and  
167  $a/h \leq 0.8$ . Moreover, it is important to note that the  $N/h$  ratio was not included in the design  
168 equations of Uzzaman et al. [42-44].

## 169 **5 eXtreme Gradient Boosting (XGBoost)**

### 170 *5.1 Overview*

171 eXtreme Gradient Boosting (XGBoost) database is a collection of algorithms based on  
172 the boosting framework. The loss function of XGBoost performs a more accurate second order  
173 Taylor expansion on the error component throughout the optimisation method of the algorithm.  
174 Parallel selection is normally used to determine the appropriate subtree splitting features and  
175 eigenvalues for each weak learner, similar to the process of decision tree construction. Prior to  
176 parallel selection, all feature values are sorted and grouped to simplify the previously described  
177 parallel selection. This algorithm selects the proper group size for the grouped features.

### 178 *5.2 Cross validation*

179 Overfitting happens frequently during the training phase, which indicates that the model  
180 can accurately match the training data but cannot reliably predict the data outside of the training  
181 set. Isolating a portion of the training data from the validation data is a standard practice. Cross-  
182 validation, also known as round robin validation, is a method of assessing a model against its  
183 validation data. In order to develop K models, the data in this study was divided into K groups  
184 (K-Fold) and a validation set for each subset of data was created, while utilising the rest of the  
185 K-1 subset data as the training set. To calculate the cross-validation error, the validation set  
186 was divided into K models, and the final MSE (Mean Squared Error) was summed and  
187 averaged.

### 188 *5.3 Data training*

189 The data obtained from the validated FE models were used to train the XGBoost  
190 algorithm. Prior to normalisation, the input and output data points were formulated as follows:

$$191 \quad \text{Input} = \{b_w, b_f, r, t, N, a, x, n_h, f_y\} \quad (4)$$

192             $\text{Output} = \{P_p\}$  (5)

193            To minimise the over-fitting of the data, this study employed a learning rate, and used  
 194 the subsample method. The available data was split into two groups including: training and  
 195 testing set. A total of 1,080 data vectors were utilised in this study. The database was randomly  
 196 divided into training and testing data sets as a ratio of 70% and 30%, respectively.

197 *5.4 Performance evaluation*

198            To evaluate the prediction accuracy of the ML algorithm, the absolute percentage error  
 199 ( $\text{Err}_i$  (%)), correlation coefficient ( $R^*$ ), mean absolute error (MAE), and the root mean square  
 200 error (RMSE) were determined. The following are the formulae for determining each of these  
 201 parameters:

202            
$$\text{Err}_i(\%) = \frac{|y_i - t_i|}{t_i} \times 100$$
 (6)

203            
$$R^* = \frac{\sum_{i=1}^N (y_i - \bar{y}_i)(t_i - \bar{t}_i)}{\sqrt{\sum_{i=1}^N (y_i - \bar{y}_i)^2 \sum_{i=1}^N (t_i - \bar{t}_i)^2}}$$
 (7)

204            
$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^N (t_i - y_i)^2}{N}}$$
 (8)

205            
$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - t_i|$$
 (9)

206 where,  $t_i$  and  $y_i$  represent the real as well as prediction output values, respectively, and  $\bar{t}_i$  and  
 207  $\bar{y}_i$  represent the averages of the real and predicted outputs, respectively.  $N$  denotes the data  
 208 series.

209            The prediction accuracy of XGBoost algorithm was evaluated using the correlation  
 210 coefficient ( $R^*$ ), root mean square error (RMSE), and mean absolute error (MAE). The  $R^*$

211 value indicates how well the proposed formulation can predict the data. The root mean square  
212 error is also referred to as the cost function, and it plays a significant role in the learning process  
213 of a machine learning algorithm. The root means square error (RMSE) and the mean absolute  
214 error (MAE) both quantify the accuracy and goodness of the data fit. A good prediction model  
215 has lower RMSE and MAE values, which are close to having an  $R^*$  value of 1.00. The  
216 performance metrics for both training and testing data sets were determined using a 70%-30%  
217 training-testing split of the entire database. Cross-validation was carried out using the same  
218 training data as what was used to evaluate the measures (see Table 2).

219 As shown in Table 2 and in Fig.4, the  $R^*$  value obtained from the training set is the  
220 highest (0.9999), while the MAE and RMSE values are 0.0057 and 0.0032, respectively.  
221 Similarly, in the XGBoost model, the  $R^*$ , RMSE, and MAE values for the testing set are 0.9969,  
222 0.5340 and 0.2442, respectively. This indicates that the XGBoost model can predict the web  
223 crippling strength of RFA channels with high accuracy. Besides, the performance of XGBoost  
224 model was also compared with that of Random Forest and Linear Regression techniques. As  
225 demonstrated in Table 3, the XGBoost model significantly performed better than the Random  
226 Forest and Linear Regression Analysis.

### 227 *5.5 Comparison of results obtained from the machine-learning methods with the current design* 228 *standards*

229 The machine-learning method's prediction accuracy was assessed by comparing its  
230 results to the current design strengths in accordance with the AS/NZS 1664 [18], CEN 2007  
231 [20], and AISI & AS/NZS [17,19]. The machine-learning method (XGBoost model) achieved  
232 high prediction accuracy for training ( $R^*=0.9998$ , MSE=0.0057, MAE=0.0033) and testing  
233 ( $R^*=0.9969$ , MSE=0.5341, MAE=0.2442) data sets. In Table 4, the mean absolute percentage  
234 errors for web crippling capacity of unfastened sections obtained from the FEA results are

235 71.5%, 83.2%, 63.2% and 5.9%, respectively, when compared to the design strengths obtained  
236 from the AS/NZS 1664 [18], CEN 2007 [20], and AISI & AS/NZS [17,19]. The mean absolute  
237 percentage errors for fastened sections are 68.0%, 81.1%, 68.1% and 6.4%. The results show  
238 that the design strengths calculated from the AS/NZS 1664 [18], CEN 2007 [20], and  
239 AISI&AS/NZS [17,19] are almost 30% lower than the FEA and XGBoost results. In  
240 comparison to the calculation results of the existing design standards, both the FEA and  
241 XGBoost results could more precisely predict the web crippling strength of perforated RFA  
242 unlippped channels.

## 243 **6 Parametric study**

244 A comprehensive parametric study was carried out utilizing the validated XGBoost  
245 model to determine the effects of hole size, hole location, section thickness, and the length of  
246 bearing plate on the web crippling strength of perforated RFA unlippped channel under ITF  
247 loading. The  $a/h$  ratio was adjusted between 0 and 0.8, with a step increment of 0.2. Thickness  
248 of the section ( $t$ ) was varied from 1 to 4mm, while the radius of the corner ( $r$ ) was altered  
249 between 2 and 6mm, as shown in Table 5. The effect of bearing lengths ( $N$ ): 50, 75, and 100mm  
250 were studied (see Table 5).

### 251 *6.1 Effect of $r/t$ , $N/t$ , $h/t$ and flange types*

252 Figs.5(a-c) present the effects of ratios  $r/t$ ,  $N/t$  and  $h/t$  on the dimensionless web crippling  
253 strength of RFA unlippped channels. The downward trend of dimensionless strength of the  
254 investigated channels was observed when the  $r/t$  and  $h/t$  ratios were increased. On the other  
255 hand, the web crippling strength increased when the  $N/t$  ratio increased from 0.21 to 0.63. From  
256 Fig.5(d), it can be seen that  $P_n$  for RFA unlippped channels with fastened flanges are typically  
257 greater than those with unfastened flanges, with a mean difference of 34.9%.

## 258 6.2 Effects of $a/h$ , $N/h$ and $x/h$ ratios on $R$

259 Fig.6(a) and Table 5 show the influence of  $a/h$  ratio on the value of  $R$ . Fig.6(a) shows a  
260 decreasing trend in the web crippling strength reduction factors as the  $a/h$  ratio increased from  
261 0.2 to 0.8. On the one hand,  $R$  values for offset-hole sections with unfastened and fastened  
262 flanges were comparable, but the mean value of  $R$  for these two groups of sections is  
263 significantly different, decreasing from 0.93 to 0.54 and from 0.95 to 0.67, respectively, as the  
264  $a/h$  ratio increased from 0.2 to 0.8. On the other hand, a rather minor variation in  $R$  value was  
265 detected between the unfastened and fastened flanges with centred web holes. As reported in  
266 Table 5, the mean value of  $R$  was reduced from 0.95 to 0.61 for centred hole sections with  
267 unfastened flanges. Similarly, when the  $a/h$  ratio was raised from 0.2 to 0.8, the value of  $R$  for  
268 sections with fastened flanges dropped from 0.96 to 0.60.

269 As the  $N/h$  ratio was increased from 0.21 to 0.75 for channels with centred web holes,  
270 the mean value of  $R$  for channels with unfastened and fastened flanges were decreased from  
271 0.84 to 0.80 and from 0.80 to 0.84, respectively.  $R$  values increased from 0.73 to 0.75 and from  
272 0.80 to 0.86 for unfastened and fastened flanges of channels with offset web holes, respectively.

273 The mean value of  $R$  for channels with unfastened and fastened flanges ranged between  
274 0.68 and 0.92 and between 0.78 to 0.95, respectively, when the  $x/h$  ratio was adjusted between  
275 0.01 and 0.50. As can be seen from Fig.6(c), there is a noticeable variation in the trend of  $R$  for  
276 the RFA unlipped channel with un-fastened and fastened flanges having offset web holes with  
277 varying  $a/h$  ratios.

278 Fig.6(d) and Table 5 show the effect of fastened flanges on the value of  $R$  when the  $a/h$   
279 ratio and hole location were varied. As can be observed from Fig.6(d) and from Table 5, the  
280 mean value of  $R$  for channels varied slightly. The value of  $R$  for channels with unfastened  
281 flanges is comparable to that of channels with fastened flanges, whereas the mean values of  $R$

282 for unfastened sections with offset web holes are greater than those for fastened sections with  
 283 offset web holes (by 11.1% on average).

## 284 **7 Proposed design equations and reliability analysis**

285 Based on the results of XGBoost model, design equations in the form of web crippling  
 286 strength and web crippling strength reduction factors are proposed. The proposed equations  
 287 have limits of the parameters as:  $h/t \leq 295$ ,  $N/t \leq 100$ ,  $R/t \leq 6.0$ ,  $N/h \leq 0.75$  and  $a/h \leq 0.8$ . The  
 288 ranges of  $h/t$ ,  $N/t$ , and  $N/h$  were increased relative to the proposed carbon steel equations of  
 289 Uzzaman et al. [42-44].

