

Local and distortional buckling behaviour of aluminium alloy back-to-back channels with web holes under axial compression

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Abstract: Aluminium alloy back-to-back channels are becoming popular in building structures. These back-to-back channels often include web holes for installation of services. No previous research, however, is available in the literature for compressive behaviour of aluminium alloy back-to-back channels with web holes. This paper presents an experimental and numerical investigation on the behaviour of screw fastened back-to-back built-up aluminium alloy stub and short columns with web holes under axial compression. Fourteen tests were conducted in total, the results of all are reported in this paper. Prior to compression tests, tensile tests were conducted to determine the material properties of test specimens and initial geometric imperfections were also measured using a laser scanner. A non-linear finite element (FE) model was then developed, and the results were compared against the experiment results showing a good match in terms of both the axial strength and failure modes. Based on 720 FE models, a comprehensive parametric study was conducted to investigate the effects of hole size, screw spacing, section thickness, column length and modified slenderness on structural behaviour of back-to-back built-up aluminium alloy channel columns. Furthermore, the performance of current design guidelines by Australian/New Zealand Standards (AS/NZS) and the American Iron and Steel Institute (AISI) standards was assessed by comparing the axial strengths obtained from the experiments and FEA. It is shown that the AISI & AS/NZS (4600:2018) are conservative by 10% on average, when compared against the test results. Parametric study results were used to propose the axial strength reduction factor equations for aluminium alloy back-to-back channels, and thereafter a reliability analysis was performed.

26 The results of reliability analysis showed that the proposed equations could closely predict the
27 reduced axial strength of aluminium alloy back-to-back channels with web holes.
28 **Keywords:** Axial compression test, finite element analysis, aluminium alloy, web hole, built-
29 up section

30 **1 Introduction**

31 In recent years, the use of aluminium alloy structural members has seen a significant
32 increase due to its attractive attributes such as excellent corrosion resistance, high strength to
33 weight ratio, ease of maintenance, convenience for transportation and recyclability. In order to
34 achieve higher strengths and better resistance against different buckling failures, these channels
35 can be connected back-to-back, with the help of intermediate screw fasteners [1]. On another
36 note, the channels often include web holes for installation of services. Such web holes,
37 however, reduce the axial strength of channel sections [2-7]. This paper investigates the local
38 and distortional buckling behaviour of aluminium alloy back-to-back channels (BTB) with web
39 holes (see Fig. 1). A total of 14 new experimental tests and 720 finite element analyses (FEA)
40 results are reported in this paper.

41 Design rules for aluminium single channels are available in the Aluminium Design
42 Manual (ADM) [8], Australian/New Zealand Standards (AS/NZS) [9-10] and Eurocode 9
43 (EC9) [11]. However, the design recommendations for axial capacity of aluminium BTB
44 channels are not included in these standards. Based on the guidelines of American Iron and
45 Steel Institute (AISI) [12] and Australian and New Zealand Standards (AS/NZS) [13], the axial
46 strength of built-up columns with web holes can be calculated by introducing modified
47 slenderness and reduced section properties. However, these design rules are for carbon steel
48 instead of aluminium alloy, but the calculation results from Roy et al. [14] have shown that the
49 carbon steel design rules of AISI [12] and AS/NZS [13] could be used to calculate the axial
50 strength of aluminium BTB channels accurately. This paper has therefore used the design rules
51 of carbon steel built-up channels in accordance with the AISI [12] and AS/NZS [13], while
52 calculating the axial strength of aluminium alloy BTB channels with web holes.

53 In terms of the cold-formed carbon steel built-up section columns, Wang et al. [15]
54 investigated the structural performance of back-to-back channels with web holes under axial
55 compression. Similarly, Stone and LaBoube [16] studied the effects of web holes on the axial
56 strength of double-limb built-up columns. Roy et al. [17-21] carried out similar research where
57 experimental tests and FEA of different cross sections of built-up columns were performed
58 (Figs. 2(a) and 3(b)). Fratamico et al. [22-23] conducted experimental tests on the buckling
59 behaviour of cold-formed steel (CFS) BTB channels. Moreover, Dabaon et al. [24-25] and
60 Anbarasu et al. [26-27] conducted experimental tests and numerical simulation on the axial
61 compressive behaviour of CFS built-up channels (Fig.2(c)). Most recently, Roy et al. [28]
62 studied the axial compressive behavior of face-to-face built-up CFS channels (Fig.2(d)). In
63 terms of CFS built-up sections with stiffeners, Zhang and Young [29-31] studied the structural
64 performance of built-up CFS channels with stiffeners subjected to axial compression (Figs.2(e)
65 and 2(f)).

66 Stainless steel built-up columns are also popular among engineering applications [32].
67 Current design guidelines in accordance with the AS/NZS [33], AISI [12], and ASCE [34]
68 provide design recommendations for calculating the axial strength of stainless steel built-up
69 columns. Yuan et al. [35], Roy et al. [36-39] and Dobric et al. [40-41] carried out experimental
70 and numerical studies to investigate the axial compressive behaviour of cold-formed stainless
71 steel built-up channels. Besides, Kechidi et al. [42-43] studied the effects of screws on the
72 structural behaviour of cold-formed stainless steel built-up channels under axial compression.

73 In terms of aluminium alloy sections, most research studies available in the literature
74 cover only single sections. Feng et al. [44-48] studied the mechanical behaviour of perforated
75 aluminium alloy single channel columns and found that the current design guidelines [8-11]
76 are not reliable to predict the axial strength of such aluminium alloy single channels. Pham et

77 al. [49-51] and Mazzolani et al. [52-53] conducted investigations on the buckling behaviour of
78 aluminium alloy channels subjected to axial compression. For calculation method, Young et
79 al. [54-56] applied the Continuous Strength Method (CSM) on the structural behaviour of
80 aluminium alloy channels, and it was concluded that CSM could well predict the axial strength
81 of such members. For aluminium BTB channels, Roy et al. [14] studied the local and
82 distortional buckling behaviour of aluminium BTB channels, however the built-up channels
83 investigated by Roy et al. [14] were non-perforated and it is worth noting that not even a single
84 study is available in the literature which investigated the buckling behaviour of aluminium
85 alloy BTB channel sections with web openings under axial compression.

86 This paper reports the analysis of 14 new experimental tests on the buckling behaviour
87 of aluminium alloy BTB channels with web holes. Prior to experimental tests, the material
88 properties of the investigated specimens were obtained from the tensile coupon tests, and the
89 initial geometric imperfections were measured by a laser scanner. A non-linear finite element
90 (FE) model, which incorporated both material non-linearities and initial geometric
91 imperfections, was then developed and validated against the test results. The current design
92 rules of AISI [12] and AS/NZS [13] were assessed by comparing the results of tests and FEA.
93 A comprehensive parametric study based on 720 FE models was then carried out to investigate
94 the effects of hole size, screw spacing, section thickness, column length and modified
95 slenderness on the axial strength of such columns. Finally, design equations in the form of axial
96 strength reduction factors were proposed for aluminium alloy BTB channels with web holes.
97 A reliability was then conducted, which showed that the proposed reduction factor equations
98 could closely predict the axial strength of aluminium alloy BTB channels with web holes.

99 **2 Experimental tests**

100 *2.1 Test specimens*

101 Axial compression tests of 14 aluminium BTB channels were conducted. Fig.1 and Table
102 1 show the cross-sectional details of test specimens (with two lengths: stub (300 mm) and short
103 (500 mm) columns). The spacing of fasteners and ratios of hole diameters to overall web depth
104 were designed to investigate the effects of varying screw spacing and web hole size on columns
105 with varying length, and the design of screw spacing was based on the clause C4.5 of AISI
106 [57].

107 The specimens were labelled to cover the related details (Fig.3). For example, the label
108 “BU240-t1.98-L300-S50-A0.6” can be interpreted as follows:

- 109 • The number “240” refers to the nominal dimension of the web depth in millimetres i.e.,
110 $d=240$ mm.
- 111 • “t1.98” represents section thickness in millimetres i.e., $t=1.98$ mm.
- 112 • “L300” refers to the column length in millimetres i.e., $L=300$ mm.
- 113 • “S50” refers to the screw spacing in millimetres i.e., $S=50$ mm.
- 114 • “A0.6” represents the ratio of hole diameter to overall web depth i.e., $a/d=0.6$.

115 *2.2 Tensile tests*

116 5052-H32 aluminium alloy was used for the investigated specimens in this paper. The
117 detailed material properties were obtained from the tensile coupon tests. The tensile coupons
118 were cut from the centre of the web plate in the longitudinal direction of the untested
119 specimens. Based on the requirements of British Standard for Testing and Materials [58], the
120 detailed dimensions of coupons were prepared as reported in Table 2. When the tensile coupons
121 were tested in an Instron testing machine (Fig.4) having 50kN- capacity, the tensile strain of

122 the coupons was obtained from a calibrated extensometer. Fig.5 shows the full stress-stain
123 curve of the specimens, and Table 3 listed the detailed material properties of the tested coupons.

124 *2.3 Test setup for compression tests*

125 The aluminium BTB channels were tested in the testing machines under pin-pin support
126 boundary conditions, and an external load cell was used to apply the load through the centre of
127 gravity (CG) of the section. The lubricating oil was applied whenever the test was conducted
128 in the bolt connector which could reduce the effect of friction from the bolt connector on the
129 axial strength. In Fig.6 and Fig.7 are shown the test setup and the pin support. A displacement
130 control with a constant loading rate at 0.02 mm/s was used in the column tests. The
131 displacement was recorded by using the three linear variable differential transformers
132 (LVDTs). LVDT-1 was used to record the axial shortening, and LVDT-2 and 3 were placed at
133 mid-height of the specimens to record the lateral displacement.

134 *2.4 Initial geometric imperfections*

135 A laser scanner was used to measure the initial geometric imperfections of the
136 investigated aluminium BTB channels along six longitudinal lines on the specimens (Fig.8 and
137 Fig.9), and the imperfection data was recorded at every 0.1mm.

138 The imperfection data of a typical profile BU240-t1.98-L500-S100-A0.2 is shown in
139 Fig.10, and the maximum local, distortional, and global imperfection magnitudes of the
140 specimens are listed in Table 4. Local initial imperfection was determined based on the
141 readings recorded along the lines W-1 and W-2 and W-3, as shown in Fig.10(a). Based on the
142 average value of the recorded readings along the line W-2 at the mid height of the columns, the
143 global imperfection was calculated (Fig.10(b)). In Fig.10(c), the distortional imperfection on
144 the flange was calculated based on the data recorded in lines F-1 and F-2. The magnitudes of
145 these imperfections were included in the FE modelling described in section 3.6 of this paper.

146 *2.5 Experimental results*

147 In total, 14 compression tests were conducted, and the test results are listed in Table 1.
148 As can be seen from Table 1, local and distortional buckling modes were observed for all
149 specimens including stub and short columns. Fig.11 shows the failure modes of some test
150 specimens. Fig.12 plots the axial load versus mid-height lateral displacement graphs for
151 BU240-t1.98-L300-S50-A0.2, BU240-t1.98-L500-S100-A0.2, BU240-t1.98-L300-S50-A0.2
152 and BU240-t1.98-L500-S400-A0.2.

153 The axial shortening versus loading behaviour is shown in Fig.13. Prior to the plastic
154 stage, the load-axial shortening behaviour was almost linear up to a load at 105 kN, which is
155 approximately 89.98% of the ultimate failure load (116.69kN) of BU240-t1.98-L300-S50-A0.2
156 specimen. When the tested specimen reached the plastic stage, nonlinear behaviour was
157 observed. Similar observation was noticed for the cases of other test specimens.

158 The effects of hole size on axial strength of aluminium alloy built-up columns were
159 studied and the results are reported in Table 1 and in Fig.14. As shown in Fig.14(a), the axial
160 strength of stub columns (BU240-t1.98-L300-S50) was decreased by 2.93% on average when
161 the a/h ratio was changed from 0 to 0.2. Upon tripling the a/h ratio from 0.2 to 0.6, an average
162 reduction of 7.93% in axial strength was observed for stub columns (BU240-t1.98-L300-S50).
163 From Fig.14(c), it can be seen that the average strength of the short columns (BU240-t1.98-
164 L500-S100) was increased by 1.40%, when the a/h ratio was increased from 0 to 0.2.
165 Meanwhile, the reduction in axial strength was not prominent (by 0.49%) when a/h ratio was
166 increased from 0.2 to 0.6 for short columns (BU240-t1.98-L500-S100).

167 The local and distortional buckling failures were observed for BU240-t1.98-L300-S50-
168 A0.2, where two single channels were connected by five screw fasteners having screw spacing
169 of 50mm. The aluminium BTB perforated channels remained integral at failure, and the

170 localized deformation near the end of the columns was observed at ultimate load, as shown in
171 Fig.11.

172 **3 Numerical simulations**

173 *3.1 General*

174 A nonlinear FE model was developed using ABAQUS [59] software to simulate the axial
175 compressive behaviour of aluminium BTB channels with web holes. The FE model included
176 the nonlinear material properties, initial geometric imperfections and residual stresses.

177 *3.2 Modelling of material properties*

178 The obtained material properties from tensile coupon tests were incorporated into the FE
179 models, and the engineering material curve was converted into a true material curve by using
180 the equations below:

$$181 \quad \sigma_{true} = \sigma(1 + \varepsilon) \quad (1)$$

$$182 \quad \varepsilon_{true(pl)} = \ln(1 + \varepsilon) - \frac{\sigma_{true}}{E} \quad (2)$$

183 Where, σ_{true} and $\varepsilon_{true(pl)}$ are the true stress and strain, respectively. σ and ε are the engineering
184 stress and strain, respectively. E is the young's modulus.

185 *3.3 FE meshing*

186 S4R shell elements and rigid quadrilateral shell elements (R3D4) were used to model the
187 aluminium BTB channels and loading plates, respectively. Mesh sizes of 5 mm × 5 mm and 10
188 mm × 10 mm were used for modelling the channel sections and endplates, respectively.
189 Fig.15(a) shows a typical FE mesh for BU240-t1.98-L300-S200-A0.4.

190 *3.4 Boundary conditions*

191 The aluminium BTB channels with web holes were pin ended columns. As shown in
192 Fig.15(a), the displacements and rotations were applied through the reference points defined at
193 the end plates. The reference points were set at the CG of the cross sections. For the loading

194 applied to the top plate, x- and y- translations were restrained, while z- translation was set as
195 free. Meanwhile, all translations at the bottom plate were restrained through the reference point.
196 It should be noted that both the top and bottom plates were set as free to rotate along the minor
197 axis. Screws were simulated using the MPC beam connector elements.

198 *3.5 Contact modelling*

199 “Surface to surface” contact was used to model the interaction between the webs of two
200 single channels and between the base plates and channels. The normal behaviour of the surface
201 was defined as “hard”, indicating that the penetration between the two surfaces was not
202 allowed. A fixed value of 0.5 was used as the friction co-efficient in the FE model developed
203 using ABAQUS [59]. The value of the friction co-efficient was based on the calibration of the
204 FEA model and its comparison against the test results using different friction coefficient values.
205 The contact between two surfaces can play an important role in load carrying capacity [60-62],
206 and therefore it is important to consider in the effect of friction between two surfaces as also
207 reported by a number of previously published papers [63-70].

208 *3.6 Initial geometric imperfections and residual stresses*

209 Eigenvalue analysis was conducted to determine the contours of local and distortional
210 imperfections, as shown in Fig.15(b). The local and distortional buckling modes were modelled
211 based on the lowest buckling mode obtained from the eigenvalue analysis. The imperfections
212 used in the modelling of aluminium BTB channels with web holes, were scaled to the values
213 given in the experimental program (Table 4). The same technique was also applied by Roy et
214 al. [14] to model the initial geometric imperfection of non-perforated aluminium alloy BTB
215 channel columns.

216 The residual stresses and corner enhancements in the corner portion of the channels were
217 modeled in the FEA, as per the guidelines proposed by Moen et al. [71]. This method was also
218 employed by Fang et al. [72-73].

219 3.7 FE validation

220 In Table 1, the axial strengths obtained from the experimental tests are compared with
221 the FEA strengths. Compared to the experimental results, FE results were close in terms of
222 both the axial strengths and failure modes. Fig.16 shows the deformed shapes of investigated
223 columns obtained from the FEA, showing good agreement with the failure modes obtained
224 from the experiments. Fig.17 plots the load-axial shortening behaviour obtained from the FEA
225 and experiments. In fact, the initial stiffness of the experimental curves is a little lesser than
226 that of FEA curves. This might be a consequence of the gap between the channel and
227 top/bottom supports, during conducting the tests in the laboratory. The mean values of the ratio
228 of test to FEA results (P_{EXP}/P_{FEA}) are 1.03 and 1.02 with the corresponding COVs of 0.01 and
229 0.02, respectively for stub and short columns. Overall, the FE model showed very good
230 agreements with the experimental results.

231 4 Parametric study

232 A parametric investigation based on 720 FE models was carried out to study the effects
233 of different parameters on the axial strength of aluminium BTB channels with web holes. The
234 range of parameters include modified slenderness covering stub and columns, number of screw
235 fasteners (2,3 and 5 number of screws), section thickness from 0.5 to 2.9mm, and column
236 length from 300 to 800mm.

237 Based on the previous research studies [14, 72-73], it was found that the axial strength
238 (P) and the axial strength reduction factor (R) of aluminium BTB channels with web holes

239 depend mainly on the ratio of hole diameter to web depth (a/h), screw spacing (number of
240 screws), section thickness (t), column length (L) and modified slenderness ($(KL/r)_m$).

241 *4.1 Parametric study on the axial strength (P) of aluminium BTB channels*

242 *4.1.1 Effect of a/h ratio on the axial strength (P)*

243 The effect of a/h ratio on the axial strength of aluminium BTB channels was studied.
244 From Fig.18(a), it can be seen that when the ratio a/h was increased, the axial strength of
245 aluminium BTB channels was generally decreased. When the a/h ratio was increased from 0
246 to 0.8, the average axial strengths of aluminium BTB channels were decreased by 2.37%,
247 2.82%, 4.82% and 17.25%, respectively for each increment of a/h ratio by 0.02.

248 *4.1.2 Effect of screw number (n) on the axial strength (P)*

249 Fig.18(b) presents the effect of screw number (n) on the axial strength of built-up
250 columns. When the screw numbers (n) were increased from 2 to 5, the average strength of all
251 sections increased slightly by 2.68%. It should be noted that the average strength of plain
252 sections with 5 screws are higher than that of plain sections with 2 screws (by around 2.27%
253 for nonperforated sections and by 2.78% for perforated sections).

254 *4.1.3 Effect of section thickness (t) on the axial strength (P)*

255 From parametric study results, it was observed that the section thickness (t) significantly
256 affects the axial strength of aluminium BTB channels with web holes, as also shown in Table
257 5 and Fig.18(c). With the increase of t from 0.5mm to 2.9mm, the average axial strength of
258 aluminium BTB plain channels increased from 12.04kN to 180.52kN, and the values for
259 channels with web holes changed from 11.23kN to 164.65kN.

260 *4.1.4 Effect of column length (L) on the axial strength (P)*

261 It can be seen from Fig.18(d) that when the column length changed from 300mm to
262 800mm, the local and distortional buckling dominate the failure modes. The average strength

263 of all investigated sections was reduced by 12.61%, and 12.78%, respectively for plain and
264 perforated built-up sections, when the column lengths were increased from 300mm to 800mm.

265 *4.1.5 Effect of modified slenderness $((KL/r)_m)$ on the axial strength (P)*

266 As shown in Table 5 and in Fig.18(e), modified slenderness $(KL/r)_m$ also affects the axial
267 strength of aluminium BTB channels. The results from Table 5 and Fig.18(e) demonstrate the
268 reduction in axial strengths by 14.96% and 10.10% on average for plain and perforated built-
269 up sections, respectively, when the modified slenderness $((KL/r)_m)$ ratio was increased from
270 16.51 to 62.73.

271 *4.2 Parametric study on the strength reduction factor (R)*

272 *4.2.1 Effect of a/h ratio on the strength reduction factor (R)*

273 Fig.19(a) shows a downward trend of axial strength reduction factor with the increase in
274 a/h ratio from 0.2 to 0.8. From Table 6, it can be seen that the reduction factors for sections
275 with varied column lengths and number of screws are similar, i.e., 0.98 for sections with the
276 ratio at 0.2; 0.97 for sections with the ratio at 0.4; 0.95 for sections with the ratio at 0.6; 0.85
277 for sections with the ratio at 0.8.

278 *4.2.2 Effect of screw number (n) on the strength reduction factor (R)*

279 Fig.19(b) shows the effect of screw number (n) on the strength reduction factor (R) . There
280 is very little difference of the average strength reduction factors for sections with varied screw
281 numbers, the value being 0.93. There is not much difference of the strength reduction factor
282 (R) from different screw numbers, and thus the effect of screw number (n) on the strength
283 reduction factor (R) is not so important.

284 *4.2.3 Effect of section thickness (t) on the strength reduction factor (R)*

285 The effect of section thickness (t) on the strength reduction factor (R) was also studied in
286 the parametric investigation. From Fig.19(c), it can be seen that when the value of R was varied

287 from 0.72 to 0.99, the average R values for each group of section thickness remained constant
288 at 0.94.

289 *4.2.4 Effect of column length (L) and modified slenderness ($(KL/r)_m$) on the strength reduction* 290 *factor (R)*

291 Figs.19(d) and (e) show that the strength reduction factor (R) varied from 0.72 to 0.99,
292 when the column length (L) was changed from 300mm to 800mm. For section with column
293 length over 700mm (modified slenderness over 39.01), the COVs of the R value are lower than
294 those of the other lengths.

295 **5 Design guidelines for axial strength of aluminium BTB channels**

296 No design guideline is available in the existing standards for axial strengths of
297 aluminium BTB channels with web holes. However, there are design guidelines mentioned in
298 the AISI [12] and AS/NZS [13] for carbon steel built-up columns with web holes. Therefore,
299 the related design rules available in the AISI [12] and AS/NZS [13] for such carbon steel
300 columns with web holes were used in this study. Besides, it should be noted that the aluminium
301 alloy does not have a distinct yield stress, and thus the axial strengths of aluminium BTB
302 channels were determined from the design formulae of CFS perforated channels by replacing
303 the yield stress of carbon steel with the 0.2% proof stress of aluminium alloy material.

304 *5.1 Design rules for CFS back-to-back plain channels*

305 The un-factored design strengths of cold-formed carbon steel built-up columns in
306 accordance with the AISI [12] and AS/NZS [13] standards can be determined using Equation
307 (3) below:

$$308 \quad P_{\text{AISI\&AS/NZS}} = A_e F_n \quad (3)$$

309 The critical elastic buckling stress (F_n) can be determined using Equations (4)-(5) as
310 follows:

311 For $\lambda_c \leq 1.5$, $F_n = (0.658^{\lambda_c^2}) F_y$ (4)

312 For $\lambda_c > 1.5$, $F_n = \left(\frac{0.877}{\lambda_c^2} \right) F_y$ (5)

313 Where non-dimensional critical slenderness (λ_c) was determined using Equation (6):

314
$$\lambda_c = \sqrt{\frac{f_y}{f_{oc}}} \quad (6)$$

315 Where, f_y is yield stress and f_{oc} is the least of elastic flexural, torsional, and flexural-torsional
 316 buckling stress calculated in accordance with the AISI [12] and AS/NZS [13].

317 Modified slenderness ratio was calculated as per equation 7, and was used in all the
 318 design calculations to determine the axial strength of back-to-back built-up columns

319 For $\left(\frac{a}{r_i} \right) \leq 0.5 \left(\frac{KL}{r} \right)_o$, $\left(\frac{KL}{r} \right)_m = \sqrt{\left(\frac{KL}{r} \right)_o^2 + \left(\frac{a}{r_i} \right)^2}$ (7)

320 Where, $(KL/r)_o$ is the overall slenderness ratio; a is the intermediate fastener spacing; and r_i is
 321 the minimum radius of gyration of full unreduced cross-sectional area of an individual shape
 322 in a built-up member.

323 5.2 Design rules for CFS back-to-back channels with web holes

324 The axial strength of CFS back-to-back channels with web holes can be calculated by
 325 following the calculation procedure of section 5.1. The reduction due to the web holes should
 326 be considered in the calculation of section properties.

327 5.3 Comparison of design strengths with test and FE strengths

328 Experimental and FEA strengths were compared with the calculated design strengths in
 329 accordance with the AISI [12] and AS/NZS [13]. From Table 7 and Fig.20, it can be concluded
 330 that the design strengths calculated from the AISI [12] and AS/NZS [13] were conservative by
 331 5%-30%, when compared to the experimental results.

332 **6 Proposed design equations**

333 *6.1 Design equations for aluminium BTB channels with web holes*

334 As mentioned previously, the validated FE models could predict the reduced axial
335 strength of aluminium BTB channels with web holes more accurately compared to the
336 predictions of current design standards. Therefore, the design equations on axial strength
337 reduction factors of aluminium BTB channels with web holes were proposed based on the
338 validated FE models. The limits for the proposed equations are $h/L \leq 0.8$, $h/t \leq 480$ and $a/h \leq$
339 0.8 .

340 Design equations in relation to the a/h ratio were developed for axial strength reduction
341 factors (R_{prop}) based on the regression analysis method employed by Fang et al. [73-76], Roy.et
342 al. [78-80] and Chen et al. [81-83]. The proposed design equations for sections with one circular
343 web hole are given below:

344 For stub columns ($(KL/r)_m \leq 29.05$),

$$345 \quad R_{prop} = 1 + 0.449 \left(\frac{a}{h}\right)^{-0.676} \leq 1 \quad (8)$$

346 For stub columns ($29.05 < (KL/r)_m \leq 62.73$),

$$347 \quad R_{prop} = 1 + 0.506 \left(\frac{a}{h}\right)^{-0.610} \leq 1 \quad (9)$$

348 As for prediction accuracy of the proposed equations, Table 8 shows that the proposed
349 reduction factor R_{prop} is very close to the experimental results, which confirms the accuracy of
350 the proposed design equations.

351 *6.2 Reliability analysis*

352 Using the method mentioned in both Fang et al. [72-76] and Hsiao et al. [84], a reliability
353 analysis was carried out to evaluate the accuracy of proposed design equations. As mentioned

354 in AISI S100-16 [12], any proposed design equation can be considered reliable when the
355 reliability index (β) is greater than or equal to the target reliability index of 2.50. In Table 9,
356 the values of β for aluminium BTB stub and short columns with web holes are over 2.50. This
357 indicates that the proposed design equations can be used to determine the reduced axial
358 capacity of aluminium BTB channels with web holes with high degree of precisions.

359 **7 Conclusions**

360 The paper reported a detailed experimental study on aluminium back-to-back channels
361 with web holes under axial compression. The results from a total of 14 new tests are reported
362 herein. Prior to compression tests, the material properties of test specimens were obtained from
363 the tensile coupon tests, and the initial geometric imperfections were measured by using a laser
364 scanner. The axial strengths, failure modes, load-axial shortening, and load-lateral
365 displacement behaviours were discussed. In the experimental study, the effects of hole size,
366 screw spacing, section thickness, column length and modified slenderness were also
367 investigated.

368 A non-linear finite element (FE) model, which incorporated material non-linearities,
369 initial geometric imperfections and residual stresses, was then developed and validated against
370 the test results. Furthermore, a comprehensive parametric study based on 720 FE models was
371 carried out to investigate the effects of different parameters including hole size, screw spacing,
372 section thickness, column length and modified slenderness on the axial strength of aluminium
373 BTB channels with web holes. The results from the parametric study show that the section
374 thickness (t) affect the axial strength of such aluminium built-up columns significantly. With
375 the increase of t from 0.5mm to 2.9mm, the average axial strength of aluminium BTB plain
376 channels were increased from 12.04kN to 180.52kN, and the values for perforated channels
377 changed from 11.23kN to 164.65kN. However, the effect of modified slenderness on axial

378 strength of stub and short columns was not noticeable. The axial strengths of the investigated
379 sections were reduced by 14.96% and 10.10% on average for plain sections and perforated
380 sections, respectively, when the modified slenderness $((KL/r)_m)$ was increased from 16.51 to
381 62.73. Screw numbers had a limited impact on the axial strength of perforated aluminium alloy
382 BTB channels. The axial strengths of columns were increased by 2.27% and 2.78% on average
383 for plain sections and perforated sections, respectively, with the screw numbers changed from
384 2 to 5.

385 The design strengths obtained from the tests and FEA were compared with the design
386 strengths calculated in accordance with the Australian/New Zealand Standards (AS/NZS), and
387 American Iron and Steel Institute (AISI) standards. The comparison results showed that the
388 AISI and AS/NZS standards are conservative by 10% on average for perforated aluminium
389 alloy BTB columns failed mainly by local and distortional buckling.

390 Finally, design recommendations in the form of axial strength reduction factors have been
391 proposed for the aluminium BTB channels with web holes. Reliability analysis was also carried
392 out to demonstrate the reliability of the proposed design equations while predicting the reduced
393 axial strength of aluminium BTB channels with web holes.

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Notations

a	Screw spacing from the AISI & AS/NZS (4600:2018);
A'	Total length of the web;
A_{eff}	Effective area of the section;
A_g	Gross cross-sectional area;
B'	Total length of the flange;
CFS	Cold-formed steel;
COV	Coefficient of variation;
E	Young's modulus of elasticity;
f_c	Stress from the ADM;
f_{oc}	Least of the elastic flexural, torsional, and flexural torsional buckling stress;
f_{cy}	Compressive yield strength from the ADM;
f_e	Least of the elastic flexural, torsional, and flexural torsional buckling stress;
F_y	Yield stress of the cold-formed steel;
FEA	Finite element analysis;
$(KL/r)_{\text{ms}}$	Modified slenderness;
$(KL/r)_o$	Overall Slenderness from the AISI & AS/NZS (4600:2018);
L	Total length of the back-to-back built-up aluminium alloy channel sections;
LVDT	Linear variable displacement transducers;
n	Screw number;
$P_{\text{AISI&AS/NZS}}$	Axial strength from the AISI & AS/NZS (4600:2018);
P_{EXP}	Axial strength from experiments;
P_{FEA}	Axial strength from the finite element analysis;
r	Radius of gyration;
r_i	Minimum radius of gyration from the AISI & AS/NZS (4600:2018);
S	Longitudinal spacing of screw;
T	Nominal thickness of the channel section;

λ_c	Non-dimensional slenderness ratio as per the AISI & AS/NZS (4600:2018);
σ	Engineering stress;
$\sigma_{0.2}$	Static 0.2% proof stress;
σ_{cr}	Elastic local buckling stress of the plate;
σ_u	Static ultimate tensile strength;
ε	Engineering strain;

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Table 1 Axial strengths and failure modes of back-to-back built-up aluminium alloy channel sections

Specimen	Web	Flange	Length	Lip	Thickness	Spacing	Hole dia	Experimental results	FEA results		AISI&AS/NZS		
	h	B'	L	C'	t	S	a	P_{EXP}	P_{FEA}	P_{EXP}/P_{FEA}	$P_{AISI&AS/NZS}$	$P_{EXP}/P_{AISI&AS/NZS}$	Failure mode
	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(kN)	(kN)		(kN)		
Stub													
BU240-t1.98-L300-S50-A0	240.54	46.57	300.4	20.23	1.98	50	0	120.21	116.58	1.03	118.65	1.01	LB+DB
BU240-t1.98-L300-S50-A0.2	240.48	45.54	300.12	20.27	1.98	50	48.1	116.69	111.72	1.04	117.20	1.00	LB+DB
BU240-t1.98-L300-S50-A0.6	240.92	45.95	300.13	20.97	1.98	50	144.55	107.44	103.3	1.04	104.85	1.02	LB+DB
BU240-t1.98-L300-S200-A0	241.07	46.83	300.07	19.87	1.97	200	0	116.81	115.77	1.01	118.65	0.98	LB+DB
BU240-t1.98-L300-S200-A0.2	240.31	45.41	300.96	20.93	1.97	200	48.06	112.56	109.51	1.03	117.20	0.96	LB+DB
BU240-t1.98-L300-S200-A0.4	240.45	45.25	300.55	20.39	1.97	200	96.18	112.09	109.42	1.02	112.73	0.99	LB+DB
Mean										1.03		1.00	
COV										0.01		0.02	
Short													
BU240-t1.98-L500-S100-A0	240.83	46.76	500.03	20.07	1.98	100	0	105.71	104.66	1.01	93.80	1.13	LB+DB
BU240-t1.98-L500-S100-A0.2	240.06	45.64	500.74	20.61	1.98	100	48.01	104.23	101.62	1.03	93.02	1.12	LB+DB
BU240-t1.98-L500-S100-A0.4	240.48	45.2	500.09	20.01	1.98	100	96.19	103.81	101.21	1.03	90.69	1.14	LB+DB
BU240-t1.98-L500-S100-A0.6	240.55	45.05	500.98	20.41	1.98	100	144.33	103.72	97.82	1.07	86.80	1.19	LB+DB
BU240-t1.98-L500-S400-A0	241	46.63	499.7	20.18	1.98	400	0	106.05	106.83	0.99	93.80	1.13	LB+DB
BU240-t1.98-L500-S400-A0.2	240.72	45.89	500.66	20.05	1.98	400	48.14	105.76	104.38	1.01	93.02	1.14	LB+DB
BU240-t1.98-L500-S400-A0.4	240.11	45.23	500.81	20.65	1.98	400	96.04	105.34	103.98	1.01	90.69	1.16	LB+DB
BU240-t1.98-L500-S400-A0.6	240.54	45.69	500.11	20.82	1.98	400	144.32	103.36	99.75	1.04	86.80	1.19	LB+DB
Mean										1.02		1.15	
COV										0.02		0.03	

Note: LB=Local buckling; DB=Distortional buckling.