### 290 *7.1 Proposed equations*

291 The design equations for calculating the web crippling strength ( $P_{prop}$ ) and web crippling  
 292 strength reduction factor ( $R_{prop}$ ) of RFA unlippped channel sections subjected to ITF loading are  
 293 proposed as follows:

$$294 \quad P_{prop} = Ct^2 f_y (1 - C_R \sqrt{\frac{r}{t}}) (1 + C_N \sqrt{\frac{N}{t}}) (1 - C_h \sqrt{\frac{h}{t}}) > 0 \quad (10)$$

295 For sections with a centred web hole,

$$296 \quad R_{prop} = \alpha - \gamma \frac{a}{h} + \lambda \frac{N}{h} \leq 1 \quad (11)$$

297 For sections with offset web holes,

$$298 \quad R_{prop} = \beta - \mu \frac{a}{h} + \zeta \frac{N}{h} + \xi \frac{x}{h} \leq 1 \quad (12)$$

299 where, the recommended values for  $C$ ,  $C_R$ ,  $C_N$  and  $C_h$  are listed in Table 6. The values of  $\alpha$ ,  $\gamma$ ,  
 300  $\lambda$ ,  $\beta$ ,  $\mu$ ,  $\zeta$  and  $\xi$  represent the coefficient values which are presented in Table 7 for each type of  
 301 section.

302 By comparing the proposed design strengths with the FE strengths and the failure  
303 strengths calculated from the equations from Uzzaman et al. [42-44], it was found that the  
304 prediction accuracy of the proposed equations is much better. The reduced web crippling  
305 strength calculated using the proposed equations are highly predictive of the FE strengths, as  
306 shown in Table 8, and the mean values of the ratios of  $P/P_{prop}$ ,  $R/R_{prop}$  are both close to 1,  
307 demonstrating that the (reduced) ITF web crippling strength of RFA unlippped channels could  
308 be closely predicted by the proposed design equations.

### 309 *7.2 Reliability analysis*

310 To assess the performance accuracy of proposed design equations, a reliability study was  
311 conducted using the technique described by Hsiao et al. [80]. Any proposed design equation is  
312 considered to be reliable if its reliability index ( $\beta'$ ) is more than or equal to the target reliability  
313 index of 2.5, according to the American standard (AISI S100-16 [17]). The reliability indices  
314 of the proposed equations are higher than the target index of 2.5, (see Table 9). This confirms  
315 that the proposed design equations could predict the ITF web crippling strength of RFA  
316 unlippped channels with high degree of precision.

## 317 **8 Conclusions**

318 A novel machine-learning model using the XGBoost tool was developed to investigate  
319 the ITF web crippling behaviour of perforated RFA unlippped channels. A nonlinear elasto-  
320 plastic FE model was developed and validated against the experimental results available in  
321 literature. To train the XGBoost model, a total of 1,080 data points were created using the  
322 validated FE model. The XGBoost predictions were close to the numerical failure loads, being  
323 conservative by only 6% for unlippped channels with unfastened flanges and by 7% for sections  
324 with fastened flanges. The training process and the performance of the proposed XGBoost  
325 model were also compared with that of Random Forest and Linear Regression techniques, and

326 it was found that the XGBoost model outperformed the other two techniques. The XGBoost  
327 results were then compared to the design strengths calculated from the Australian/New Zealand  
328 standard (AS/NZS 1664.1; AS/NZS 4600:2018), American Iron and Steel Institute (AISI), and  
329 Eurocode standards (CEN 2007). The developed XGBoost model was found to outperform the  
330 existing design standards. The design strengths in accordance with the AS/NZS 1664.1,  
331 AISI&AS/NZS 4600:2018, and CEN 2007 were found to be excessively conservative by  
332 95.5%, 65.3%, and 34.1% for aluminium alloy unlipped channels with unfastened flanges,  
333 respectively, and conservative by 34.9%, 21.7%, and 7.3% for channels with fastened flanges.

334 Finally, using the XGBoost output, a parametric study was conducted, and it was found  
335 that the web crippling strength is sensitive to the changes in geometrical parameters such as  
336 hole size, hole location, section thickness, and the length of bearing plate. Using the XGBoost  
337 predictions, new design equations for web crippling strength and web crippling strength  
338 reduction factor were proposed. A reliability analysis was also performed; the results of which  
339 confirmed that the proposed design equations could be used to predict the web crippling  
340 strength of perforated RFA unlipped channels subjected to ITF loading condition.

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<b>Notation</b>	
$a$	Hole diameter;
$b_w$	Overall web depth of section;
$b_f$	Overall flange width of section;
COV	Coefficient of variation;

$E$	Young's modulus of elasticity;
$Err$	Absolute percentage error;
FEA	Finite element analysis;
$h$	Web flat depth;
ITF	Interior-two-flange;
$L$	Total length of the channel sections;
MAE	Mean absolute error;
MSE	Mean squared error;
$P_{AS/NZS1664}$	Web crippling strength from AS/NZS 1664.1
$P_{AISI\&AS/NZS}$	Web crippling strength from the AISI & AS/NZS (4600:2018);
$P_{CEN}$	Web crippling strength from the Eurocode;
$P_{EXP}$	Web crippling strength from experiments;
$P_{FEA}$	Web crippling strength from the finite element analysis;
$P_p$	Prediction value;
$P_{prop}$	Web crippling strength from the proposed equation;
$r$	Inside bend radius;
$R_{prop}$	Web crippling strength reduction factor from the proposed equation;
$R_{Uzzaman}$	Reduction factor from Uzzaman et al.;
$R^*$	Correlation coefficient;
$t$	Nominal thickness of the channel section;
$t_i$	Real output value;
$\bar{t}_i$	Average real output value;
$x$	Hole distance to bearing block;
$y_i$	Prediction output value;
$\bar{y}_i$	Average prediction output value;
$\alpha, \beta, \gamma, \lambda, \rho, \mu, \zeta, \zeta$	Equation coefficients;

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**Table 1** Comparison of experimental and numerical results

Specimen ID	Web	Length	Bend radius	Thickness	Hole dia	Bearing length	Exp. Load	FEA result	$P_{EXP}/P_{FEA}$
	$d$	$L$	$r$	$t$	$a$	$N$	$P_{EXP}$	$P_{FEA}$	
	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(kN)	(kN)	
Unfastened sections									
ITF240-N50-NH-A0-FR	241.75	770	3	1.96	0	50	5.25	5.01	1.05
ITF240-N75-NH-A0-FR	240.78	795	3	1.95	0	75	5.39	5.07	1.06
ITF240-N100-NH-A0-FR	240.35	820	3	1.95	0	100	5.44	5.21	1.05
ITF240-N50-DH-A0.2-FR	241.14	770	3	1.95	48	50	5.06	4.74	1.07
ITF240-N75-DH-A0.2-FR	240.26	795	3	1.95	48	75	5.12	4.86	1.05
ITF240-N100-DH-A0.2-FR	240.93	820	3	1.95	48	100	5.32	4.99	1.07
ITF240-N50-OH-A0.2-FR	241.51	770	3	1.95	48	50	4.82	4.56	1.06
ITF240-N75-OH-A0.2-FR	241.28	795	3	1.95	48	75	4.85	4.69	1.03
ITF240-N100-OH-A0.2-FR	240.27	820	3	1.95	48	100	5.06	4.83	1.05
ITF240-N50-DH-A0.6-FR	240.44	770	3	1.95	144	50	3.81	3.59	1.06
ITF240-N75-DH-A0.6-FR	241.71	795	3	1.96	144	75	3.84	3.77	1.02
ITF240-N100-DH-A0.6-FR	240.54	820	3	1.95	144	100	4.06	3.86	1.05
ITF240-N50-OH-A0.6-FR	241.96	770	3	1.95	144	50	3.5	3.17	1.11
ITF240-N75-OH-A0.6-FR	241.44	795	3	1.95	144	75	3.48	3.3	1.05
ITF240-N100-OH-A0.6-FR	241.15	820	3	1.95	144	100	3.74	3.43	1.09
Average									1.06
Cov									0.02
Fastened sections									
ITF200-N50-NH-A0-FX	240.12	770	3	1.95	0	50	7.63	7.25	1.05
ITF200-N75-NH-A0-FX	240.63	795	3	1.95	0	75	7.68	7.42	1.03
ITF200-N100-NH-A0-FX	241.68	820	3	1.95	0	100	7.99	7.61	1.05
ITF200-N50-DH-A0.2-FX	241.11	770	3	1.96	48	50	7.17	6.99	1.03
ITF200-N75-DH-A0.2-FX	241.45	795	3	1.95	48	75	7.17	7.06	1.02
ITF200-N100-DH-A0.2-FX	241.59	820	3	1.96	48	100	7.44	7.31	1.02
ITF200-N50-OH-A0.2-FX	241.68	770	3	1.96	48	50	7.1	6.86	1.03
ITF200-N75-OH-A0.2-FX	241.43	795	3	1.96	48	75	7.21	7.04	1.02
ITF200-N100-OH-A0.2-FX	241.1	820	3	1.96	48	100	7.6	7.21	1.05
ITF200-N50-DH-A0.6-FX	241.79	770	3	1.94	144	50	4.98	4.92	1.01
ITF200-N75-DH-A0.6-FX	241.51	795	3	1.94	144	75	5.1	5.11	1
ITF200-N100-DH-A0.6-FX	241.13	820	3	1.94	144	100	5.41	5.37	1.01
ITF200-N50-OH-A0.6-FX	241.83	770	3	1.95	144	50	5.84	5.4	1.08
ITF200-N75-OH-A0.6-FX	240.69	795	3	1.95	144	75	5.87	5.54	1.06
ITF200-N100-OH-A0.6-FX	240.53	820	3	1.95	144	100	6.36	5.74	1.11
Average									1.04
Cov									0.03

**Table 2** Performance measure of developed machine learning model

XGBoost Training			XGBoost Testing		
$R^*$	RMSE	MAE	$R^*$	RMSE	MAE
0.9998	0.0057	0.0033	0.9969	0.5341	0.2442

**Table 3** Cross-validation with linear regression and random forest regression analysis results

Methods	XGBoost	Random Forest	Linear Regression
Cross validation Score	0.996786	0.992931	0.902183
NMSE	-0.288674	-0.622938	-8.486916