Table 2 Tensile coupon dimensions

Gauge length (<i>G</i>)	Width (<i>W</i>)	Thickness (<i>t</i>)	Radius of fillet (<i>R</i>)	Overall length (<i>L</i>)	Reduced parallel length (<i>A</i>)	Grip Length (<i>B</i>)	Grip width (<i>C</i>)
50 ± 0.1	12.5 ± 0.2	1.56 ± 0.05	12.6	200	57	50	20

Table 3 Material properties obtained from the tensile coupon tests

Coupon ID	Thickness, t (mm)	Ultimate stress, f_u (MPa)	Yield stress, f_y (MPa)
BU240-1	1.98	206.40	150.60
BU240-2	1.97	204.80	150.40
Mean	1.98	205.60	150.50

Table 4 Maximum amplitudes of local, distortional, and overall imperfections

Specimen	Local	Distortional	Global
	(mm)	(mm)	(mm)
BU240-t1.98-L300-S50-A0	0.41	0.88	0.89
BU240-t1.98-L300-S50-A0.2	0.55	0.69	0.94
BU240-t1.98-L300-S50-A0.6	0.28	0.79	0.82
BU240-t1.98-L300-S200-A0	0.35	0.89	1.23
BU240-t1.98-L300-S200-A0.2	0.51	1.21	0.68
BU240-t1.98-L300-S200-A0.4	0.53	0.99	1.15
BU240-t1.98-L500-S100-A0	0.60	1.12	1.27
BU240-t1.98-L500-S100-A0.2	0.46	0.75	0.81
BU240-t1.98-L500-S100-A0.4	0.89	1.02	1.02
BU240-t1.98-L500-S100-A0.6	0.68	0.98	1.11
BU240-t1.98-L500-S400-A0	0.92	0.89	1.23
BU240-t1.98-L500-S400-A0.2	0.80	1.12	1.26
BU240-t1.98-L500-S400-A0.4	0.98	0.99	1.20
BU240-t1.98-L500-S400-A0.6	1.10	0.89	1.11

Table 5 Parametric study results

Specimen	Thickness	Spacing(s)/mm For			Failure Mode(s)	P_{FEA} for plain section			P_{FEA} for section ($a/h=0.2$)			P_{FEA} for section ($a/h=0.4$)			P_{FEA} for section ($a/h=0.6$)			P_{FEA} for section ($a/h=0.8$)		
		2	3	5		2	3	5	2	3	5	2	3	5	2	3	5	2	3	5
	t	screws	screws	screws		screws	screws	screws	screws	screws	screws	screws	screws	screws	screws	screws	screws	screws	screws	screws
	mm	mm	mm	mm		kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN
BU240×45×20-L300	0.50	200	100	50	LB+DB	12.99	13.01	13.16	12.18	12.30	12.27	12.05	12.03	12.06	11.72	11.75	11.76	12.04	12.52	11.33
	1.00					43.55	44.17	44.53	42.66	43.98	44.41	43.47	42.54	42.38	40.37	41.57	40.46	37.30	36.33	43.79
	1.90					115.69	115.75	115.30	114.96	115.56	115.03	114.32	112.79	113.54	108.10	107.28	113.20	99.29	104.89	104.93
	2.10					129.91	129.95	132.02	127.64	129.84	131.71	127.61	127.30	130.57	120.38	125.97	126.67	107.67	114.11	113.23
	2.30					145.14	145.42	145.93	141.64	143.72	144.66	139.43	142.74	145.89	133.08	142.61	140.31	116.03	121.51	121.96
	2.50					160.46	160.66	160.86	157.52	160.40	160.27	151.92	159.40	158.69	146.71	159.05	156.25	124.53	131.10	130.42
	2.70					168.54	174.60	175.54	168.34	173.59	174.98	168.10	172.98	172.86	161.55	173.16	173.28	133.28	139.44	138.98
	2.90					186.33	191.84	192.84	185.99	191.18	192.08	183.17	187.30	187.05	175.12	186.52	187.36	141.75	147.81	147.30
BU240×45×20-L400	0.50	300	150	75	LB+DB	12.31	12.39	12.52	12.01	12.19	12.10	11.83	11.87	11.97	11.44	11.66	11.58	11.13	11.20	11.01
	1.00					43.09	43.16	43.61	43.12	43.03	43.19	42.61	42.56	42.70	40.88	41.30	39.98	38.17	37.78	36.54
	1.90					113.25	113.54	113.60	110.45	110.38	110.25	110.37	109.48	110.13	104.64	104.67	103.18	95.40	95.66	96.67
	2.10					126.76	127.67	127.77	124.59	124.32	123.88	121.96	122.97	122.77	116.47	118.85	117.38	103.97	105.16	105.03
	2.30					135.51	142.48	142.44	132.92	138.69	139.21	133.13	136.00	136.22	130.11	131.86	130.85	113.02	114.14	114.04
	2.50					149.60	158.47	158.52	147.39	153.98	154.62	147.20	149.82	149.63	144.52	146.70	144.77	121.45	122.88	122.81
	2.70					164.20	174.32	174.33	162.91	168.80	170.32	161.19	164.00	164.01	159.70	159.64	156.50	130.09	131.87	131.85
	2.90					181.42	185.10	191.01	178.39	181.42	185.73	180.47	178.86	178.20	170.84	173.71	170.22	138.70	141.11	139.62
BU240×45×20-L500	0.50	400	200	100	LB+DB	11.84	11.95	12.36	11.14	11.17	11.79	11.38	10.89	11.56	11.29	10.32	11.33	10.70	10.02	10.95
	1.00					43.13	43.56	43.89	42.93	43.20	43.53	42.33	42.40	43.41	38.93	39.55	40.24	34.48	34.90	34.96
	1.90					110.27	110.35	110.64	106.52	106.66	107.16	107.65	106.77	107.85	103.30	104.22	104.06	94.93	96.05	96.35
	2.10					124.59	124.68	125.04	121.61	121.27	121.60	120.76	120.70	121.46	115.22	117.23	115.64	105.40	107.05	106.62
	2.30					137.96	137.99	138.52	128.72	134.90	135.52	132.88	133.77	134.07	127.61	130.16	127.49	113.59	116.05	114.58
	2.50					152.26	152.35	153.87	142.61	148.37	150.49	143.70	145.86	147.62	141.97	145.28	142.72	122.05	123.83	122.76
	2.70					164.07	165.94	166.03	160.94	162.35	164.30	162.65	159.17	160.05	160.64	159.36	155.91	133.53	132.33	130.05
	2.90					177.70	184.42	184.74	170.62	177.20	179.81	173.87	173.80	173.96	171.45	173.03	170.63	138.89	141.29	139.21
BU240×45×20-L600	0.50	500	250	125	LB+DB	11.69	11.93	12.52	11.64	11.92	12.13	11.60	11.85	11.85	11.05	11.38	11.31	10.65	11.20	11.21
	1.00					42.60	42.88	42.94	41.24	41.82	41.74	41.96	41.06	42.60	40.27	40.41	39.60	33.56	34.59	34.92
	1.90					104.50	104.82	104.98	101.25	103.72	103.39	101.99	102.91	102.96	99.67	103.38	103.99	94.66	94.64	94.27
	2.10					117.04	117.98	118.02	115.17	117.51	116.25	115.19	117.13	117.81	112.35	117.45	117.08	105.25	104.67	104.13
	2.30					132.26	132.44	132.75	125.36	129.71	131.02	129.95	129.81	131.27	126.48	129.18	129.99	114.73	114.33	113.59
	2.50					147.10	147.26	147.90	135.51	144.90	145.87	137.18	143.21	144.85	136.35	142.86	143.72	121.93	124.40	124.05
	2.70					159.09	161.53	162.56	147.64	158.87	161.38	150.90	157.60	158.96	152.68	156.06	157.42	130.43	133.17	133.11
	2.90					179.94	179.95	180.17	164.41	174.09	177.40	167.19	172.87	173.04	168.18	169.98	171.71	139.48	141.94	142.28
BU240×45×20-L700	0.50	600	300	150	LB+DB	11.19	11.43	11.43	10.88	11.28	11.27	10.71	11.11	11.36	10.09	11.04	10.29	10.54	10.83	10.93
	1.00					41.33	41.34	42.74	41.20	41.11	42.15	40.49	40.37	42.43	40.06	40.30	40.40	34.92	34.10	34.45
	1.90					98.13	98.21	100.09	95.97	97.16	100.07	98.66	96.33	98.86	97.63	95.90	97.57	94.68	93.74	93.04

	2.10					111.49	111.64	113.12	107.94	110.34	112.58	108.94	110.14	111.48	110.14	109.55	108.24	102.73	99.05	103.05
	2.30					124.60	126.17	126.83	120.83	126.14	126.20	121.96	126.10	125.52	122.55	125.66	121.00	111.49	26.96	113.29
	2.50					140.82	141.38	141.59	139.77	139.58	140.15	140.16	139.11	139.59	136.04	139.04	139.04	122.41	121.40	123.35
	2.70					154.29	156.68	156.97	145.07	153.78	155.21	151.81	156.22	156.49	150.65	151.87	154.56	130.90	129.75	132.93
	2.90					173.32	174.55	174.93	159.50	166.79	173.03	161.00	168.29	172.84	163.61	163.26	168.76	137.85	138.65	143.77
BU240×45×20-L800	0.50	700	350	175	LB+DB	11.10	11.35	11.52	10.78	10.71	11.10	10.28	10.36	10.80	9.78	9.90	10.60	9.40	9.97	10.17
	1.00					40.83	41.35	41.90	40.73	40.90	41.89	40.25	40.60	41.77	37.62	39.00	39.02	32.94	33.53	34.29
	1.90					96.10	96.97	106.74	96.05	96.22	101.97	95.80	95.79	105.02	95.49	94.83	105.28	90.19	89.79	89.78
	2.10					107.33	108.75	120.03	104.01	107.34	119.15	103.31	106.66	118.43	103.64	105.89	116.15	101.23	100.12	99.90
	2.30					120.34	123.11	122.87	117.16	120.00	120.83	115.80	119.69	120.59	115.32	119.35	117.75	111.24	109.60	111.74
	2.50					135.14	139.51	139.62	131.46	131.75	139.38	129.60	130.93	138.45	128.71	128.22	136.72	119.85	119.68	122.61
	2.70					152.70	153.24	153.63	141.84	144.21	152.59	150.01	147.64	152.45	147.52	145.90	151.38	128.78	127.43	133.16
	2.90					169.98	170.34	170.77	154.23	157.87	170.56	161.21	156.85	169.30	160.93	153.71	162.05	136.30	136.21	141.68

Note: LB=Local buckling; DB=Distortional buckling.

Table 6 Average axial strength reduction factor (R) of investigated sections

Section type \ Screw number		2	3	5
$L=300\text{mm}$	$a/h=0.2$	0.98	0.99	0.99
	$a/h=0.4$	0.97	0.97	0.97
	$a/h=0.6$	0.93	0.96	0.95
	$a/h=0.8$	0.82	0.85	0.85
$L=400\text{mm}$	$a/h=0.2$	0.98	0.98	0.97
	$a/h=0.4$	0.98	0.96	0.96
	$a/h=0.6$	0.95	0.93	0.91
	$a/h=0.8$	0.83	0.82	0.81
$L=500\text{mm}$	$a/h=0.2$	0.96	0.97	0.98
	$a/h=0.4$	0.97	0.96	0.96
	$a/h=0.6$	0.94	0.93	0.93
	$a/h=0.8$	0.83	0.82	0.82
$L=600\text{mm}$	$a/h=0.2$	0.95	0.98	0.98
	$a/h=0.4$	0.97	0.98	0.98
	$a/h=0.6$	0.95	0.97	0.96
	$a/h=0.8$	0.85	0.86	0.85
$L=700\text{mm}$	$a/h=0.2$	0.97	0.99	0.99
	$a/h=0.4$	0.98	0.98	0.99
	$a/h=0.6$	0.97	0.97	0.96
	$a/h=0.8$	0.89	0.79	0.88
$L=800\text{mm}$	$a/h=0.2$	0.96	0.96	0.99
	$a/h=0.4$	0.97	0.96	0.98
	$a/h=0.6$	0.95	0.94	0.96
	$a/h=0.8$	0.87	0.86	0.86

Table 7 Parametric study results in terms of $P_{FEA}/P_{AISI\&AS/NZS}$

Specimen	Thickness t mm	Spacing(s)/mm For			Failure Mode(s)	$P_{FEA}/P_{AISI\&AS/NZS}$			$P_{FEA}/P_{AISI\&AS/NZS}$			$P_{FEA}/P_{AISI\&AS/NZS}$			$P_{FEA}/P_{AISI\&AS/NZS}$			$P_{FEA}/P_{AISI\&AS/NZS}$		
		2	3	5		for plain section			for section ($a/h=0.2$)			for section ($a/h=0.4$)			for section ($a/h=0.6$)			for section ($a/h=0.8$)		
		screws	screws	screws		2	3	5	2	3	5	2	3	5	2	3	5	2	3	5
		mm	mm	mm		kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN	kN
BU240×45×20-L300	0.5	200	100	50	LB+DB	1.30	1.29	1.30	1.24	1.24	1.23	1.29	1.28	1.28	1.38	1.37	1.37	1.67	1.73	1.56
	1					1.18	1.19	1.20	1.17	1.20	1.21	1.26	1.22	1.21	1.28	1.31	1.27	1.38	1.34	1.61
	1.9					1.06	1.05	1.05	1.07	1.07	1.06	1.10	1.08	1.09	1.12	1.10	1.17	1.17	1.22	1.22
	2.1					1.04	1.04	1.05	1.03	1.05	1.07	1.08	1.07	1.10	1.09	1.14	1.15	1.09	1.15	1.14
	2.3					1.03	1.03	1.03	1.02	1.03	1.04	1.04	1.07	1.09	1.07	1.15	1.13	1.04	1.09	1.09
	2.5					1.01	1.01	1.02	1.01	1.03	1.03	1.01	1.06	1.06	1.05	1.14	1.12	1.00	1.05	1.05
	2.7					0.96	0.99	1.00	0.97	1.00	1.01	1.01	1.04	1.04	1.05	1.12	1.12	0.97	1.01	1.01
	2.9					0.96	0.99	0.99	0.97	1.00	1.00	1.00	1.02	1.02	1.03	1.09	1.10	0.93	0.97	0.97
BU240×45×20-L400	0.5	300	150	75	LB+DB	1.25	1.24	1.25	1.24	1.24	1.23	1.27	1.25	1.26	1.31	1.32	1.30	1.42	1.41	1.39
	1					1.19	1.18	1.19	1.21	1.19	1.19	1.24	1.22	1.22	1.27	1.26	1.22	1.31	1.28	1.24
	1.9					1.22	1.22	1.22	1.20	1.20	1.20	1.23	1.22	1.23	1.23	1.23	1.21	1.20	1.21	1.22
	2.1					1.20	1.21	1.21	1.19	1.19	1.18	1.20	1.21	1.21	1.21	1.23	1.22	1.16	1.17	1.17
	2.3					1.14	1.20	1.20	1.13	1.18	1.18	1.17	1.19	1.19	1.20	1.22	1.21	1.13	1.14	1.14
	2.5					1.13	1.20	1.20	1.12	1.18	1.18	1.16	1.18	1.18	1.20	1.22	1.20	1.09	1.10	1.10
	2.7					1.12	1.19	1.19	1.12	1.16	1.17	1.15	1.17	1.17	1.20	1.20	1.17	1.05	1.07	1.07
	2.9					1.13	1.15	1.18	1.12	1.14	1.16	1.17	1.16	1.15	1.16	1.18	1.16	1.02	1.04	1.03
BU240×45×20-L500	0.5	400	200	100	LB+DB	1.24	1.22	1.26	1.18	1.15	1.21	1.24	1.16	1.22	1.30	1.16	1.26	1.34	1.22	1.33
	1					1.23	1.21	1.21	1.24	1.21	1.21	1.26	1.22	1.24	1.21	1.20	1.21	1.16	1.15	1.14
	1.9					1.27	1.27	1.27	1.24	1.24	1.24	1.28	1.27	1.28	1.29	1.30	1.29	1.26	1.27	1.28
	2.1					1.24	1.24	1.25	1.22	1.22	1.22	1.25	1.25	1.25	1.24	1.27	1.25	1.22	1.23	1.23
	2.3					1.21	1.21	1.21	1.14	1.19	1.20	1.20	1.21	1.21	1.21	1.23	1.21	1.15	1.18	1.16
	2.5					1.18	1.18	1.19	1.11	1.16	1.18	1.15	1.17	1.18	1.19	1.22	1.20	1.10	1.11	1.10
	2.7					1.14	1.15	1.15	1.13	1.14	1.15	1.17	1.14	1.15	1.21	1.20	1.17	1.07	1.06	1.04
	2.9					1.11	1.15	1.16	1.08	1.12	1.14	1.13	1.13	1.13	1.16	1.17	1.16	1.01	1.02	1.01
BU240×45×20-L600	0.5	500	250	125	LB+DB	1.27	1.25	1.29	1.28	1.25	1.26	1.30	1.28	1.27	1.29	1.28	1.26	1.33	1.32	1.31
	1					1.27	1.27	1.27	1.24	1.24	1.24	1.29	1.24	1.29	1.29	1.27	1.24	1.14	1.11	1.12
	1.9					1.22	1.22	1.22	1.19	1.22	1.21	1.22	1.23	1.23	1.24	1.29	1.30	1.25	1.22	1.22
	2.1					1.17	1.18	1.18	1.16	1.19	1.17	1.19	1.21	1.22	1.20	1.26	1.25	1.19	1.16	1.16
	2.3					1.16	1.16	1.16	1.11	1.14	1.16	1.17	1.17	1.18	1.18	1.21	1.22	1.12	1.11	1.10
	2.5					1.14	1.14	1.15	1.06	1.13	1.14	1.09	1.14	1.16	1.13	1.18	1.19	1.05	1.07	1.07
	2.7					1.10	1.12	1.13	1.03	1.11	1.13	1.08	1.12	1.13	1.13	1.16	1.17	1.00	1.02	1.02
	2.9					1.13	1.13	1.13	1.04	1.10	1.12	1.08	1.11	1.11	1.12	1.14	1.15	0.97	0.99	0.99