**Table 4** Absolute percentage error for numerical failure load

Specimen ID	Web	Length	Hole dia	Bearing length	Failure load	Err% (AS/NZS1664)	Err% (EC)	Err% (AISI&AS/NZS)	Err (XGBoost)
	$d$	$L$	$a$	$N$	$P_{FEA}$				
	(mm)	(mm)	(mm)	(mm)	(kN)				
Unlipped channels with un-fastened flanges									
1 ITF240-N50-NH-A0-FR	240	746	0	50	28.07	74.08	84.35	64.72	5.59
2 ITF240-N75-NH-A0-FR	240	771	0	75	28.66	71.52	83.11	63.09	5.68
3 ITF240-N100-NH-A0-FR	240	796	0	100	29.43	69.01	82.13	61.83	3.49
4 ITF240-N50-DH-A0.2-FR	240	746	46.4	50	25.97	--	--	--	5.14
5 ITF240-N75-DH-A0.2-FR	240	771	46.4	75	26.53	--	--	--	6.2
6 ITF240-N100-DH-A0.2-FR	240	796	46.4	100	27.25	--	--	--	5.17
7 ITF240-N50-OH-A0.2-FR	240	746	46.4	50	26.33	--	--	--	8.1
8 ITF240-N75-OH-A0.2-FR	240	771	46.4	75	27	--	--	--	7.43
9 ITF240-N100-OH-A0.2-FR	240	796	46.4	100	27.81	--	--	--	6.55
10 ITF240-N50-DH-A0.6-FR	240	746	139.2	50	17.38	--	--	--	4.4
11 ITF240-N75-DH-A0.6-FR	240	771	139.2	75	18.23	--	--	--	5.87
12 ITF240-N100-DH-A0.6-FR	240	796	139.2	100	19.16	--	--	--	5.13
13 ITF240-N50-OH-A0.6-FR	240	746	139.2	50	19.22	--	--	--	7.68
14 ITF240-N75-OH-A0.6-FR	240	771	139.2	75	19.96	--	--	--	5.32
15 ITF240-N100-OH-A0.6-FR	240	796	139.2	100	20.77	--	--	--	6.46
Average						71.54	83.2	63.21	5.88
Cov						2.07	0.91	1.19	1.19
Unlipped channels with fastened flanges									
16 ITF240-N50-NH-A0-FX	240	746	0	50	28.07	71.09	82.55	68.91	6.59
17 ITF240-N75-NH-A0-FX	240	771	0	75	28.66	67.71	80.84	67.79	6.55
18 ITF240-N100-NH-A0-FX	240	796	0	100	29.43	65.15	79.9	67.61	8.49
19 ITF240-N50-DH-A0.2-FX	240	746	46.4	50	25.97	--	--	--	7.14
20 ITF240-N75-DH-A0.2-FX	240	771	46.4	75	26.53	--	--	--	5.2
21 ITF240-N100-DH-A0.2-FX	240	796	46.4	100	27.25	--	--	--	6.17
22 ITF240-N50-OH-A0.2-FX	240	746	46.4	50	26.33	--	--	--	8.1
23 ITF240-N75-OH-A0.2-FX	240	771	46.4	75	27	--	--	--	5.43
24 ITF240-N100-OH-A0.2-FX	240	796	46.4	100	27.81	--	--	--	5.55
25 ITF240-N50-DH-A0.6-FX	240	746	139.2	50	17.38	--	--	--	7.4
26 ITF240-N75-DH-A0.6-FX	240	771	139.2	75	18.23	--	--	--	5.87
27 ITF240-N100-DH-A0.6-FX	240	796	139.2	100	19.16	--	--	--	5.13
28 ITF240-N50-OH-A0.6-FX	240	746	139.2	50	19.22	--	--	--	5.68
29 ITF240-N75-OH-A0.6-FX	240	771	139.2	75	19.96	--	--	--	5.32
30 ITF240-N100-OH-A0.6-FX	240	796	139.2	100	20.77	--	--	--	7.46
Average						67.98	81.1	68.1	6.41
Cov						2.44	1.1	0.57	1.06

**Table 5** Web crippling strength reduction factors ( $R$ ) of RFA unlipped channels

Flange type		$R$	
		Un-fastened flanges	Fastened flanges
Centre hole	$a/h=0.2$	0.95	0.96
	$a/h=0.4$	0.85	0.87
	$a/h=0.6$	0.74	0.75
	$a/h=0.8$	0.57	0.59
Offset hole	$a/h=0.2$	0.93	0.95
	$a/h=0.4$	0.80	0.86
	$a/h=0.6$	0.67	0.76
	$a/h=0.8$	0.53	0.65

**Table 6** Coefficients of web crippling strength formulae

	Support and Flange conditions	$C$	$C_R$	$C_N$	$C_h$
$h/t < 60$	Unfastened to support	15.980	0.184	0.073	0.050
	Fastened to support	16.411	0.247	0.156	0.047
$h/t \geq 60$	Unfastened to support	14.564	0.095	0.048	0.048
	Fastened to support	19.252	0.131	0.065	0.047

**Table 7** Coefficients for web crippling strength reduction factor formulae

Coefficient	Flange unfastened to support	Flange fastened to support
$\alpha$	1.072	1.082
$\gamma$	0.623	0.609
$\lambda$	0.040	0.027
$\beta$	0.968	0.950
$\mu$	0.617	0.438
$\zeta$	0.077	0.052
$\xi$	0.099	0.125

**Table 8** Comparisons of web crippling strengths obtained from FEA and current design rules

Specimen ID	Failure load	$P_{FEA}/P_{AS/NZS1664}$	$P_{FEA}/P_{CE}$	$P_{FEA}/P_{AISI\&AS/NZS}$	$P_{FEA}/P_{pro}$	$R_{FEA}/P_{Uzzama}$	$R_{FEA}/P_{pro}$
	$P_{FEA}$ (kN)						
Plain unlippped channels with un-fastened flanges							
ITF240-N50-NH-A0-FR	28.07	0.69	1.14	0.51	1.08	--	--
ITF240-N75-NH-A0-FR	28.66	0.62	1.05	0.48	1.05	--	--
ITF240-N100-NH-A0-FR	29.43	0.57	0.99	0.46	1.04	--	--
Average		0.63	1.06	0.48	1.06	--	--
Cov		0.05	0.06	0.02	0.02	--	--
Plain sections with fastened flanges							
ITF200-N50-NH-A0-FX	36.43	0.89	1.48	0.83	1.12	--	--
ITF200-N75-NH-A0-FX	36.99	0.80	1.35	0.80	1.05	--	--
ITF200-N100-NH-A0-FX	38.22	0.74	1.29	0.80	1.03	--	--
Average		0.81	1.37	0.81	1.07	--	--
Cov		0.06	0.08	0.01	0.04	--	--
Perforated unlippped channels with un-fastened flanges							
ITF240-N50-DH-A0.2-FR	1.27	--	--	--	--	0.98	0.98
ITF240-N75-DH-A0.2-FR	1.43	--	--	--	--	0.98	0.97
ITF240-N100-DH-A0.2-FR	1.54	--	--	--	--	0.98	0.96
ITF240-N50-OH-A0.2-FR	1.44	--	--	--	--	--	1.02
ITF240-N75-OH-A0.2-FR	1.59	--	--	--	--	--	1.02
ITF240-N100-OH-A0.2-FR	1.75	--	--	--	--	--	1.02
ITF240-N50-DH-A0.6-FR	0.79	--	--	--	--	0.85	0.85
ITF240-N75-DH-A0.6-FR	0.89	--	--	--	--	0.87	0.87
ITF240-N100-DH-A0.6-FR	0.98	--	--	--	--	0.89	0.88
ITF240-N50-OH-A0.6-FR	1.13	--	--	--	--	--	1.04
ITF240-N75-OH-A0.6-FR	1.27	--	--	--	--	--	1.05
ITF240-N100-OH-A0.6-FR	1.41	--	--	--	--	--	1.05
Average		--	--	--	--	0.93	0.98
Cov		--	--	--	--	0.06	0.07
Perforated unlippped channels with fastened flanges							
ITF200-N50-DH-A0.2-FX	2.16	--	--	--	--	0.99	0.94
ITF200-N75-DH-A0.2-FX	2.46	--	--	--	--	0.99	0.95
ITF200-N100-DH-A0.2-FX	2.84	--	--	--	--	0.98	0.94
ITF200-N50-OH-A0.2-FX	2.45	--	--	--	--	--	1.01
ITF200-N75-OH-A0.2-FX	2.84	--	--	--	--	--	1.00
ITF200-N100-OH-A0.2-FX	3.24	--	--	--	--	--	1.00
ITF200-N50-DH-A0.6-FX	1.5	--	--	--	--	0.86	0.85
ITF200-N75-DH-A0.6-FX	1.73	--	--	--	--	0.89	0.87
ITF200-N100-DH-A0.6-FX	1.97	--	--	--	--	0.90	0.89
ITF200-N50-OH-A0.6-FX	2.13	--	--	--	--	--	0.96
ITF200-N75-OH-A0.6-FX	2.53	--	--	--	--	--	0.97
ITF200-N100-OH-A0.6-FX	2.9	--	--	--	--	--	0.97
Average		--	--	--	--	0.94	0.95
Cov		--	--	--	--	0.05	0.05

**Table 9** Reliability analysis results

(a) For web crippling strength equations

Section type	Unfastened section	Fastened section
Ratio of equations	$P_{FEA} / P_{prop}$	$P_{FEA} / P_{prop}$
Data number	108	108
Mean, $P_m$	1.02	1.03
$\beta'$ [17]	3.41	3.62
$\varphi$ [17]	0.85	0.85

(b) For web crippling strength reduction factor equations

Section type	Unfastened section	Fastened section
Ratio of equations	$R_{FEA} / R_{prop}$	$R_{FEA} / R_{prop}$
Data number	432	432
Mean, $P_m$	1.00	1.00
$\beta'$ [17]	3.61	3.61
$\varphi$ [17]	0.85	0.85