BU240×45×20-L700	0.5	600	300	150	LB+DB	1.27	1.22	1.21	1.24	1.22	1.20	1.25	1.22	1.23	1.22	1.26	1.16	1.31	1.27	1.27
	1					1.29	1.28	1.32	1.29	1.28	1.31	1.30	1.28	1.35	1.33	1.32	1.32	1.19	1.14	1.15
	1.9					1.14	1.14	1.16	1.12	1.14	1.17	1.18	1.15	1.18	1.20	1.18	1.20	1.20	1.19	1.18
	2.1					1.12	1.12	1.13	1.09	1.11	1.13	1.12	1.13	1.14	1.17	1.16	1.15	1.12	1.08	1.13
	2.3					1.09	1.10	1.11	1.06	1.11	1.11	1.09	1.13	1.13	1.14	1.16	1.12	1.06	0.26	1.08
	2.5					1.09	1.10	1.10	1.09	1.09	1.09	1.11	1.11	1.11	1.12	1.14	1.14	1.03	1.03	1.04
	2.7					1.07	1.09	1.09	1.01	1.07	1.08	1.08	1.11	1.11	1.10	1.11	1.13	0.99	0.98	1.00
	2.9					1.09	1.09	1.10	1.00	1.05	1.09	1.03	1.08	1.11	1.08	1.08	1.12	0.94	0.95	0.98
BU240×45×20-L800	0.5	700	350	175	LB+DB	1.33	1.25	1.25	1.30	1.19	1.21	1.26	1.17	1.20	1.23	1.15	1.21	1.21	1.19	1.19
	1					1.35	1.29	1.31	1.35	1.28	1.32	1.36	1.30	1.33	1.31	1.28	1.28	1.16	1.12	1.15
	1.9					1.14	1.13	1.24	1.14	1.13	1.19	1.16	1.14	1.25	1.18	1.16	1.29	1.13	1.12	1.12
	2.1					1.11	1.09	1.20	1.08	1.08	1.20	1.09	1.09	1.21	1.11	1.12	1.22	1.10	1.08	1.08
	2.3					1.10	1.08	1.08	1.07	1.06	1.06	1.07	1.07	1.08	1.09	1.10	1.08	1.06	1.03	1.05
	2.5					1.10	1.08	1.08	1.07	1.03	1.09	1.07	1.04	1.10	1.09	1.04	1.11	1.02	1.00	1.02
	2.7					1.12	1.06	1.07	1.04	1.01	1.06	1.11	1.05	1.08	1.12	1.06	1.10	0.99	0.95	0.99
	2.9					1.12	1.07	1.07	1.02	0.99	1.07	1.08	1.00	1.08	1.10	1.01	1.06	0.94	0.92	0.95

Table 8 Comparisons of axial strength reduction factors obtained from the experiments and proposed design equations

Specimen	a/h	Experimental results	R_{EXP}	R_{prop}	R_{EXP}/R_{prop}
		P_{EXP} (kN)			
Stub					
BU240-t1.98-L300-S50-A0.2	0.2	116.69	0.97	0.98	0.99
BU240-t1.98-L300-S50-A0.6	0.6	107.44	0.89	0.93	0.96
BU240-t1.98-L300-S200-A0.2	0.2	112.56	0.96	0.98	0.99
BU240-t1.98-L300-S200-A0.4	0.4	112.09	0.96	0.97	0.99
Mean					0.98
COV					0.01
Stub					
BU240-t1.98-L500-S100-A0.2	0.2	104.23	0.99	0.97	1.01
BU240-t1.98-L500-S100-A0.4	0.4	103.81	0.98	0.97	1.01
BU240-t1.98-L500-S100-A0.6	0.6	103.72	0.98	0.96	1.03
BU240-t1.98-L500-S400-A0.2	0.2	105.76	0.99	0.97	1.02
BU240-t1.98-L500-S400-A0.4	0.4	105.34	0.99	0.97	1.02
BU240-t1.98-L500-S400-A0.6	0.6	103.36	0.97	0.96	1.02
Mean					1.02
COV					0.01

Table 9 Results of the reliability analysis for proposed strength reduction factor equations of aluminium BTB channels with web holes

Column type	Stub column	Short column
Ratio of equations	R_{FEA} / R_{prop}	R_{FEA} / R_{prop}
Data number	256	320
Mean, P_m	1.00	1.00
Coefficient of variation, COV	0.04	0.06
Reliability index, β [12]	2.70	2.70
Resistance factor, ϕ [12]	0.85	0.85

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(b) Roy et al. [20-21]

(c) Dabaon et al. [24-25] and Anbarasu et al. [26-27]

(d) Roy et al. [28]

(e) Zhang and Young [29]

(f) Zhang and Young [30-31]

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Fig.19 Parametric effects on axial strength reduction factor of investigated sections

(a) Strength reduction factor of sections against the ratio of a/h

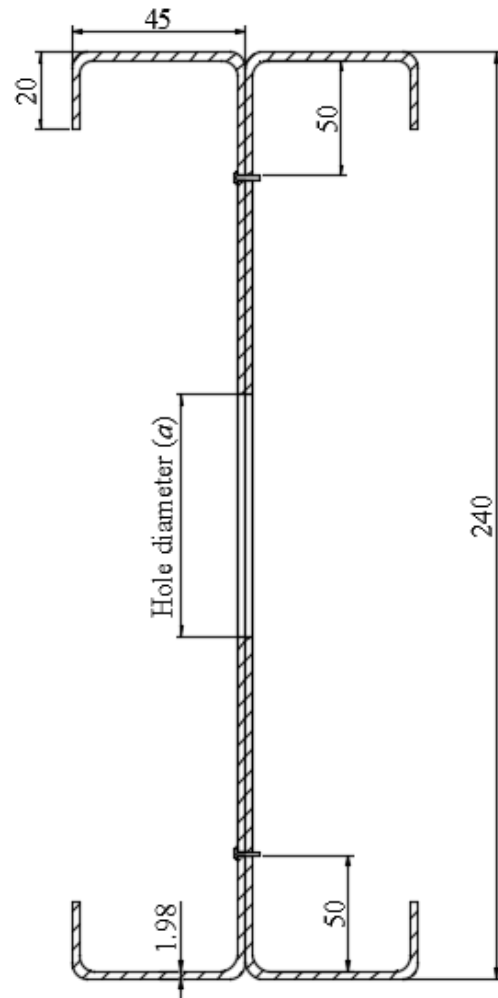
(b) Strength reduction factor of sections against screw number

(c) Strength reduction factor of sections against section thickness

(d) Strength reduction factor of sections against column length

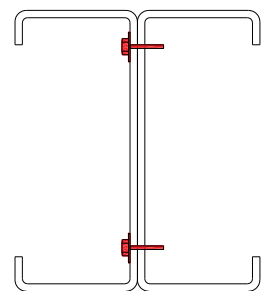
(e) Strength reduction factor of sections against modified slenderness

Fig.20 Comparison of axial strengths obtained from the FEA and the current design standards (AISI & AS/NZS)

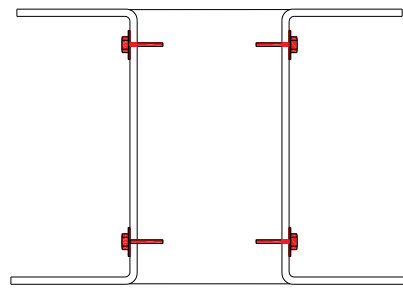


(All dimensions are in mm)

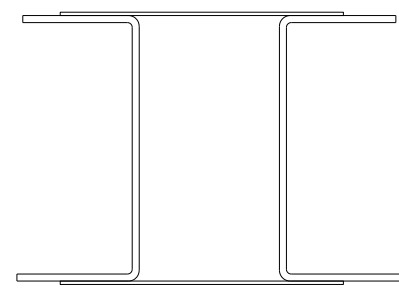
Fig.1 Cross-sectional details of the investigated aluminium alloy built-up channels with web holes



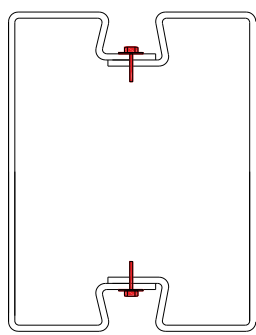
(a) Roy *et al.* [17-19]



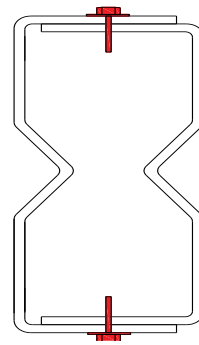
(b) Roy *et al.* [20-21]



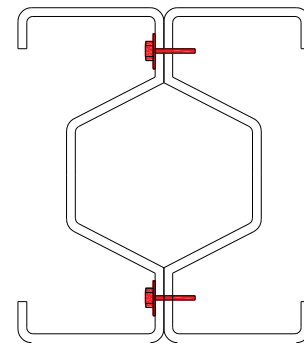
(c) Dabaon *et al.* [24-25] and Anbarasu *et al.* [26-27]



(d) Roy *et al.* [28]



(e) Zhang and Young [29]



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Fig.2 Cross-section of various built-up columns from the literature

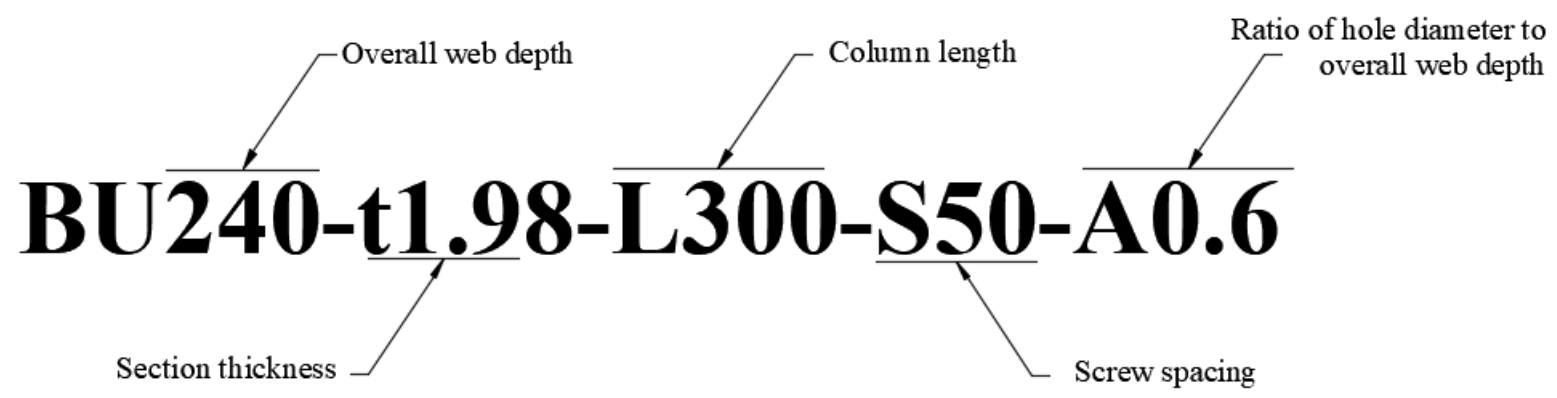


Fig.3 Specimen labelling



Fig.4 Setup of the tensile coupon tests

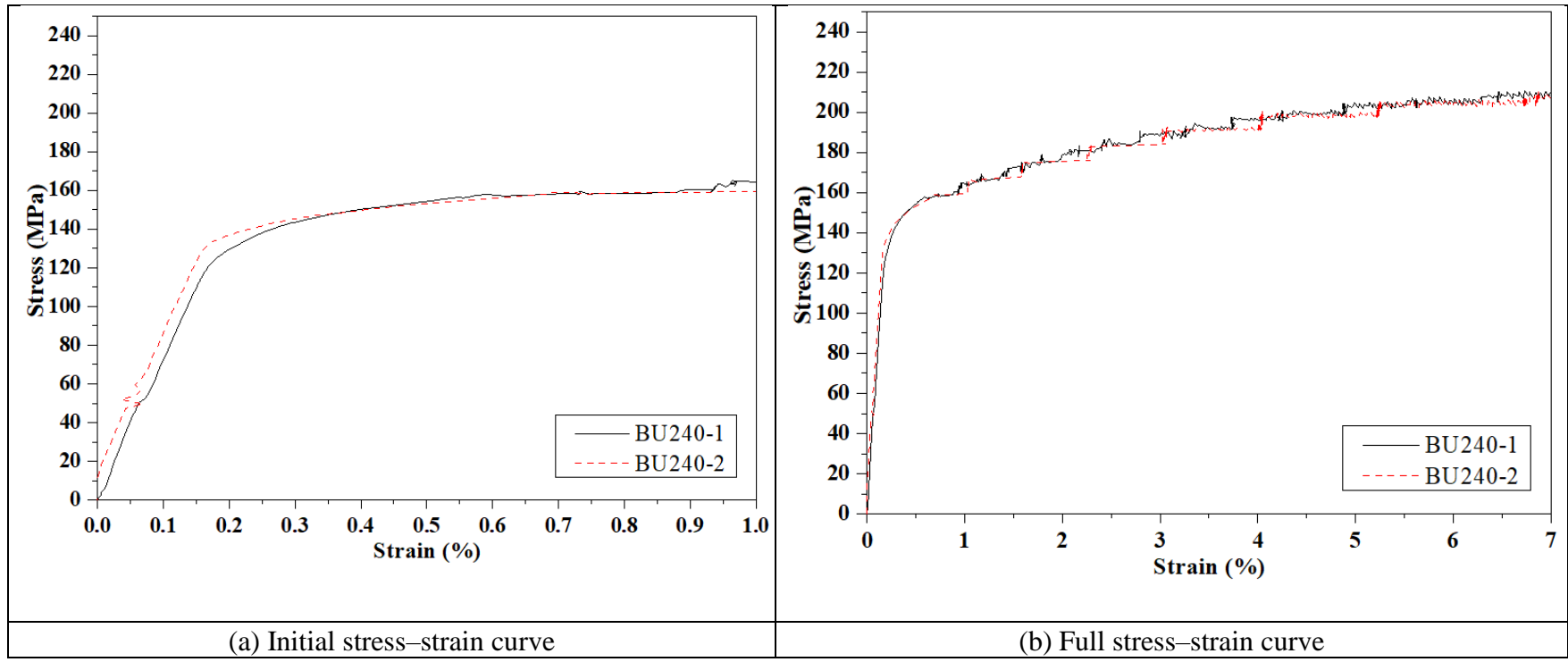


Fig.5 Stress-strain curves [14]