## List of Figures

**Fig.1** Cross-section dimension and loading condition

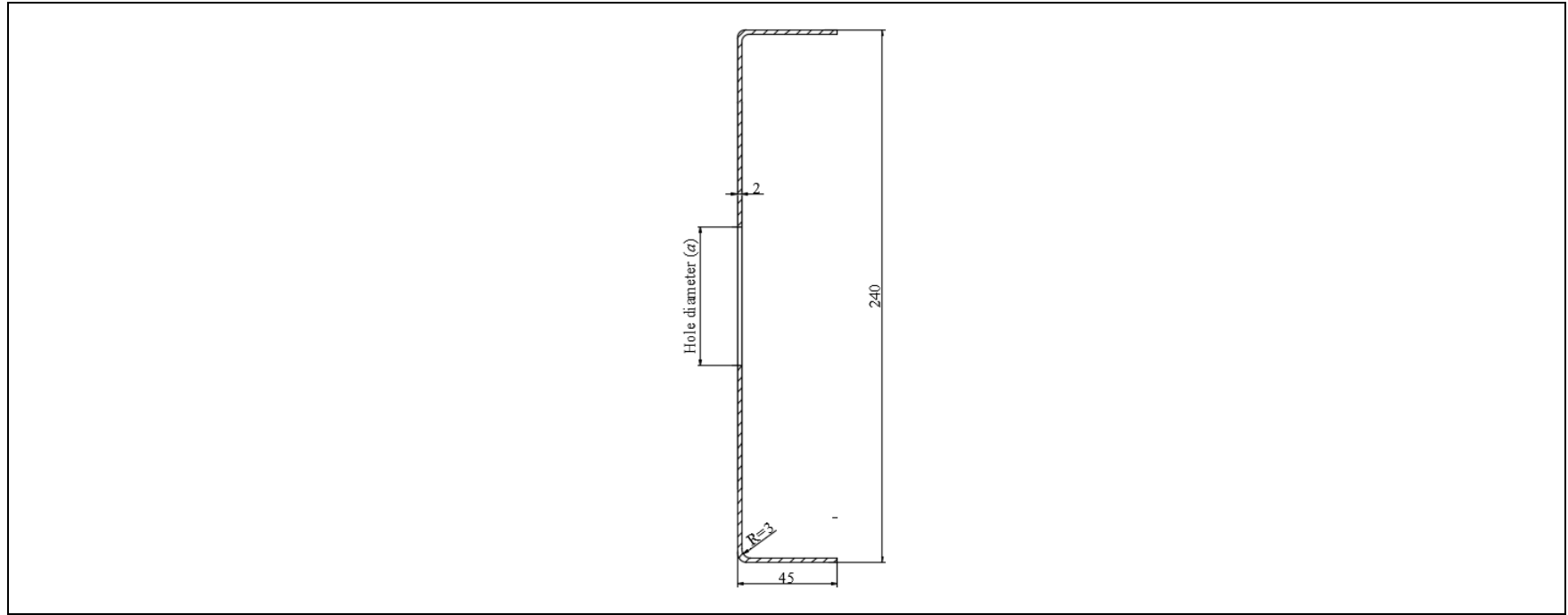
**Fig.2** Details of FE model

**Fig.3** Validation of FE model

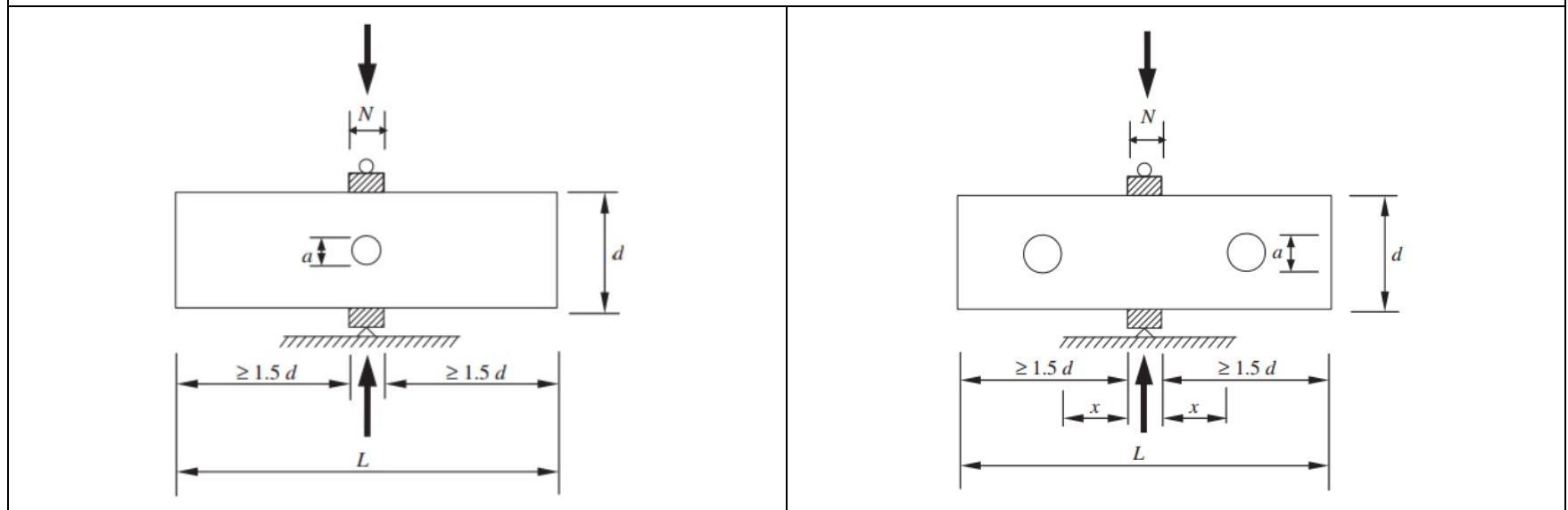
**Fig.4** XGBoost training

**Fig.5** Effect of  $r/t$ ,  $N/t$ ,  $h/t$  and flange type

**Fig.6** Effect of  $a/h$ ,  $N/h$ ,  $x/h$  and flange type



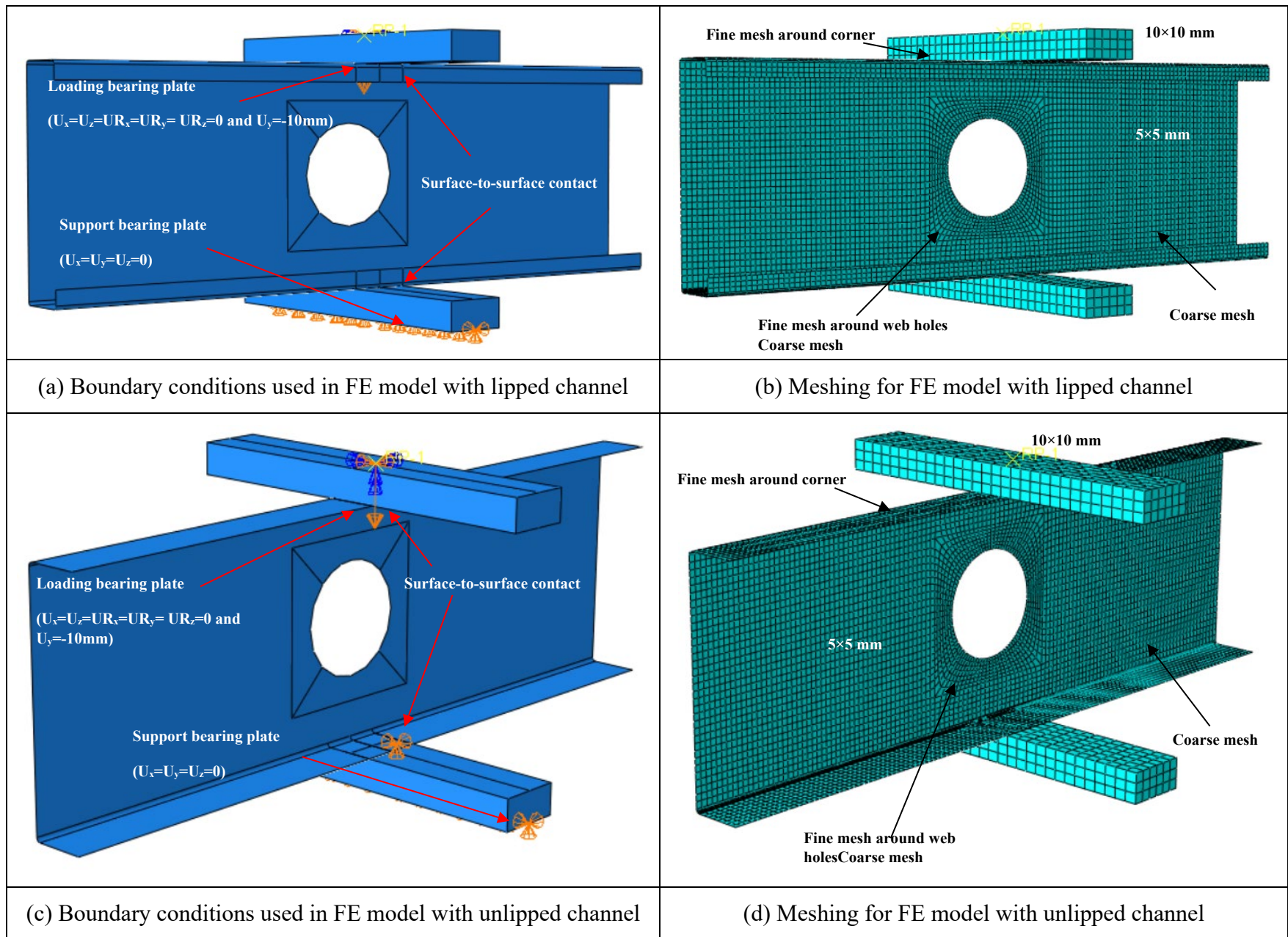
(a) Nominal cross-section of investigated channel (All dimensions are in mm)



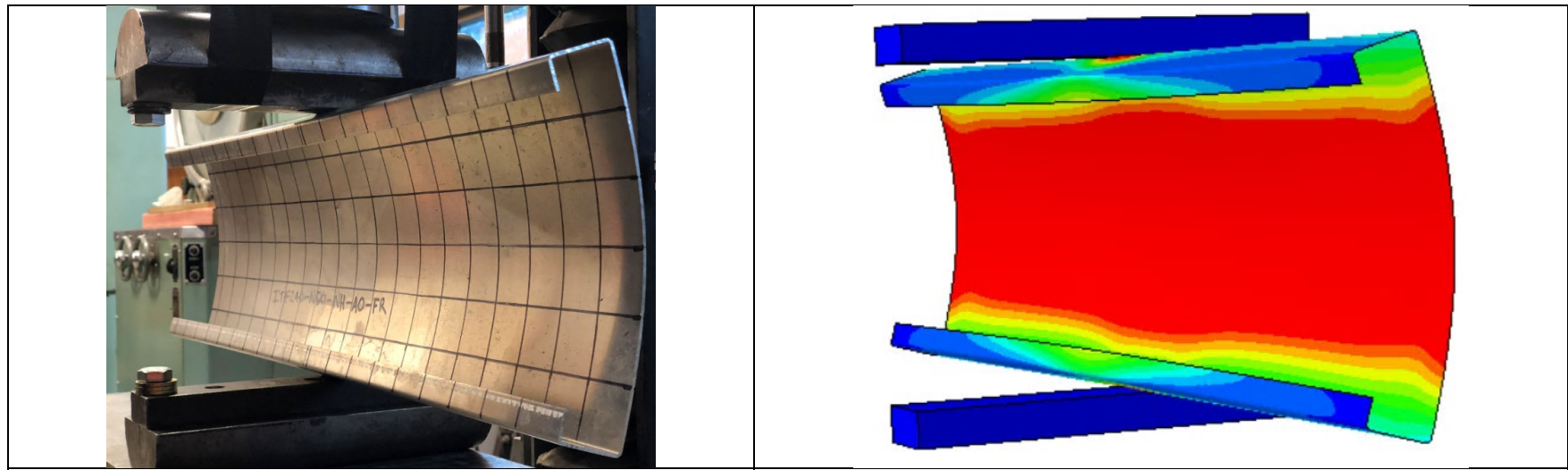
(b) ITF loading condition with centred web hole