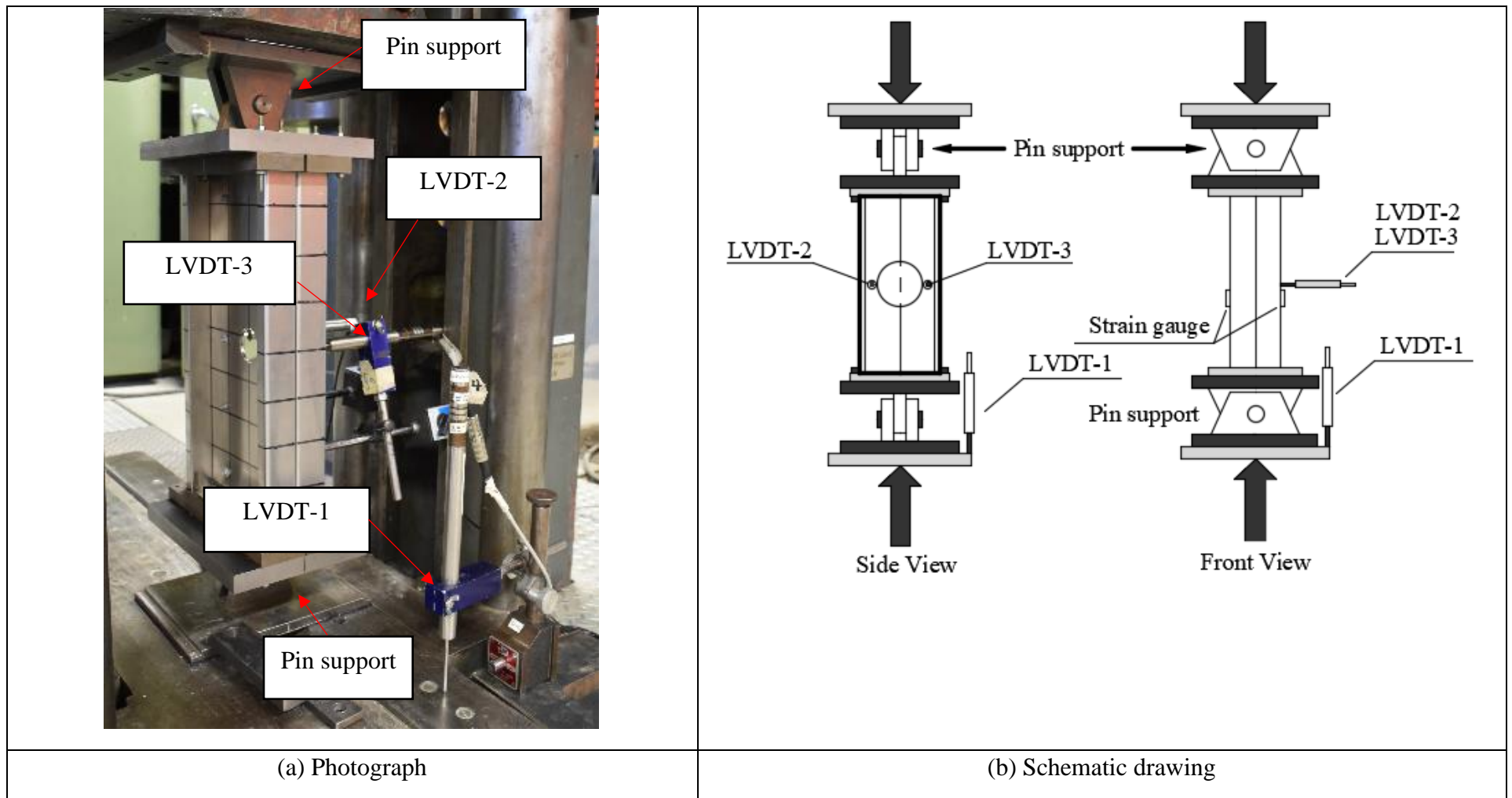


Fig.6 Photograph and schematic drawings of the test set-up



(a) Bottom support



(b) Top support

Fig.7 End plates used in compression tests

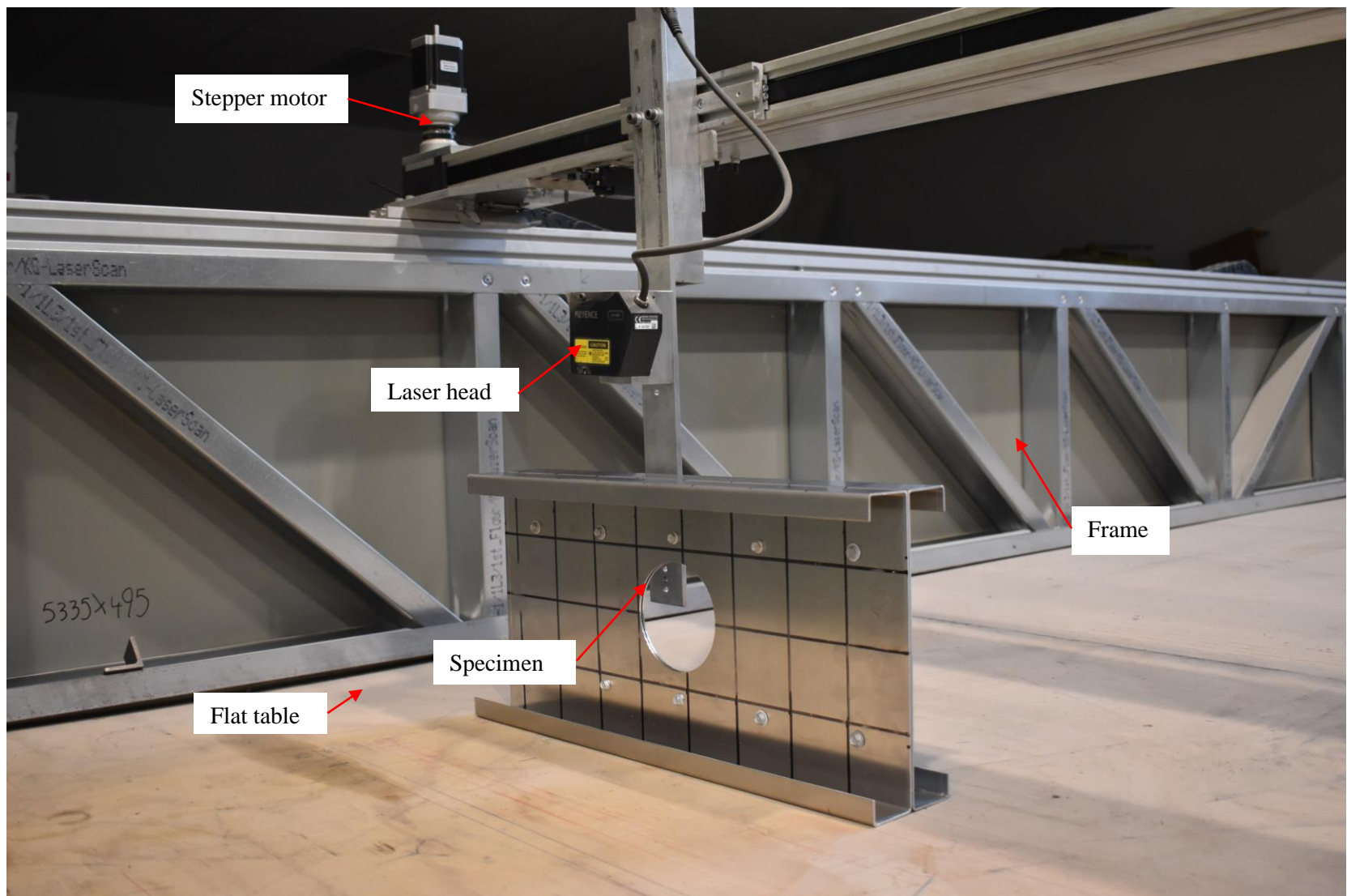


Fig.8 Imperfection measurements setup

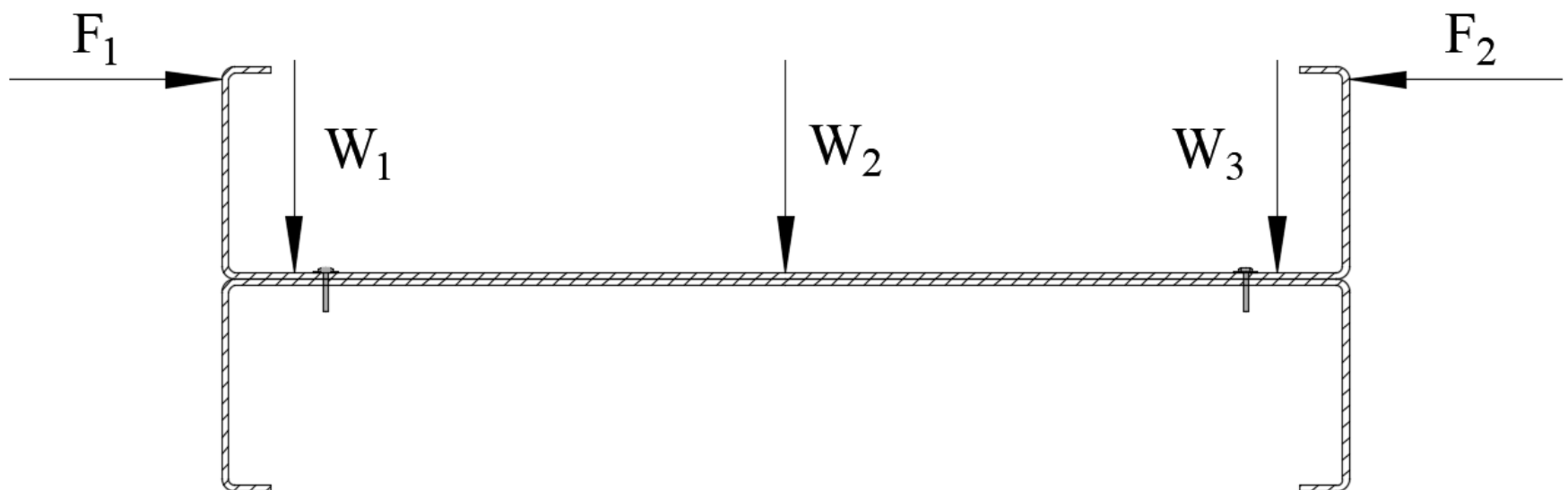
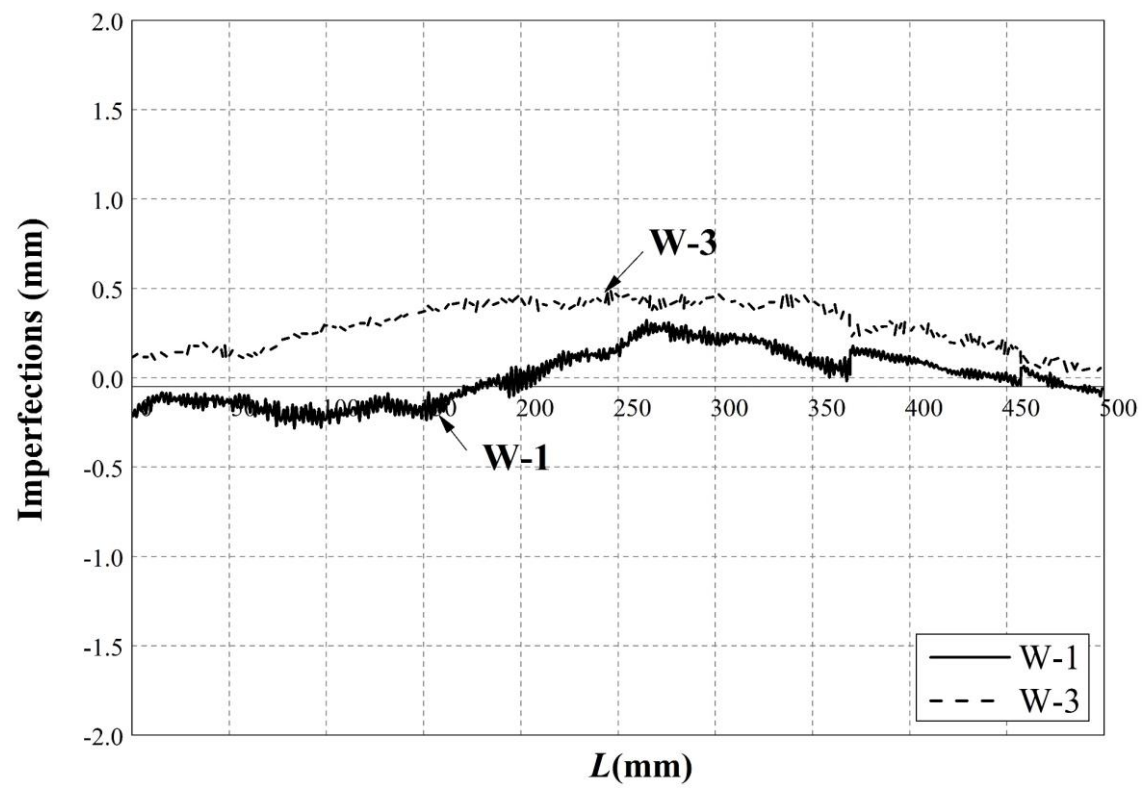
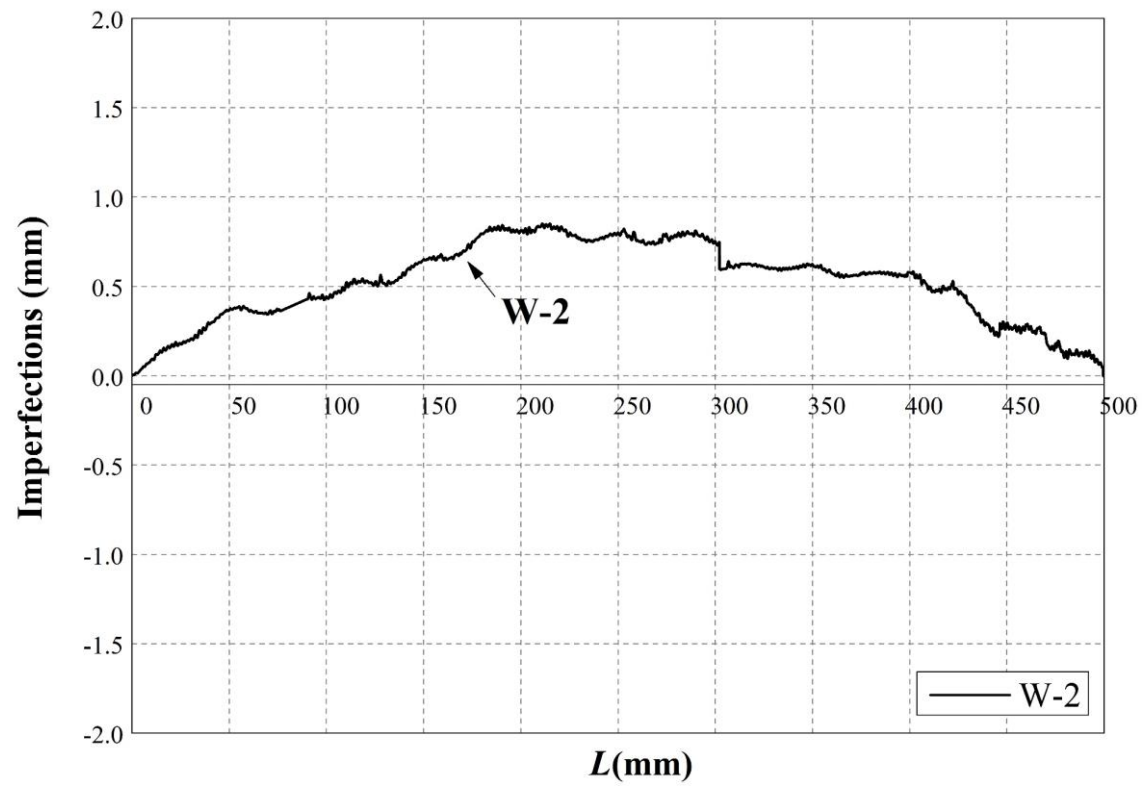


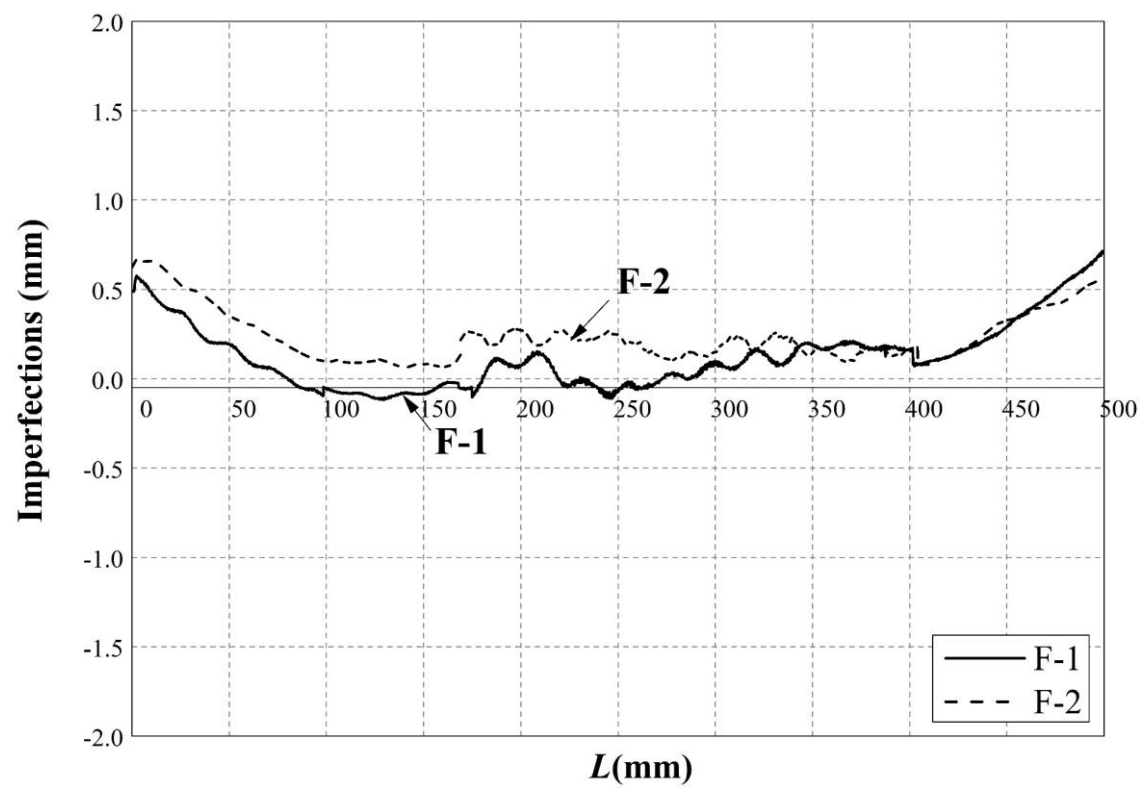
Fig.9 Locations of the initial geometric imperfection measurements



(a) Imperfection of W-1 and W-3



(b) Imperfection of W-2



(c) Imperfection of F-1 and F-2

Fig.10 Typical imperfection profile (BU240-t1.98-L500-S100-A0.2)

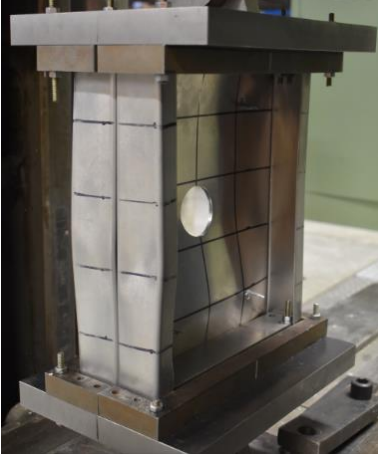
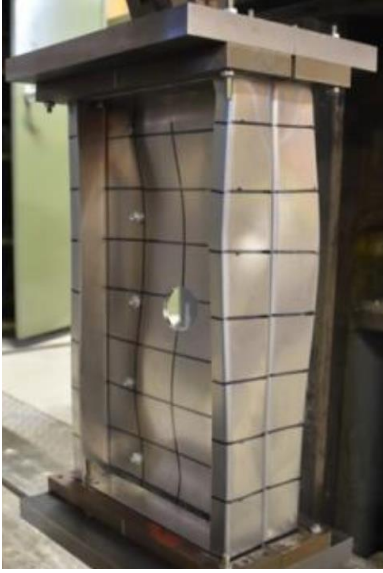