(c) ITF loading condition with offset web hole

**Fig.1** Cross-section dimension and loading condition

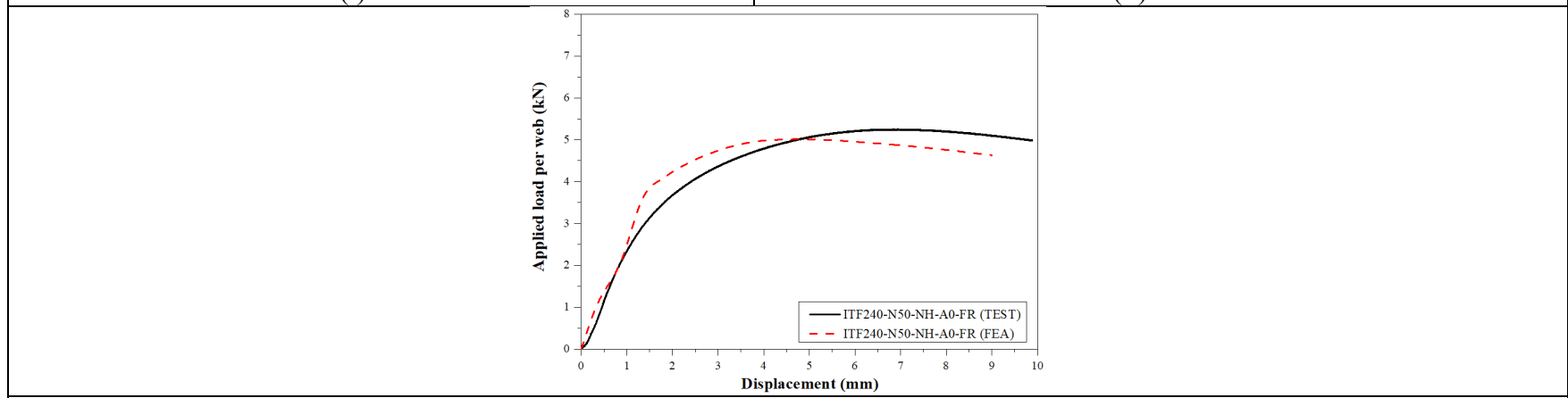


**Fig.2** Details of FE model



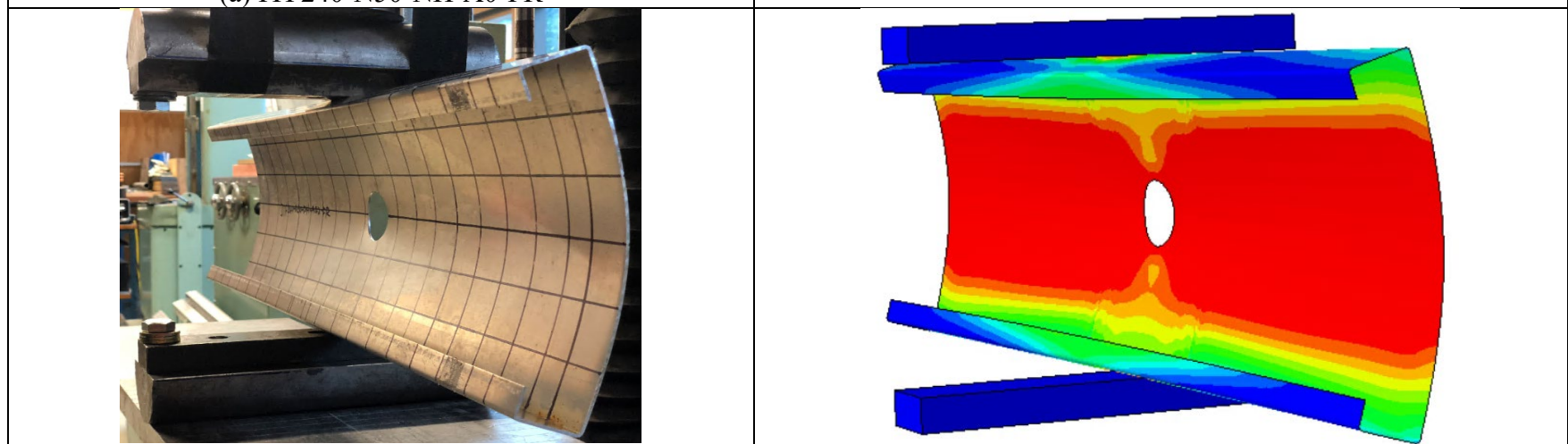
(i) Test

(ii) FEA



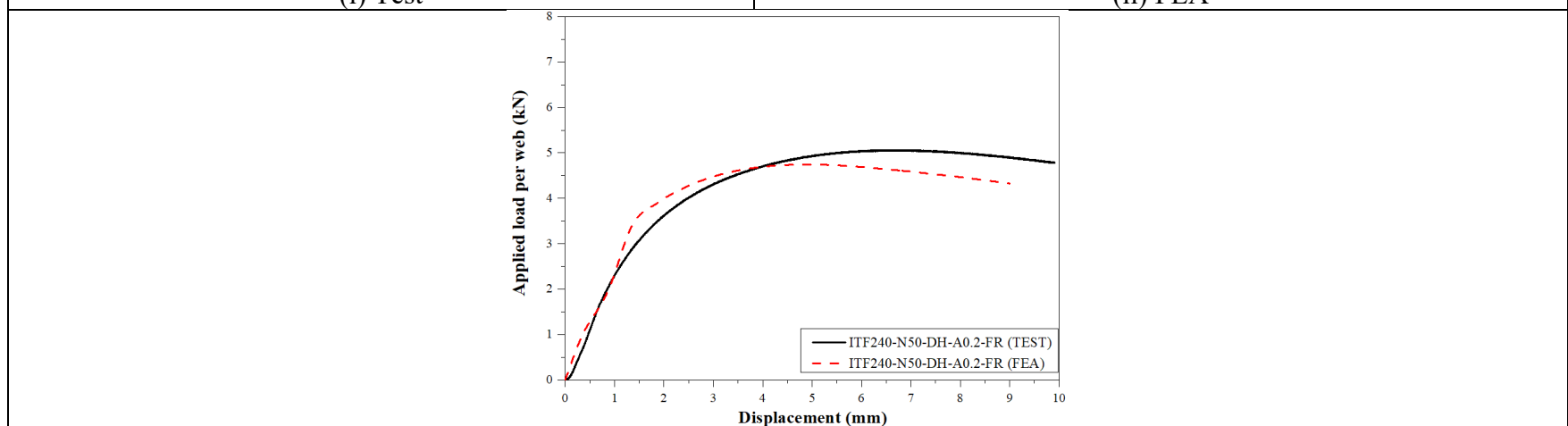
(iii) Web deformation curves

(a) ITF240-N50-NH-A0-FR



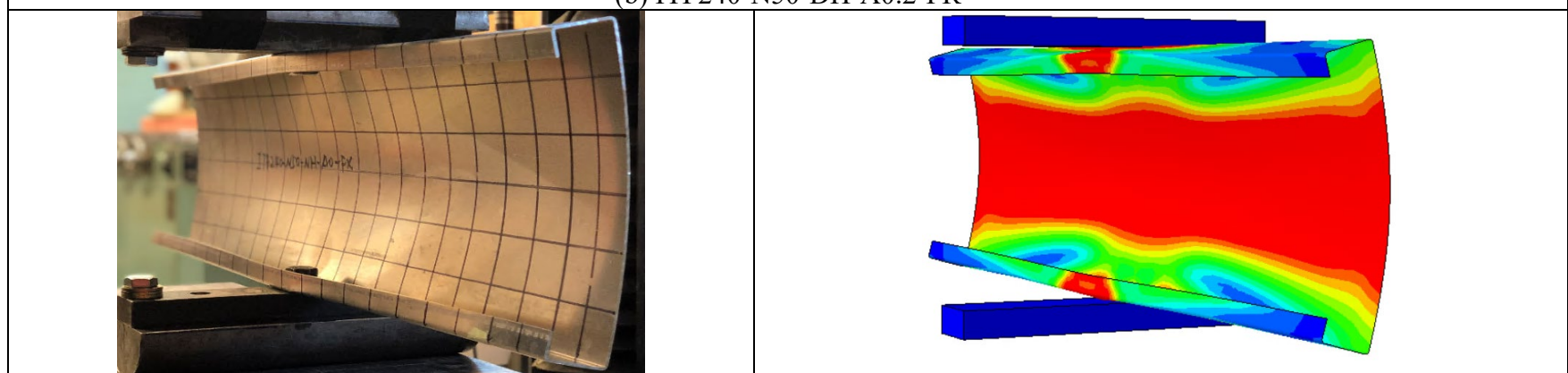
(i) Test

(ii) FEA