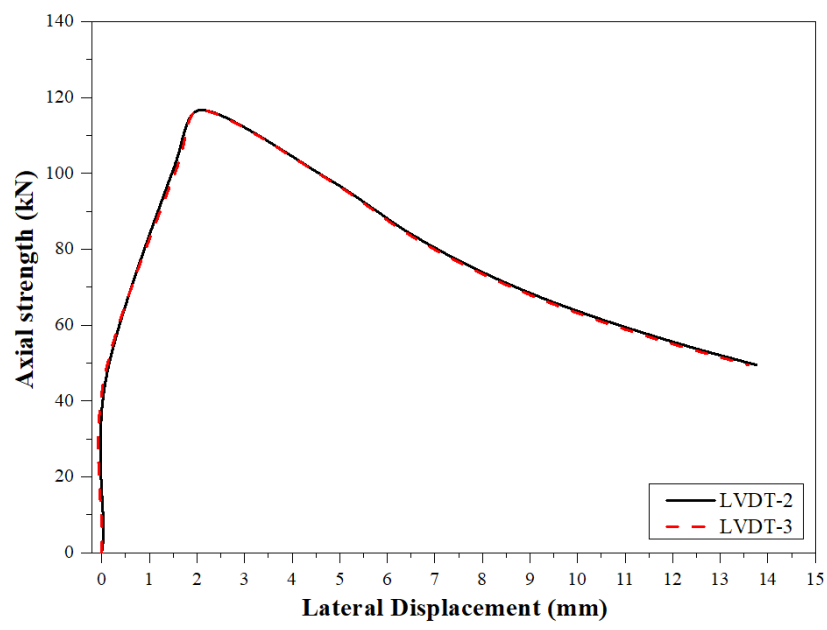
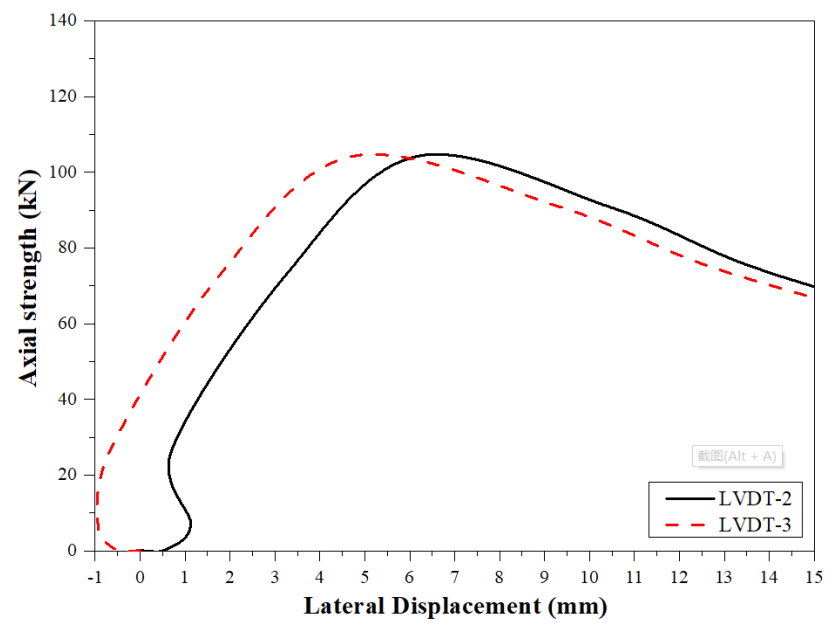
			
(a) BU240-t1.98-L300-S50-A0.2	(b) BU240-t1.98-L300-S200-A0.2	(c) BU240-t1.98-L500-S100-A0.2	(d) BU240-t1.98-L500-S400-A0.2

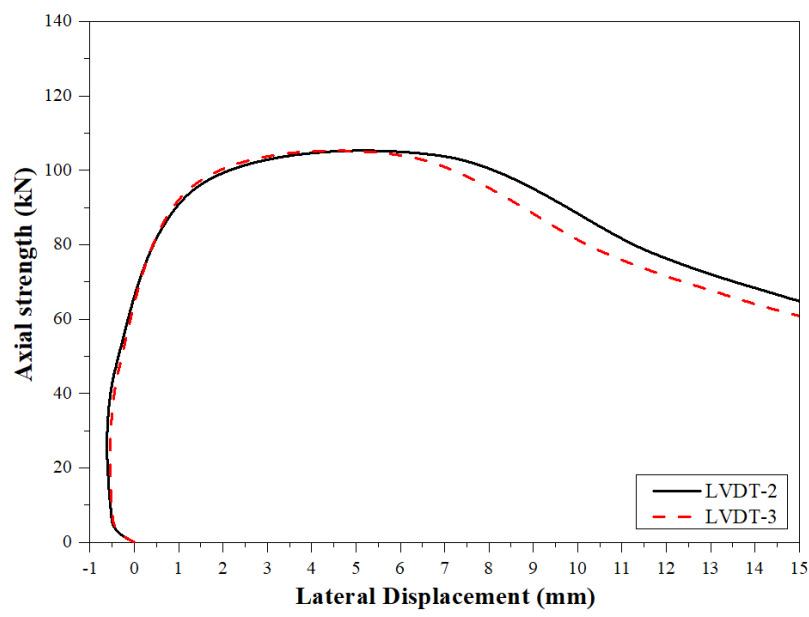
Fig.11 Test pictures of the 300- and 500mm-long sections



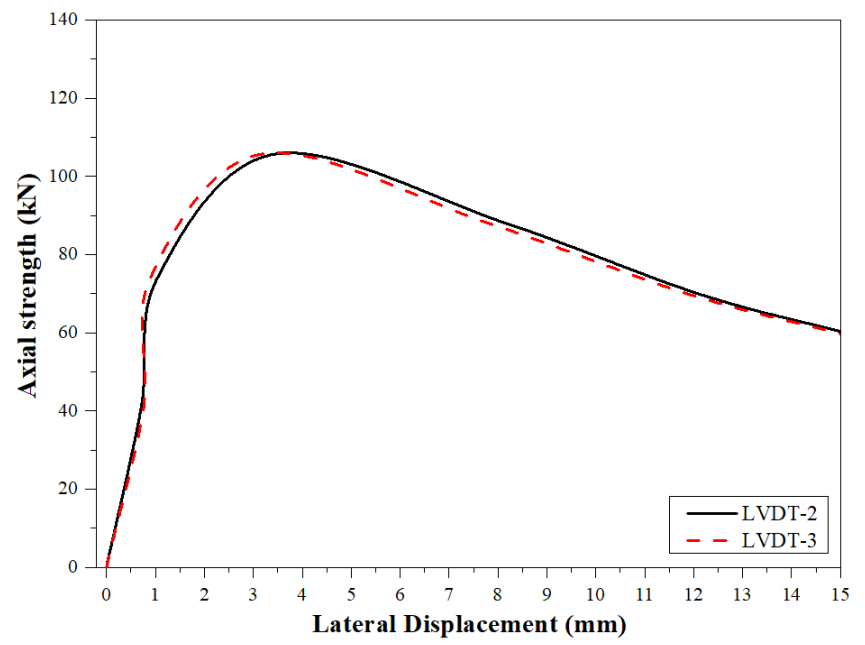
(a) BU240-t1.98-L300-S50-A0.2



(b) BU240-t1.98-L500-S100-A0.2

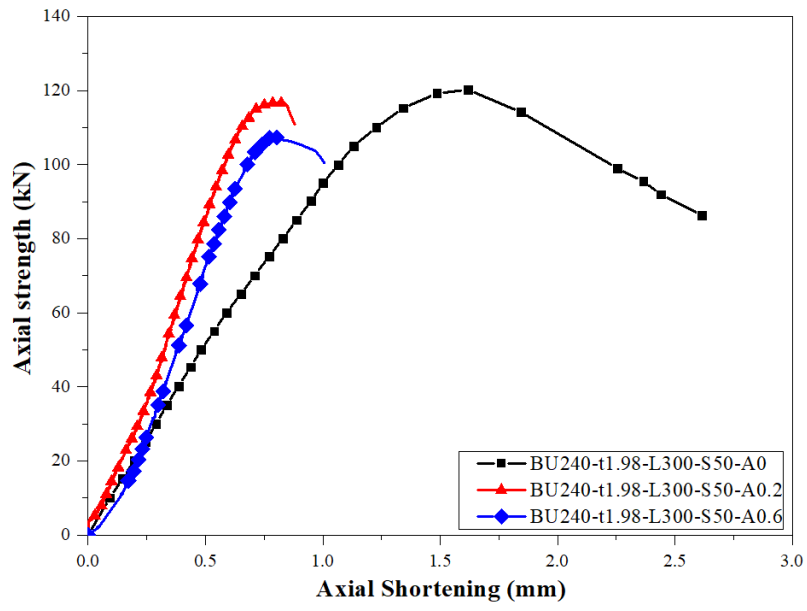


(c) BU240-t1.98-L300-S50-A0.2

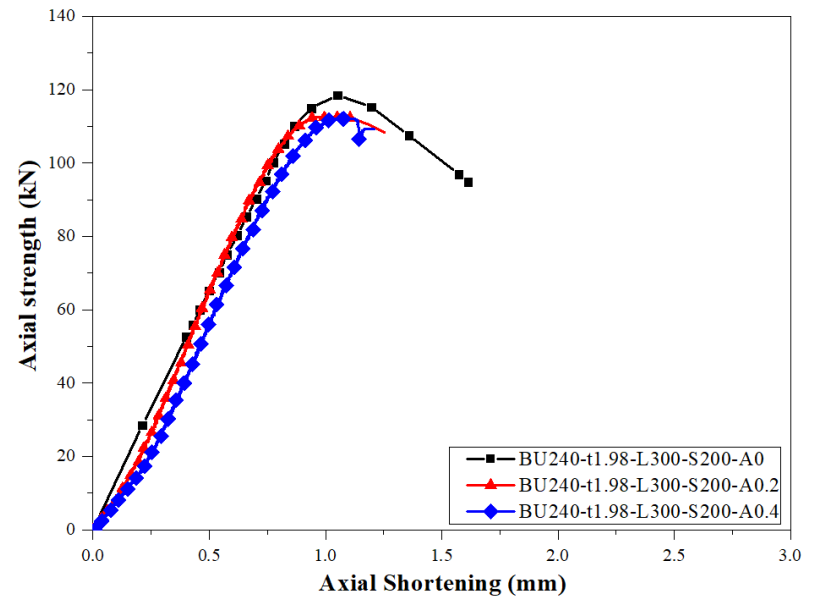


(d) BU240-t1.98-L500-S400-A0.2

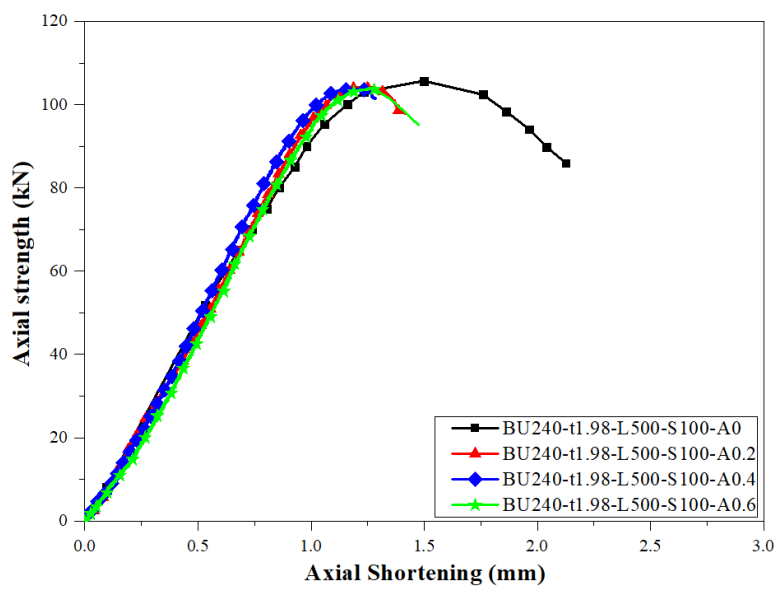
Fig.12 Load versus lateral deflection curves at mid-height



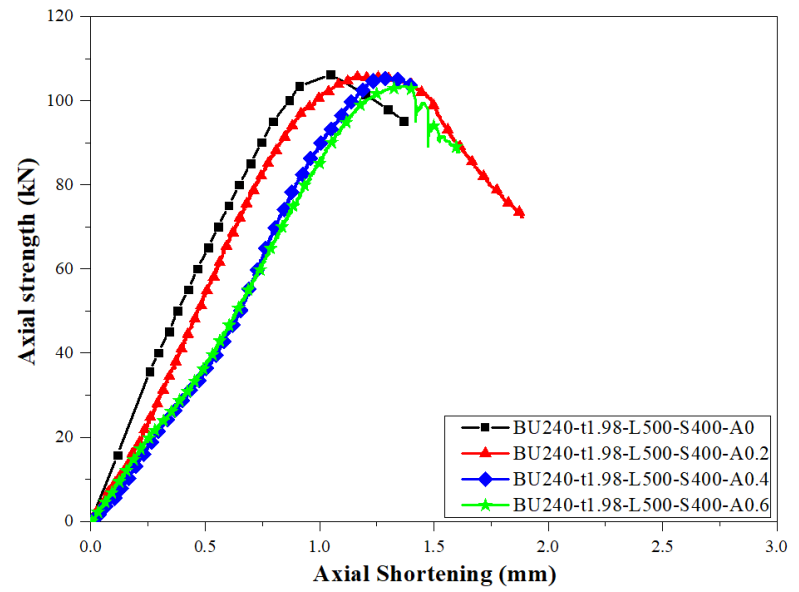
(a) BU240-t1.98-L300-S50



(b) BU240-t1.98-L300-S200

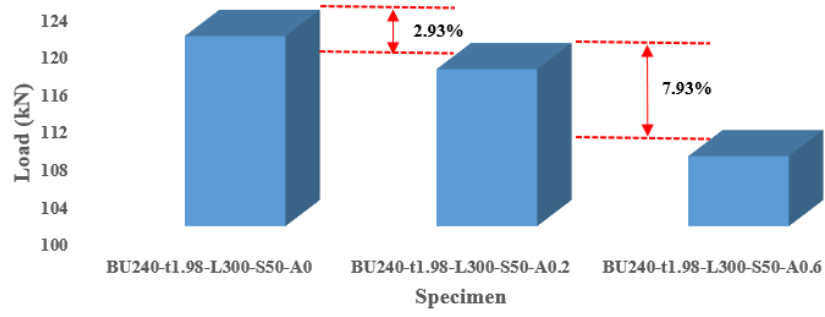


(c) BU240-t1.98-L500-S100

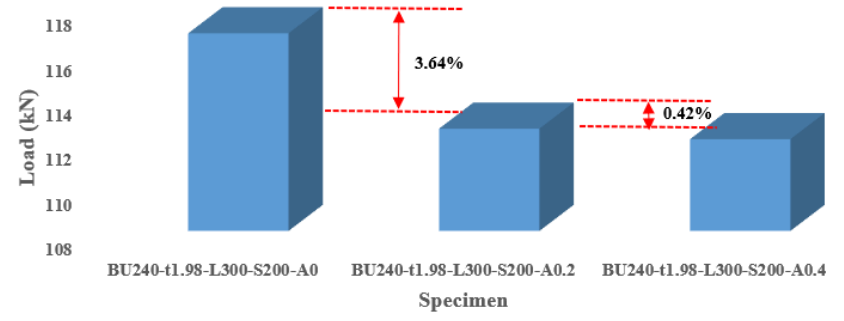


(d) BU240-t1.98-L500-S400

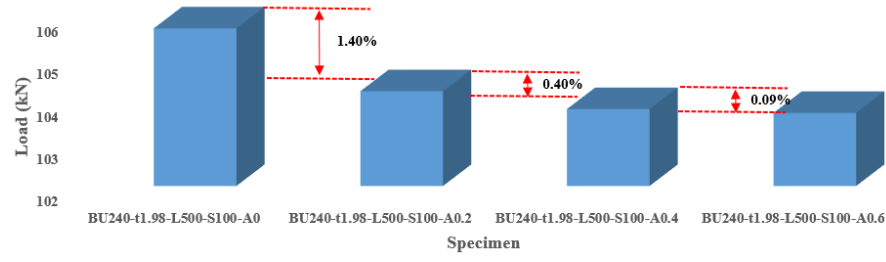
Fig.13 Axial load versus axial shortening curves



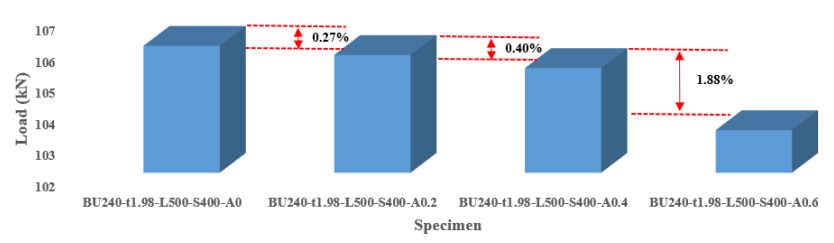
(a) BU240-t1.98-L300-S50



(b) BU240-t1.98-L300-S200

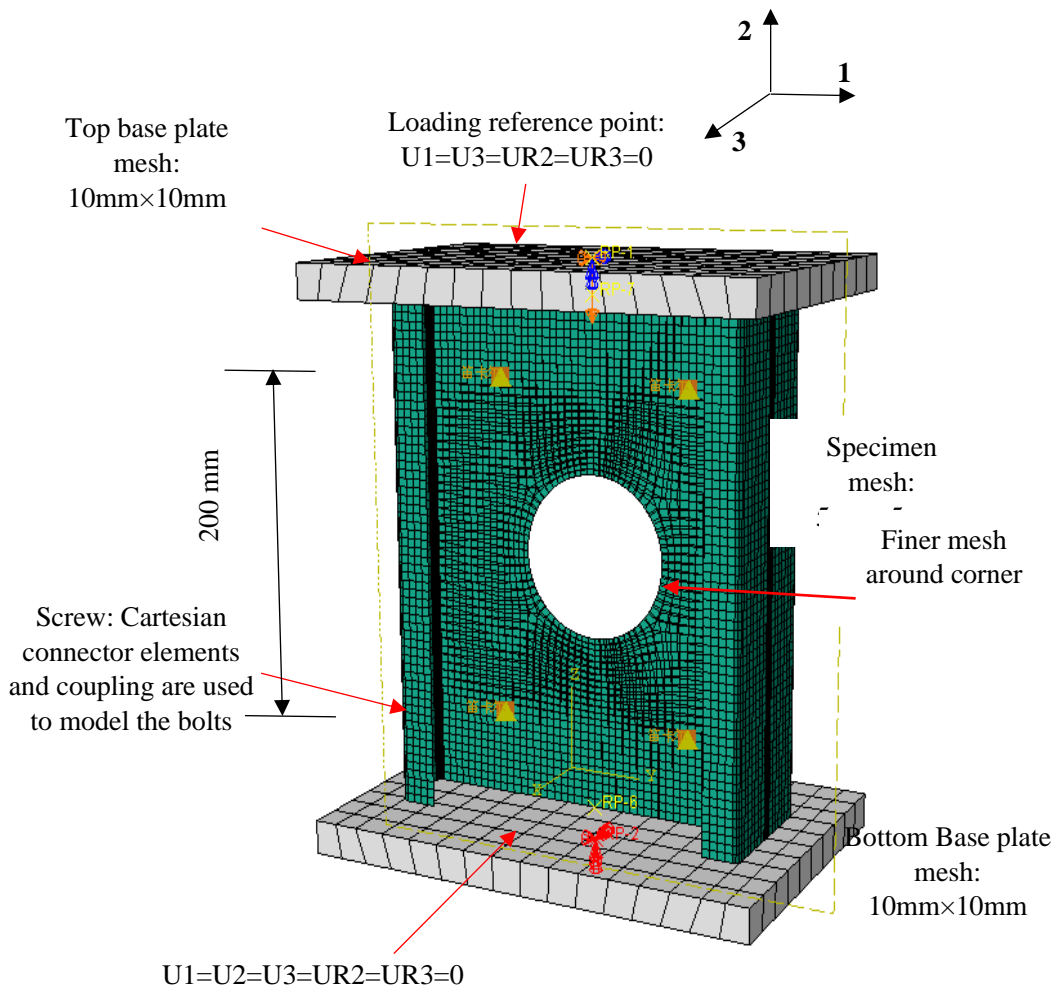


(c) BU240-t1.98-L500-S100

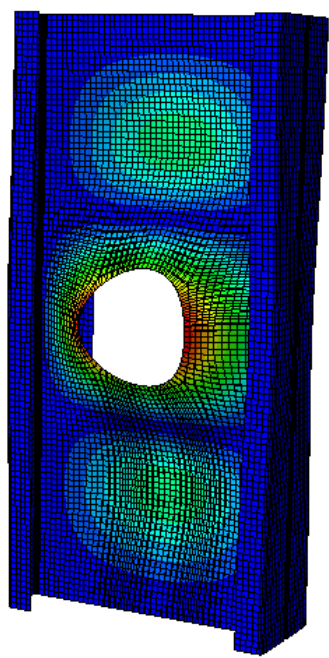


(d) BU240-t1.98-L500-S400

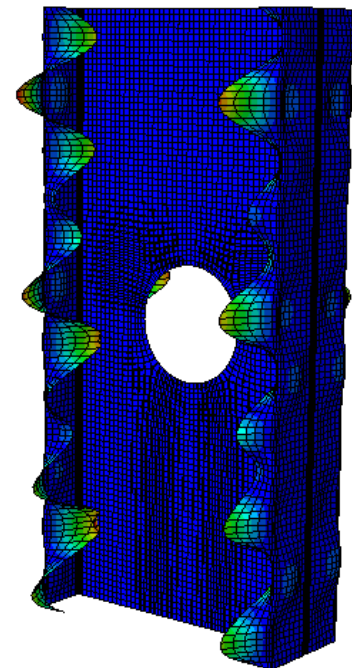
Fig.14 Effect of hole size on axial strength of aluminium BTB channels



(a) Mesh type and boundary condition applied in FE model for BU240-t1.98-L300-S200-A0.4




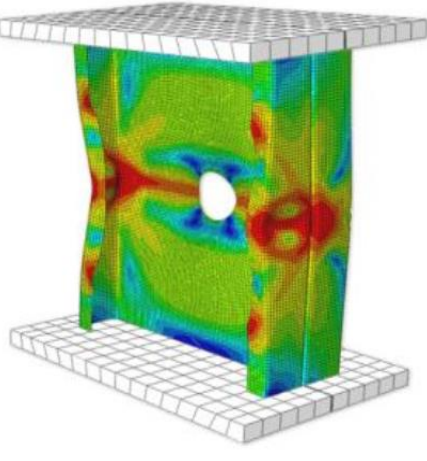
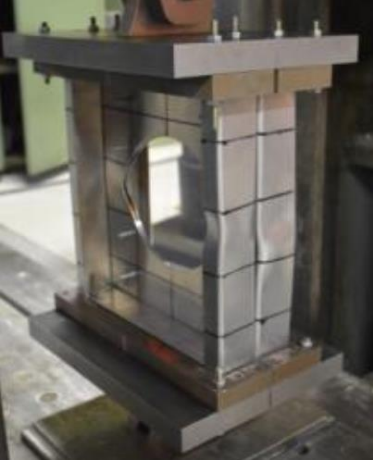
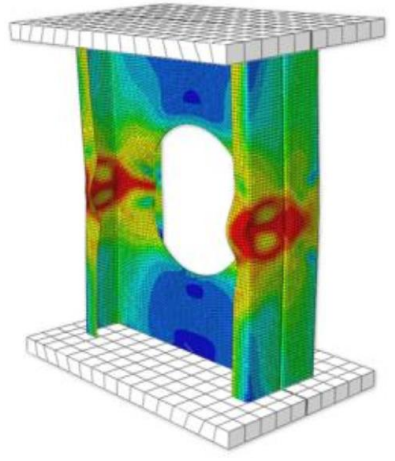
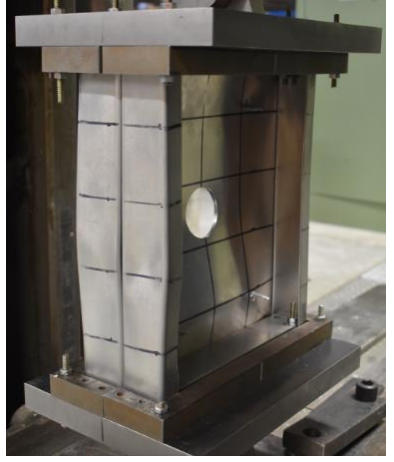
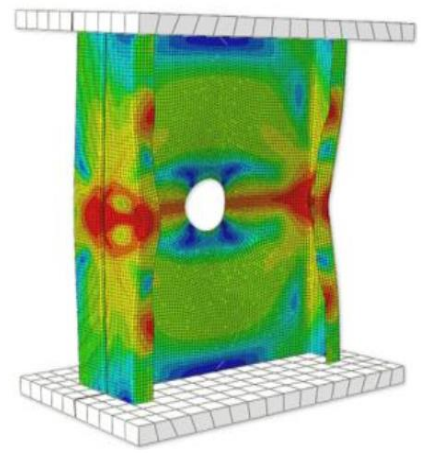

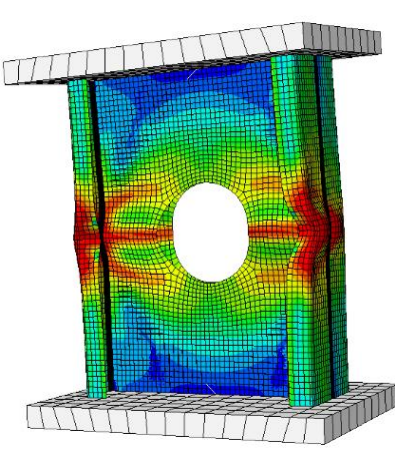

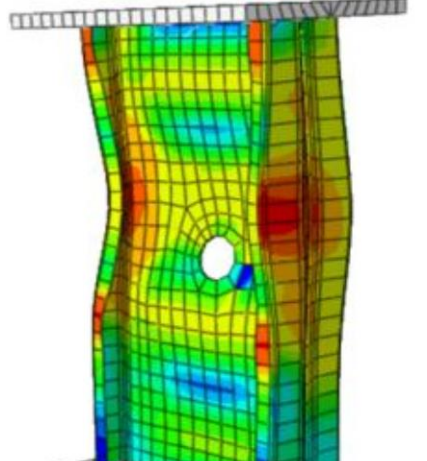

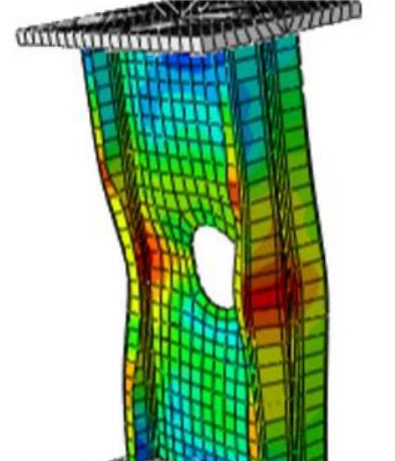

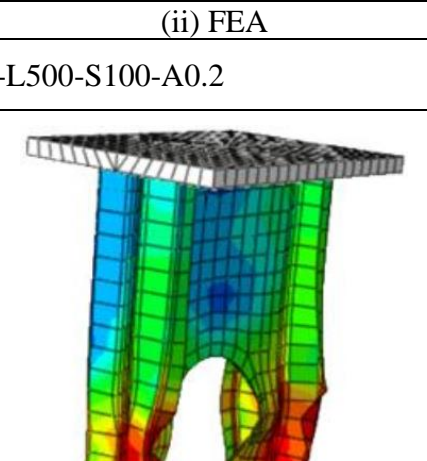
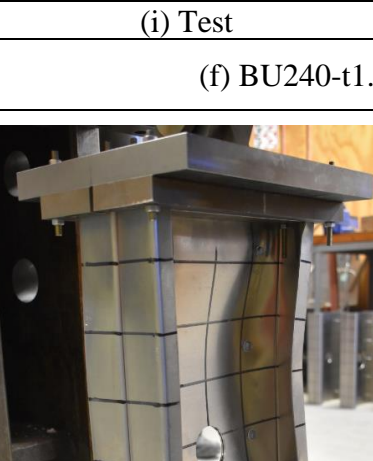
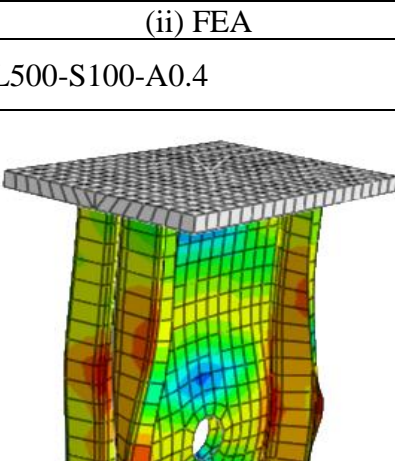
(i) Local buckling



(ii) Distortional buckling

(b) Initial imperfection contours from eigenvalue buckling analysis

Fig.15 Details of the FE model

			
(i) Test	(ii) FEA	(i) Test	(ii) FEA
(a) BU240-t1.98-L300-S50-A0.2		(b) BU240-t1.98-L300-S50-A0.6	
			
(i) Test	(ii) FEA	(i) Test	(ii) FEA
(c) BU240-t1.98-L300-S200-A0.2		(d) BU240-t1.98-L300-S200-A0.4	
			
(i) Test	(ii) FEA	(i) Test	(ii) FEA
(e) BU240-t1.98-L500-S100-A0.2		(f) BU240-t1.98-L500-S100-A0.4	
			
(i) Test	(ii) FEA	(i) Test	(ii) FEA
(g) BU240-t1.98-L500-S100-A0.6		(h) BU240-t1.98-L500-S400-A0.2	


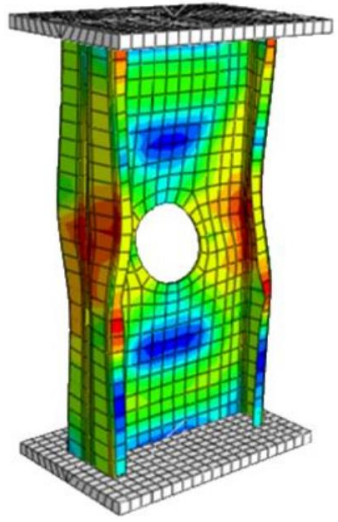

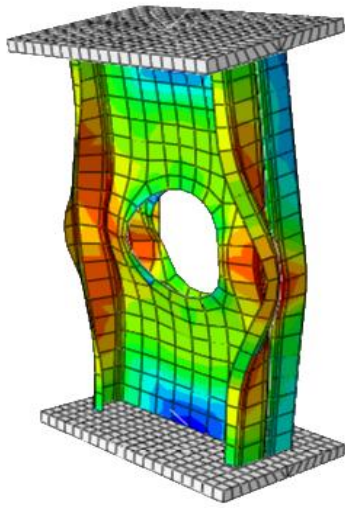
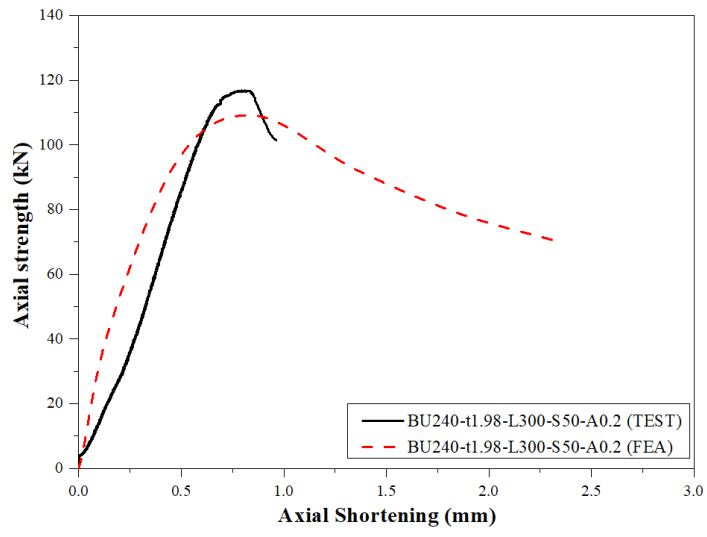
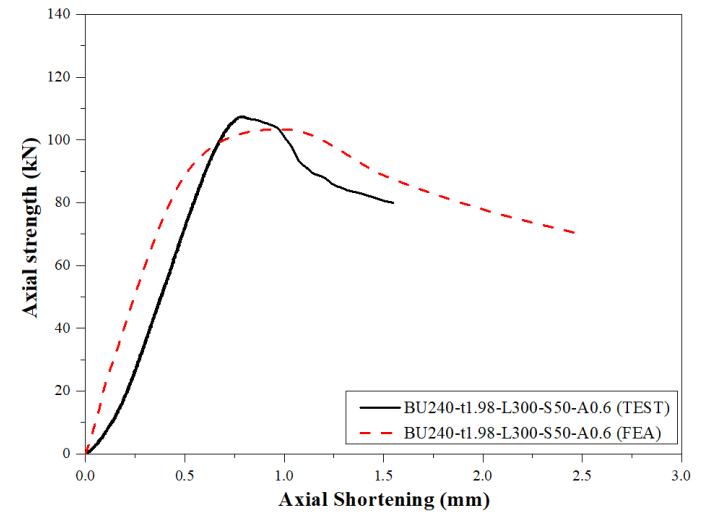
			
(i) Test	(ii) FEA	(i) Test	(ii) FEA
(i) BU240-t1.98-L500-S400-A0.4		(j) BU240-t1.98-L500-S400-A0.4	

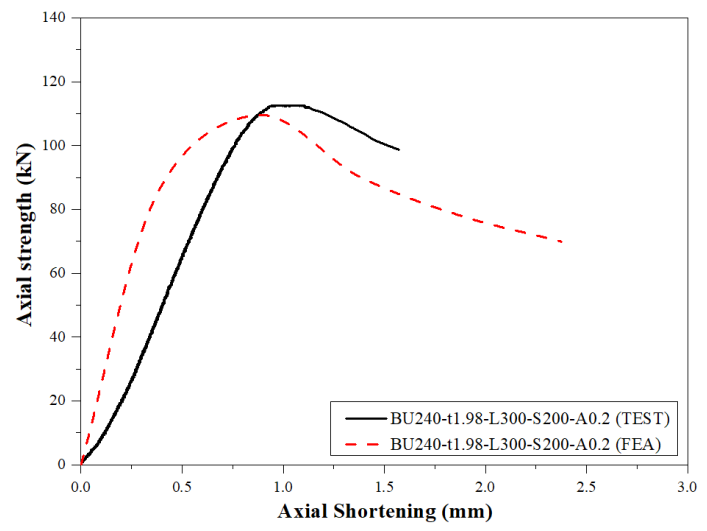
Fig.16 Deformed shapes at failure from experiments and FEA