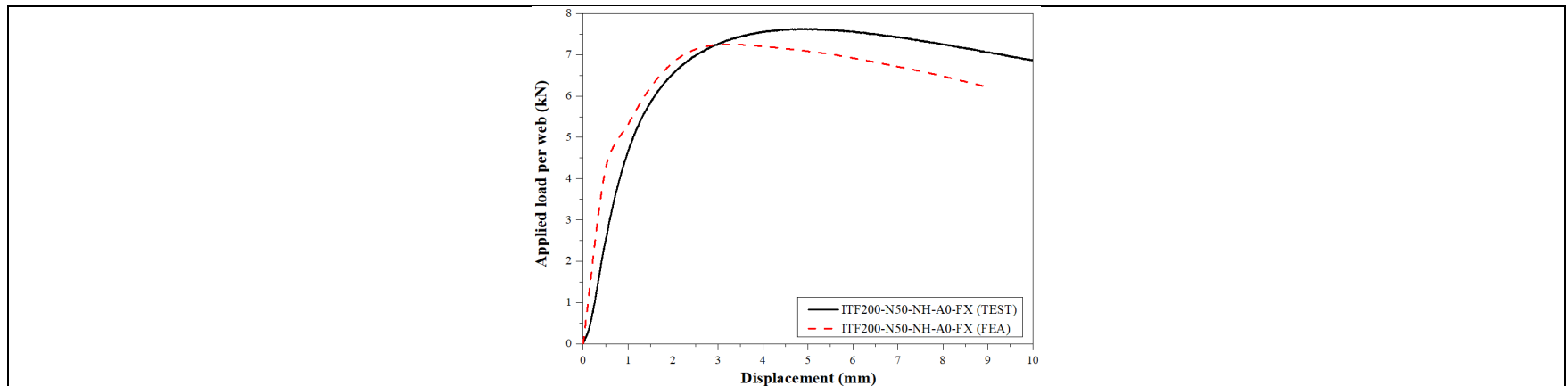
(iii) Load-displacement curve

(b) ITF240-N50-DH-A0.2-FR



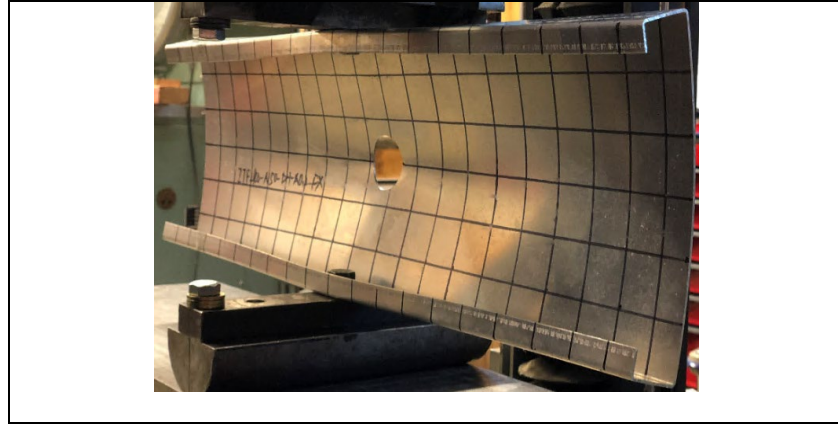
(i) Test

(ii) FEA

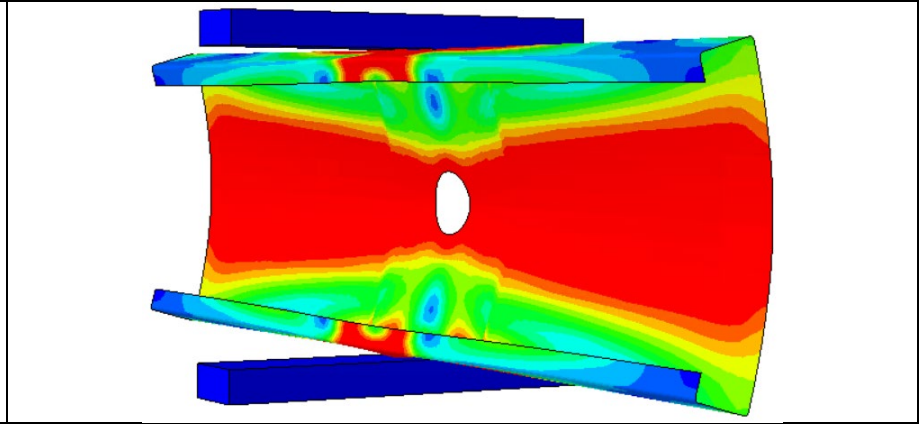


(iii) Load-displacement curve

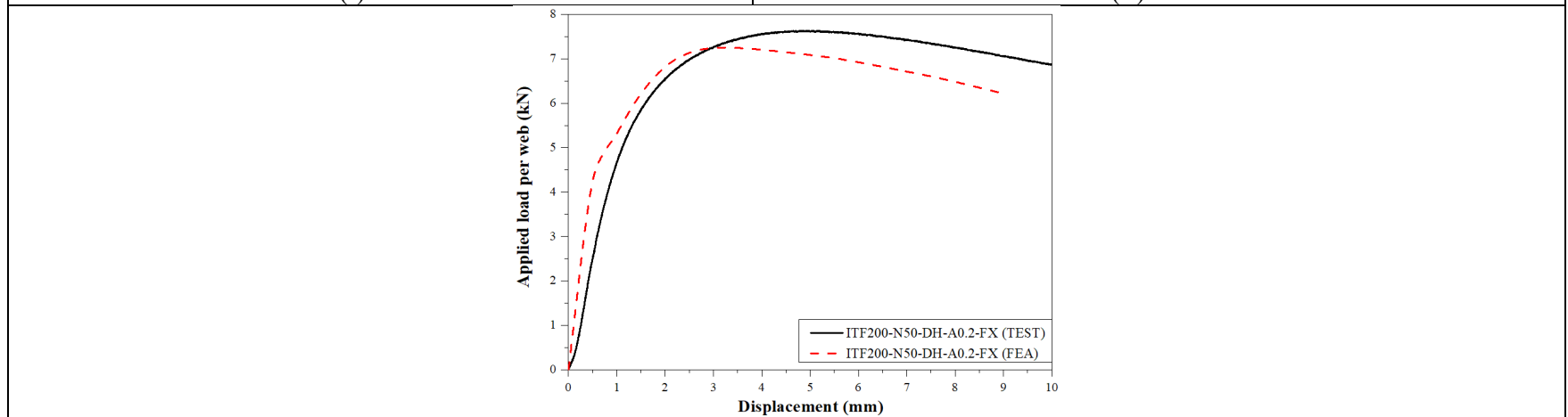
(c) ITF200-N50-NH-A0-FX



(i) Test

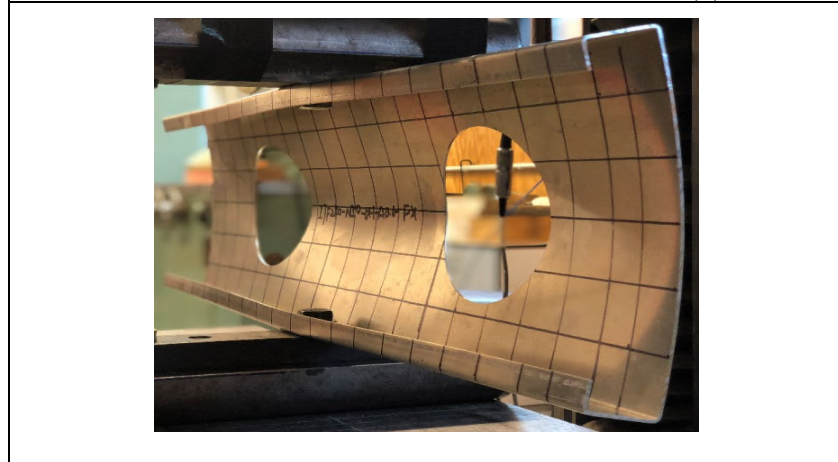


(ii) FEA

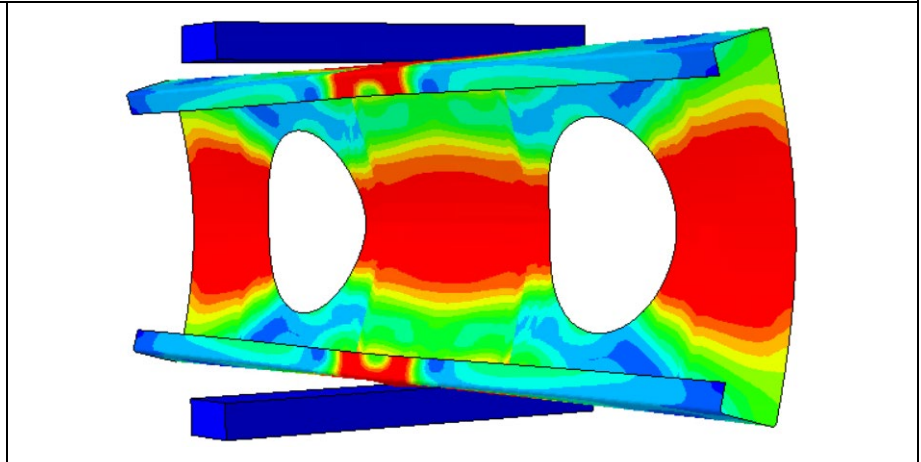


(iii) Load-displacement curve

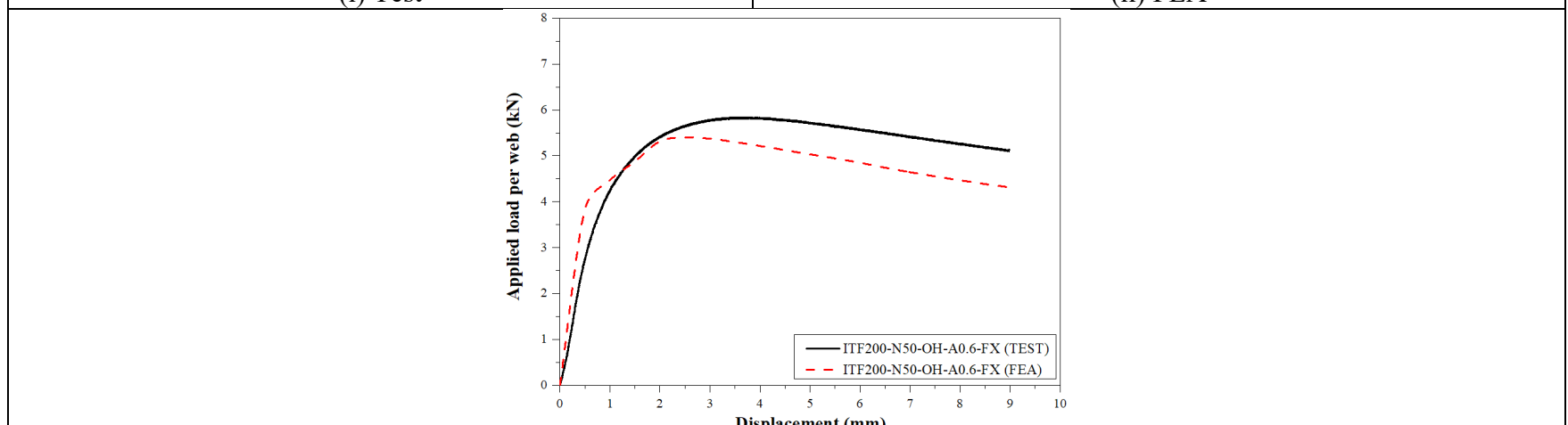
(d) ITF200-N50-DH-A0.2-FX



(i) Test



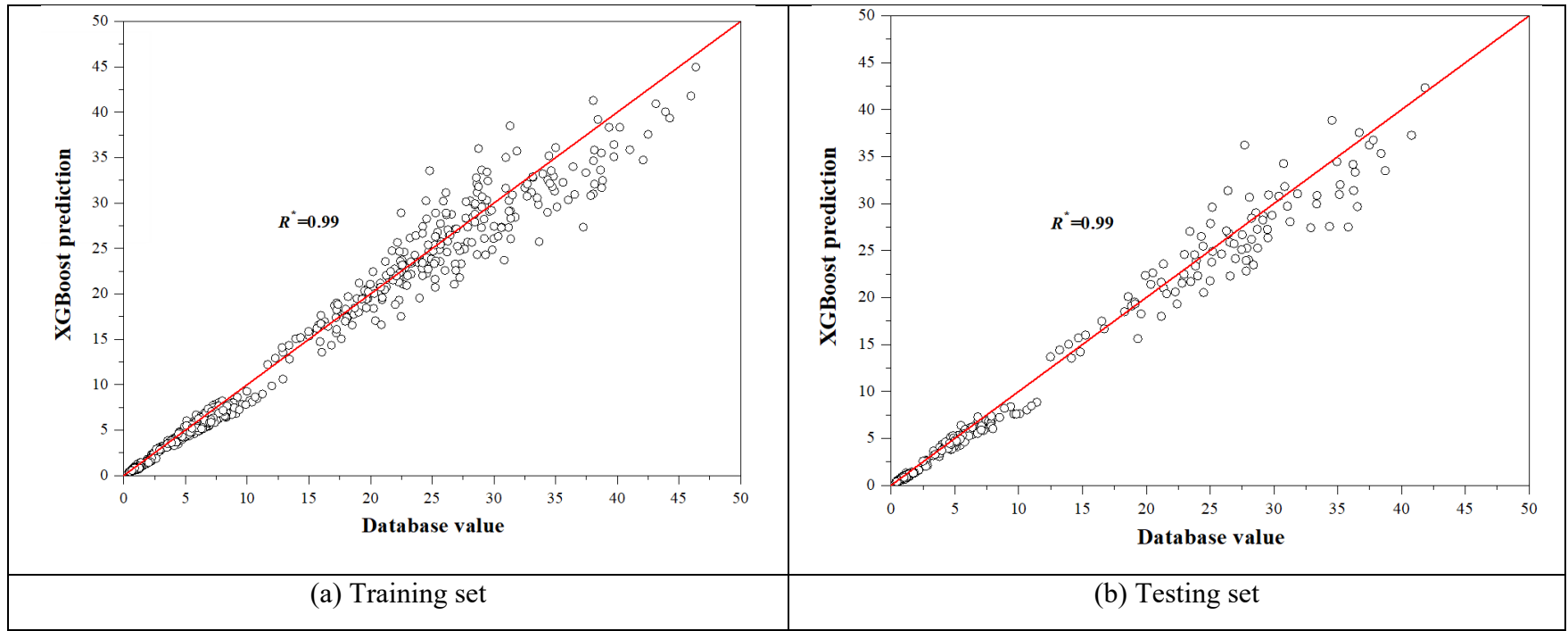
(ii) FEA



(iii) Load-displacement curve

(e) ITF200-N50-OH-A0.6-FX

Fig.3 Validation of FE model [57]



**Fig.4** XGBoost training

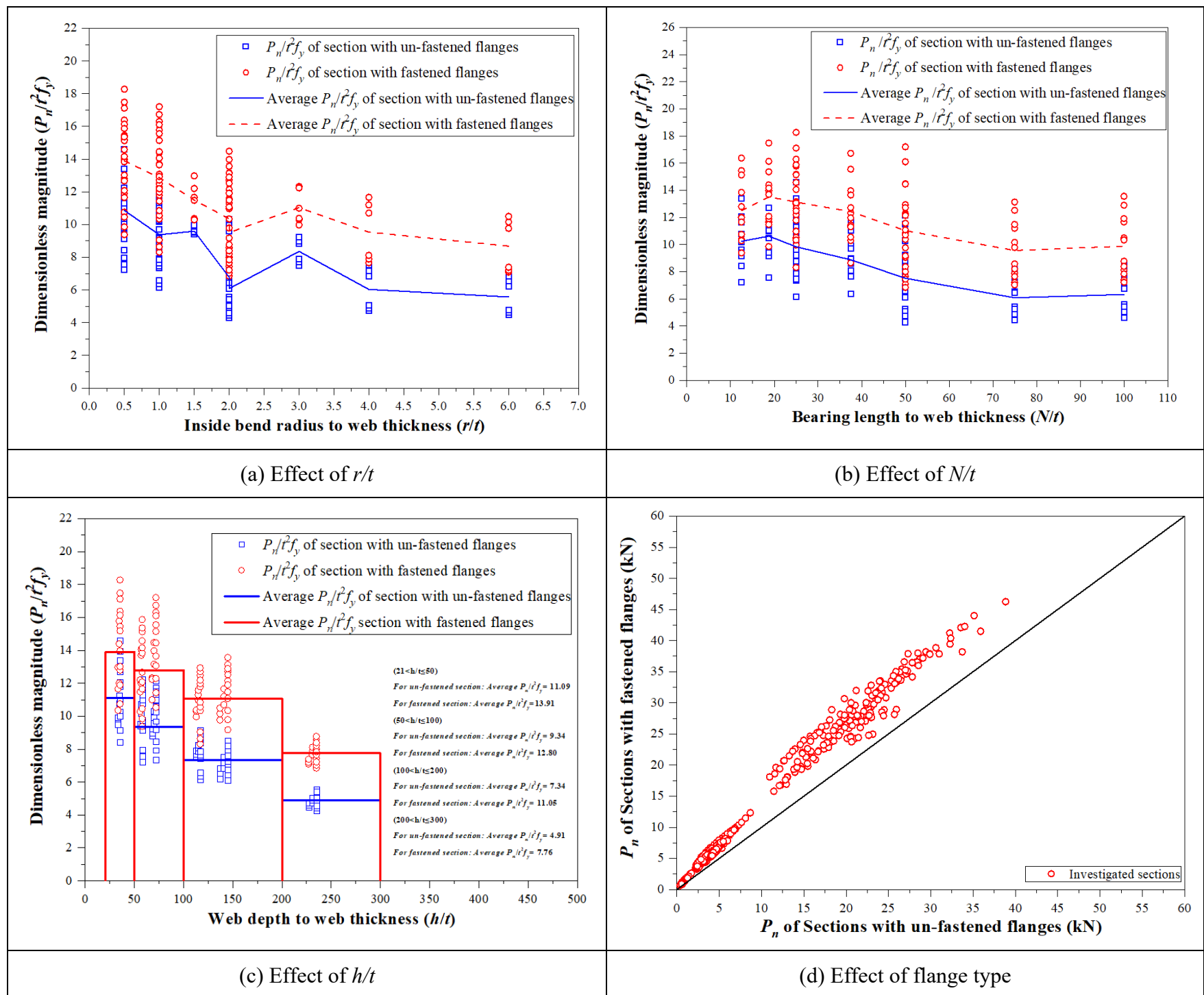
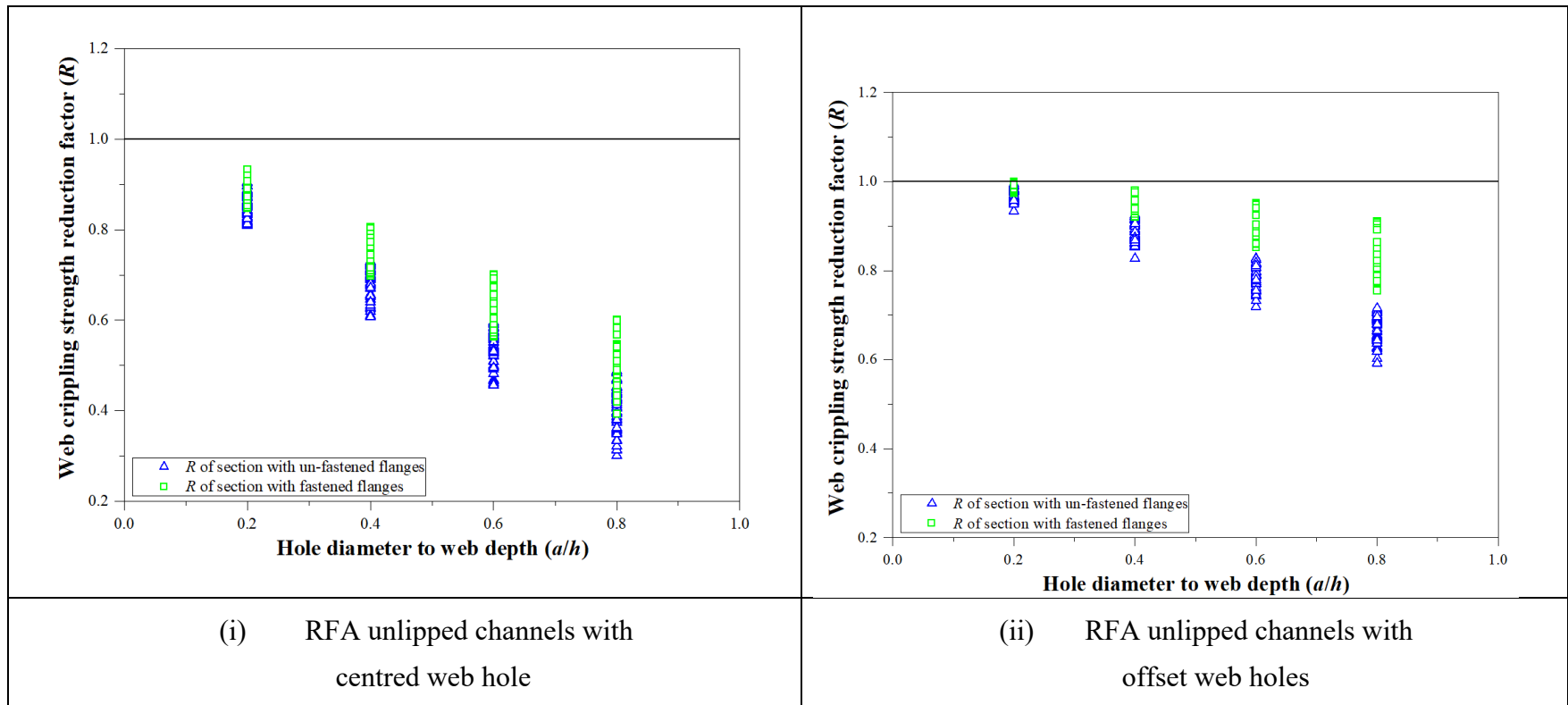
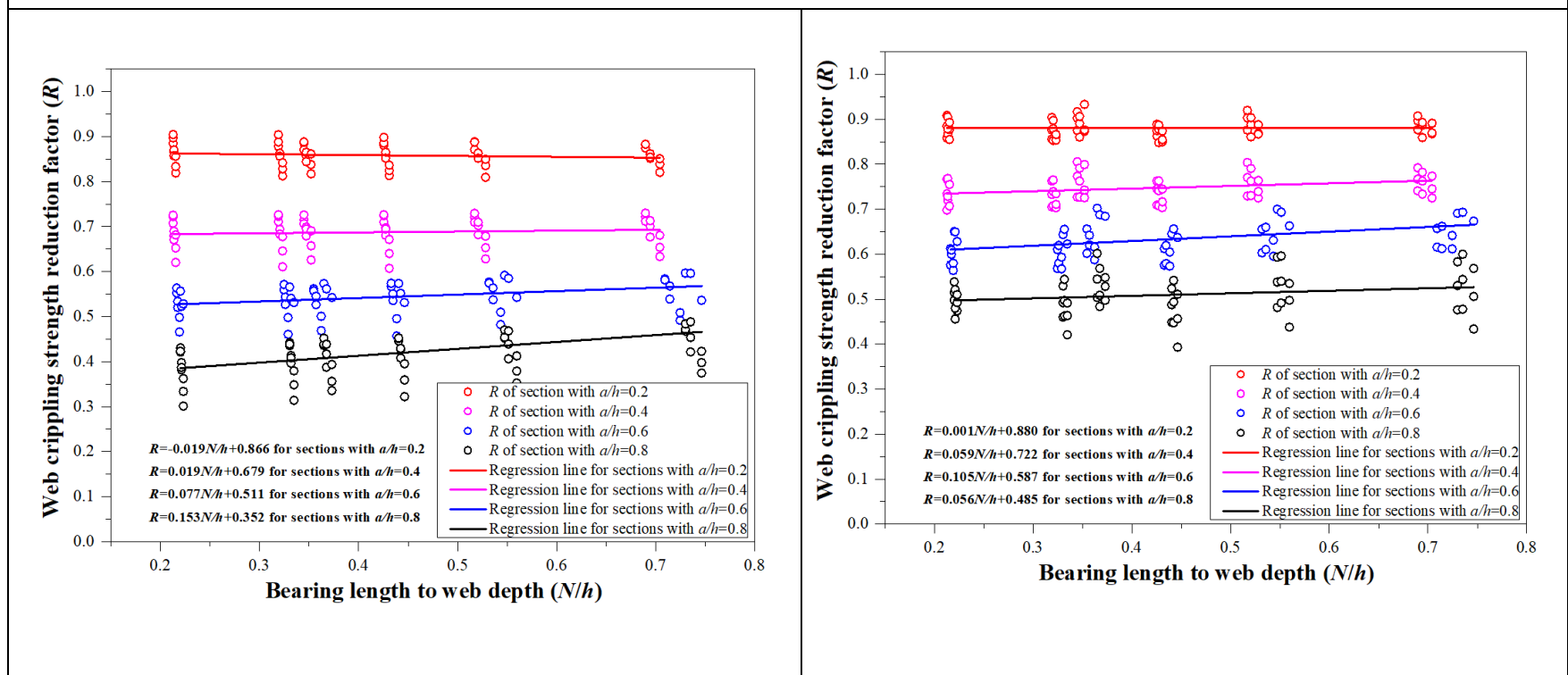