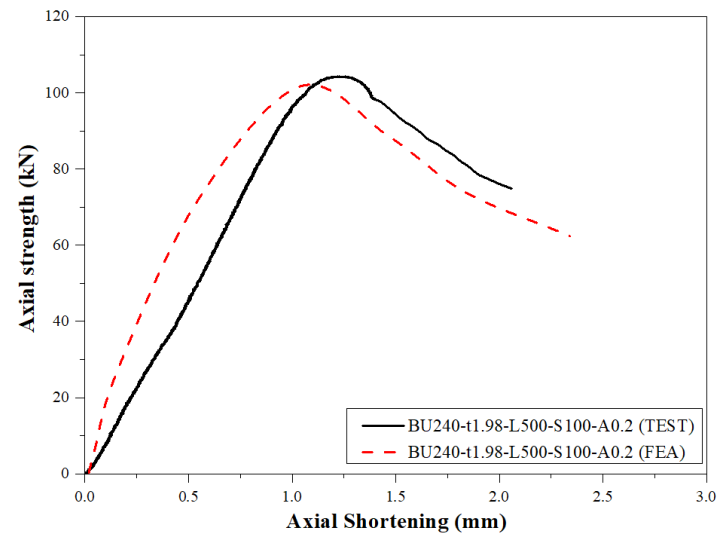
(a) BU240-t1.98-L300-S50-A0.2



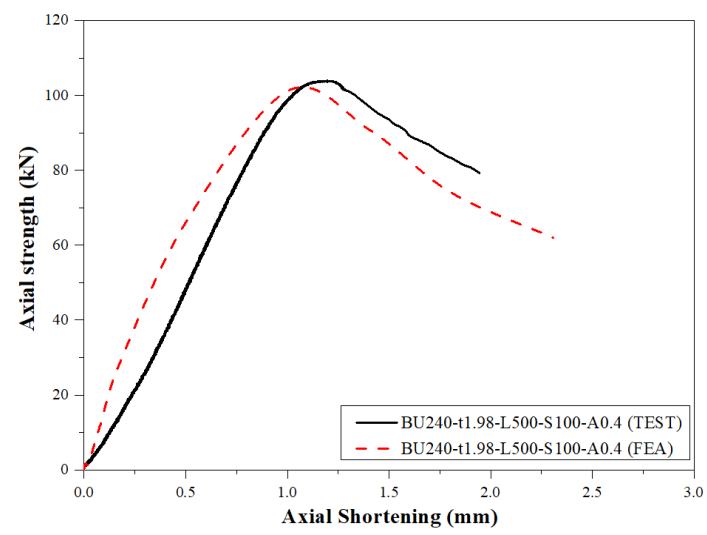
(b) BU240-t1.98-L300-S50-A0.6



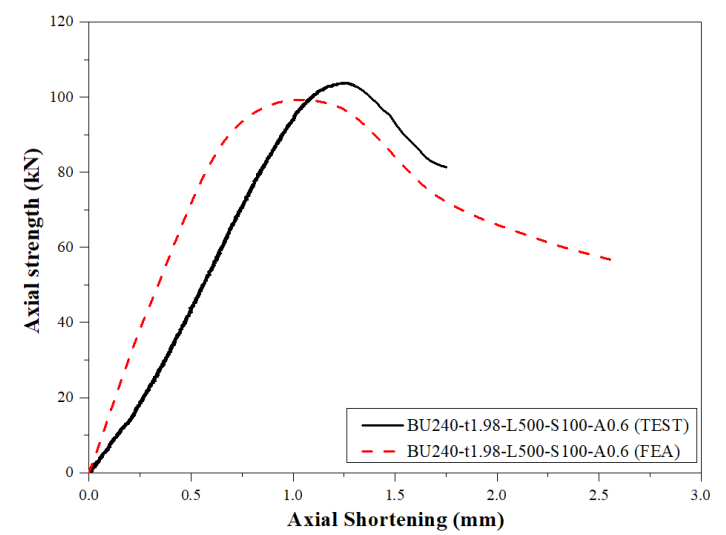
(c) BU240-t1.98-L300-S200-A0.2



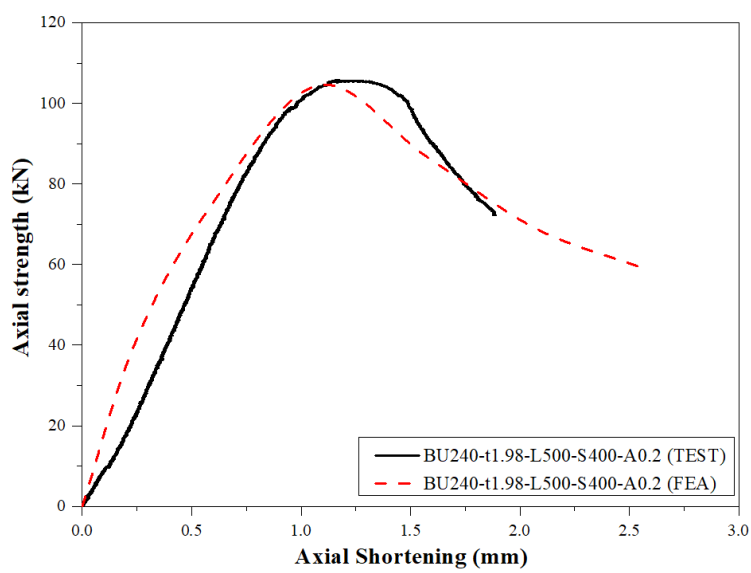
(d) BU240-t1.98-L500-S100-A0.2



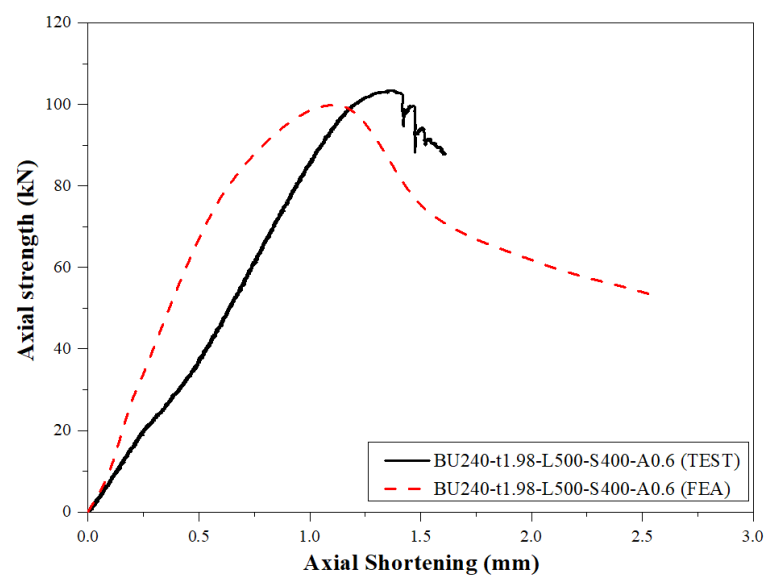
(e) BU240-t1.98-L500-S100-A0.4



(f) BU240-t1.98-L500-S100-A0.6



(g) BU240-t1.98-L500-S400-A0.2



(h) BU240-t1.98-L500-S400-A0.6

Fig.17 Load versus axial-shortening relationship for columns

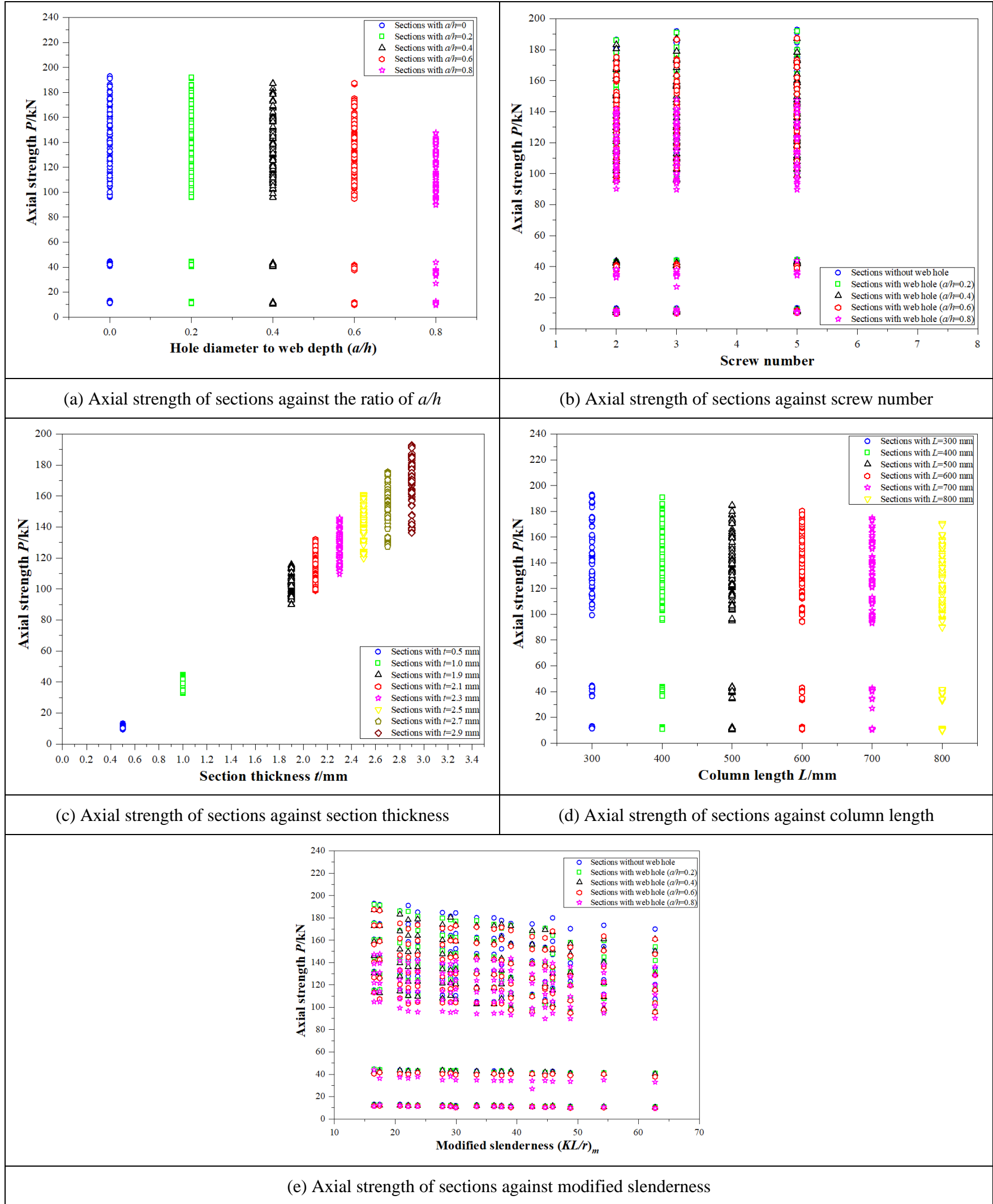


Fig.18 Parametric effects on axial strength of investigated sections

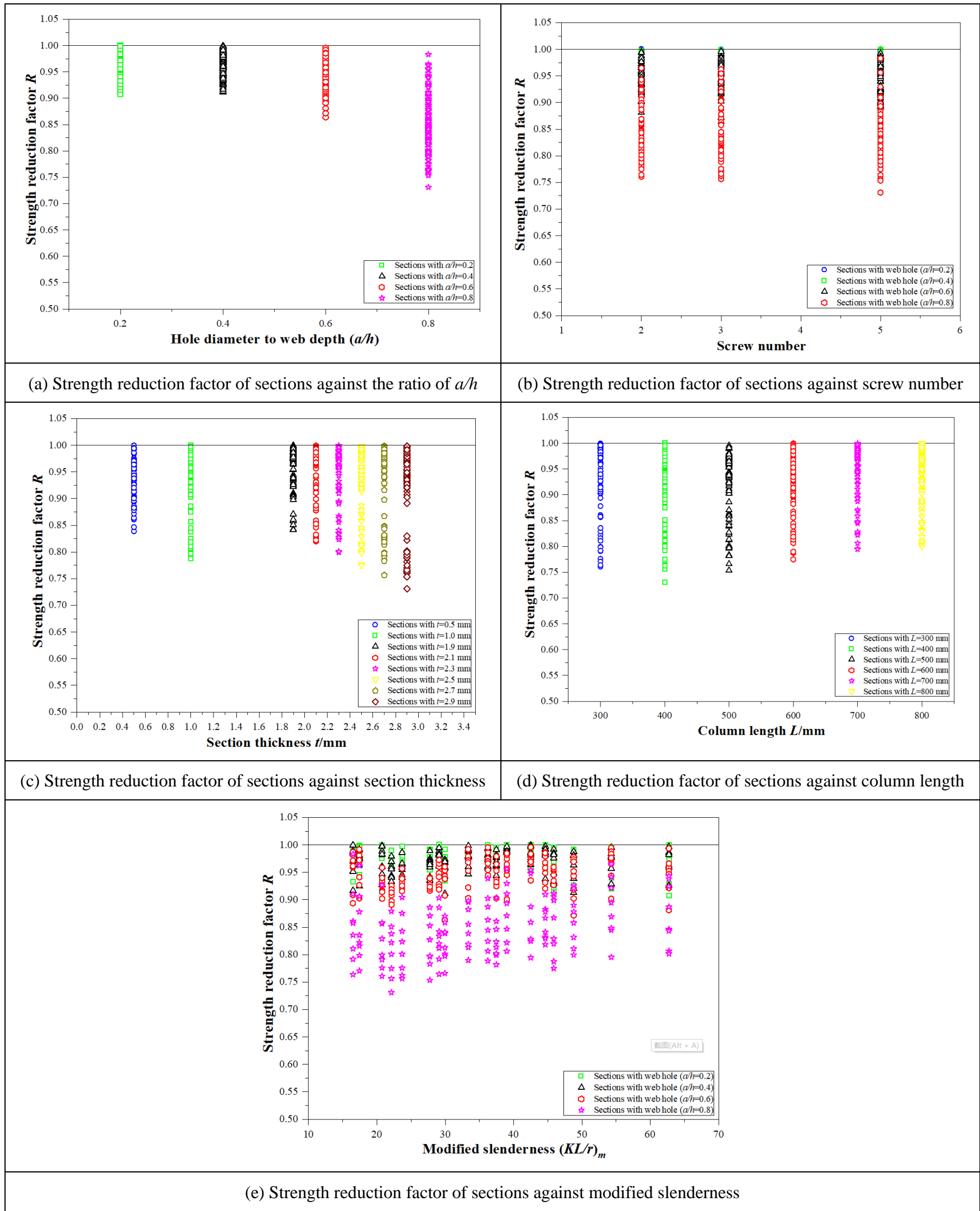


Fig.19 Parametric effects on axial strength reduction factor of investigated sections

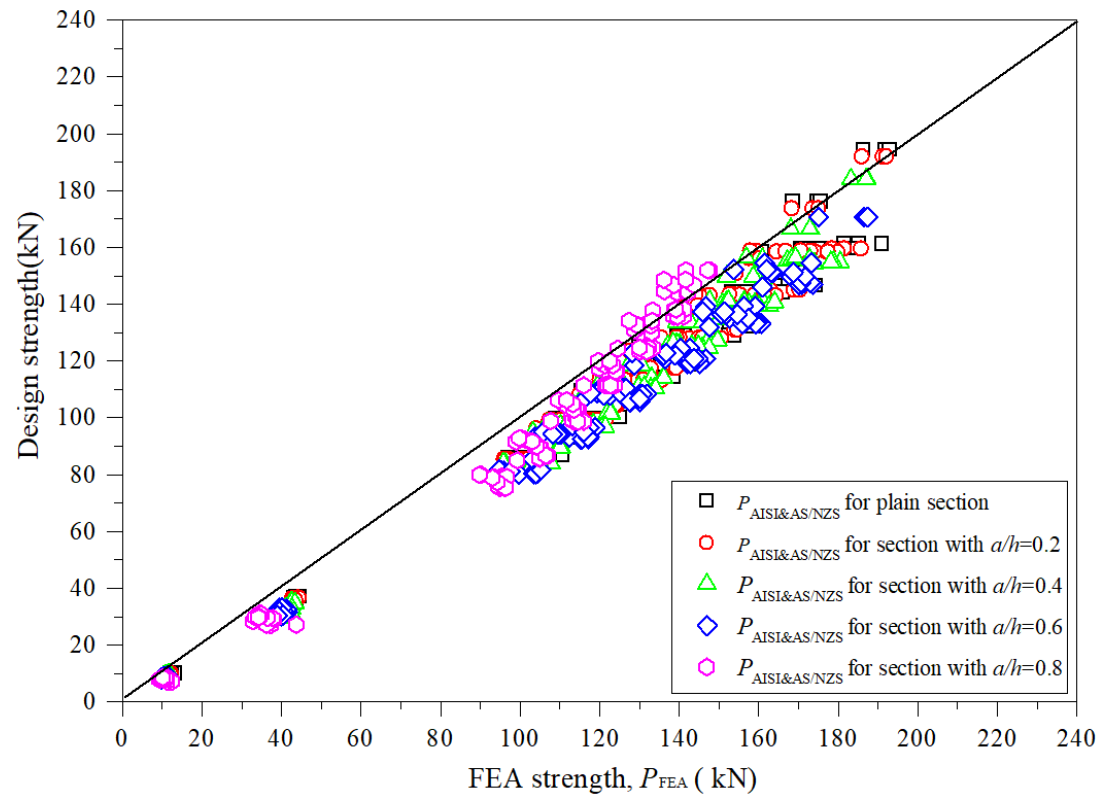


Fig.20 Comparison of axial strengths obtained from the FEA and the current design standards (AISI & AS/NZS)