Fig.5 Effect of  $r/t$ ,  $N/t$ ,  $h/t$  and flange type

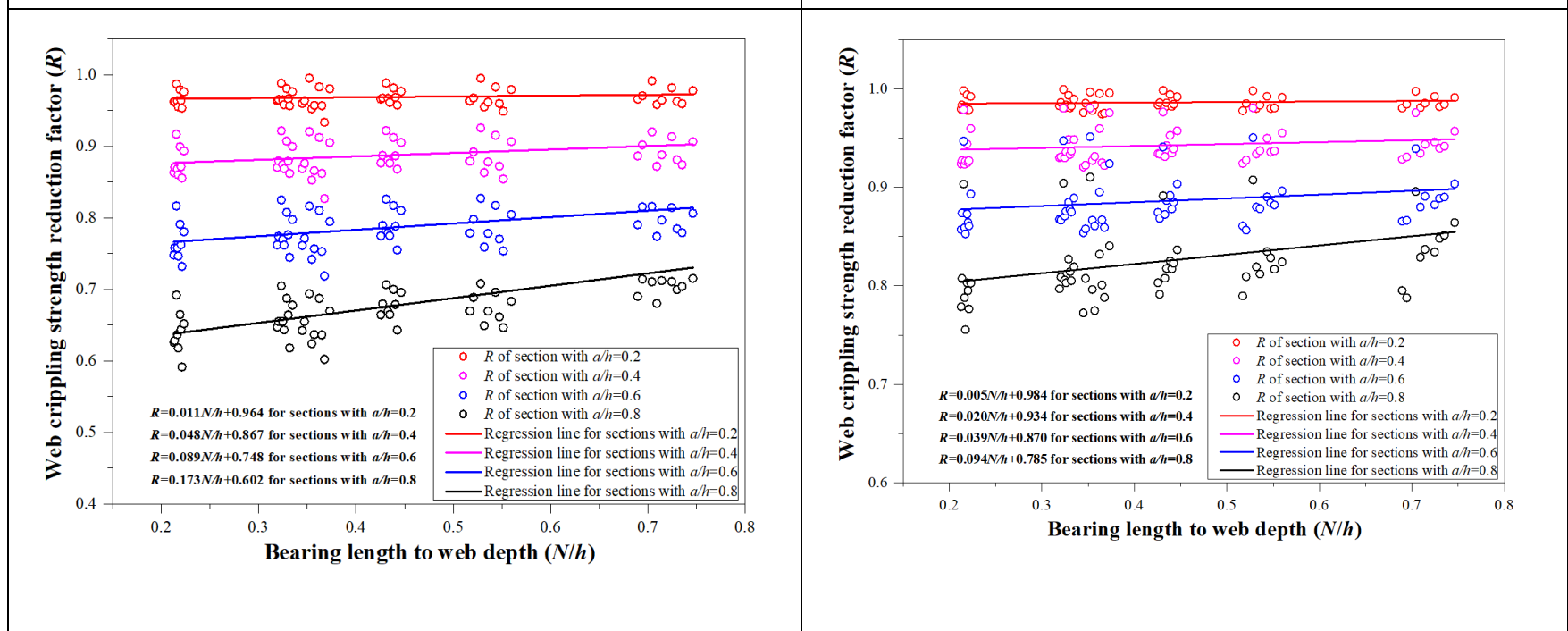


(a) Effect of  $a/h$



(i) RFA unlippped channels with un-fastened flanges and centred web holes

(ii) RFA unlippped channels with fastened flanges and centred web holes



(iii) RFA unlippped channels with un-fastened flanges and offset web holes

(iv) RFA unlippped channels with fastened flanges and offset web holes

(b) Effect of  $N/h$

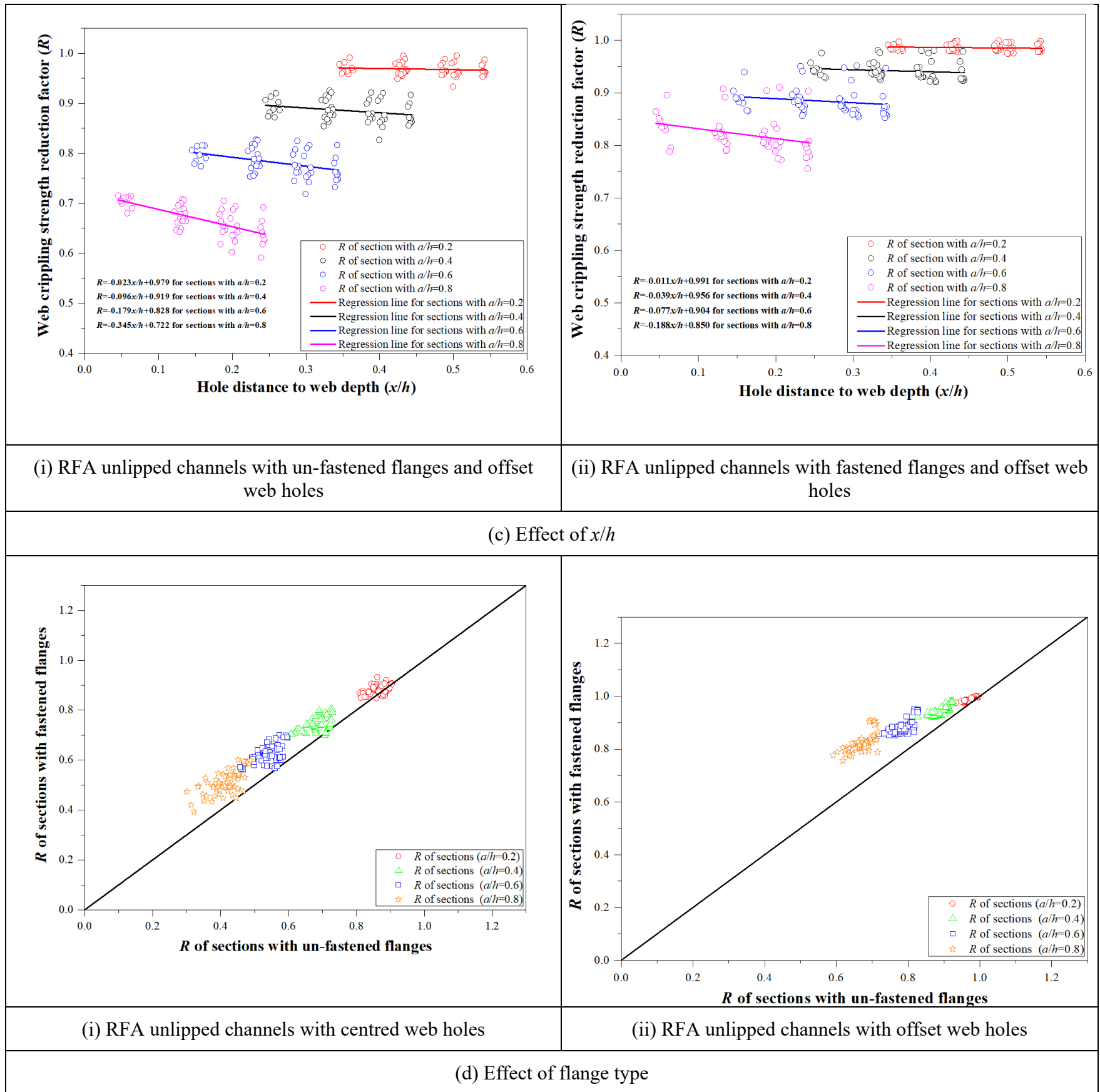


Fig.6 Effect of  $a/h$ ,  $N/h$ ,  $x/h$  and flange type